

Long-Term Evolution in Genetic Programming

Computer Science, Aston University

2pm 7th March 2017

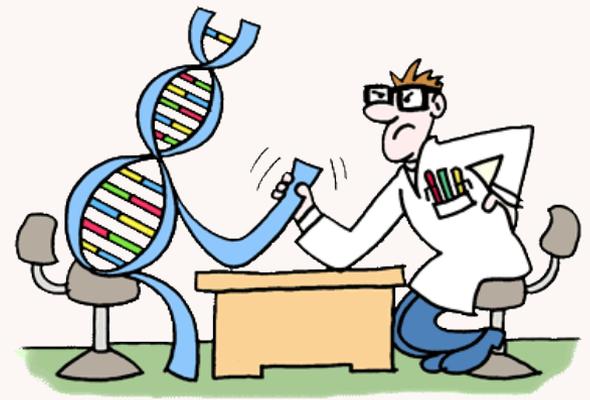
[W. B. Langdon](#)

Department of Computer Science



[GI 2017](#), Berlin
deadline 29th March
GECCO workshop

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\$10000 Human-Competitive
Results



Long-Term Evolution in Genetic Programming

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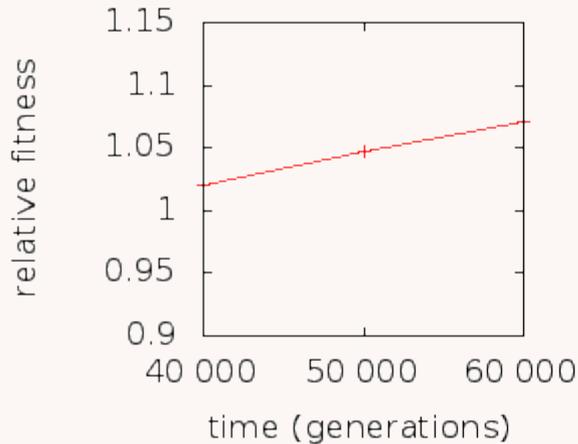


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Genetic Programming and Long-Term Evolution Experiments

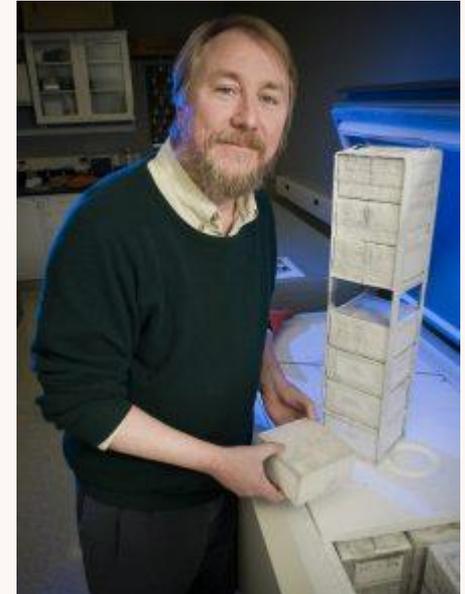
- Evolving Bacteria 60,000 generations v. evolving programs 100,000 generations
- LTEE continuous innovation v convergence
- Intro what is genetic programming:
 - GP is artificial evolution of functions
- Results
 - Increase in code (bloat), end of bloat
 - Theory some true, some less so

Long-Term Evolution Experiment



Mean fitness of nine *E. coli* populations from the LTEE

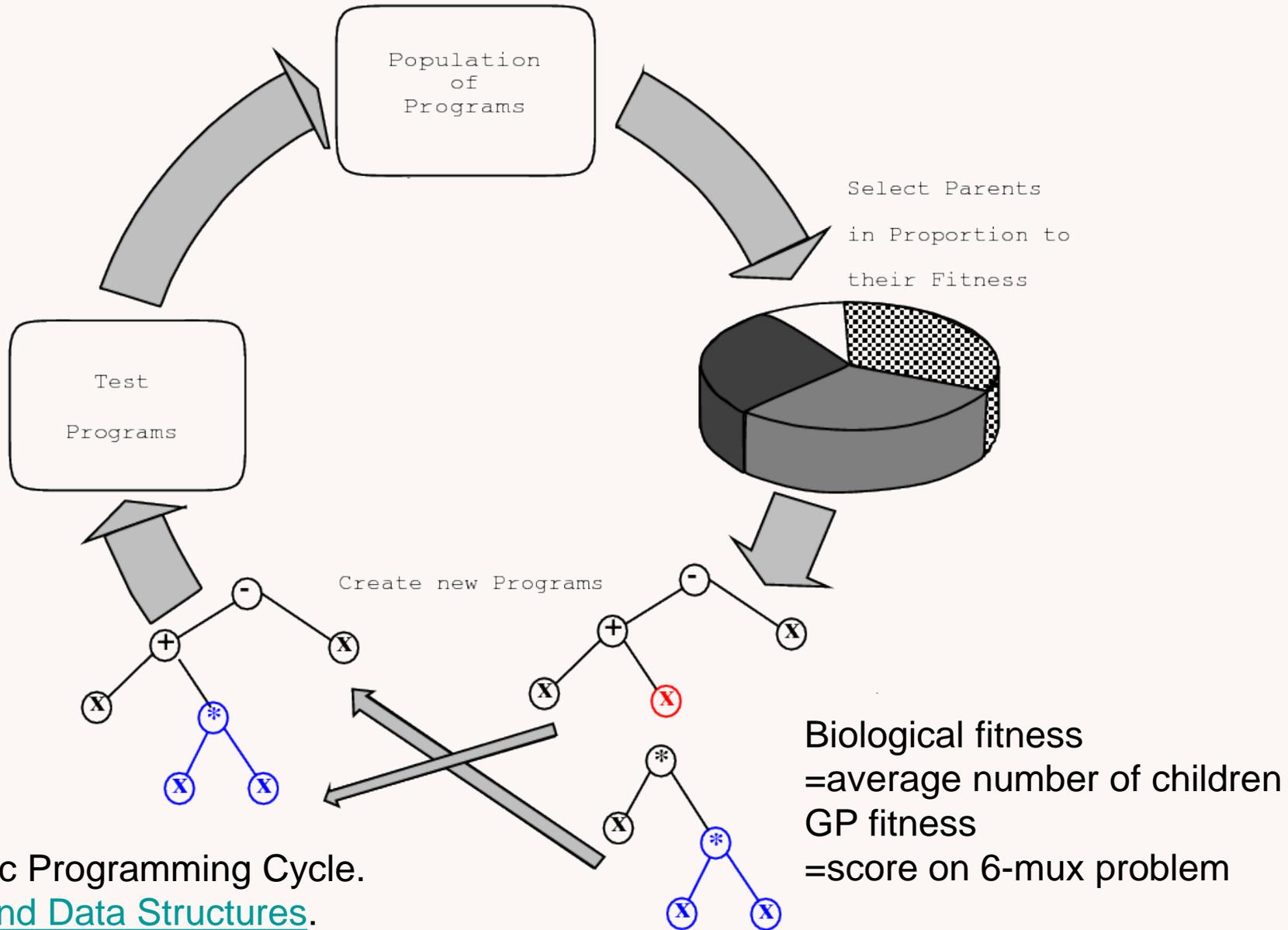
Evolving Bacteria 60,000 generations
Even after 60000 gens fitness still improving



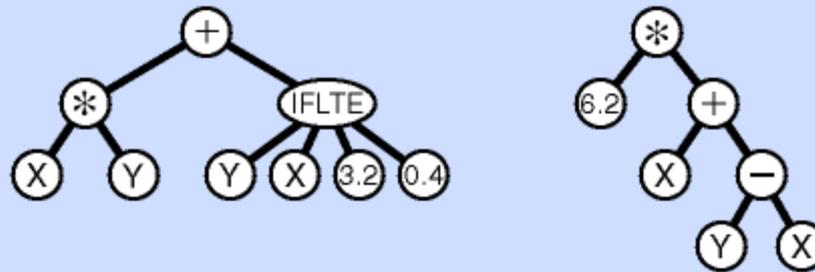
Richard Lenski pulls frozen bacteria cultures out of a freezer 15 Oct 2009

R. E. Lenski *et al.* 2015. [Sustained fitness gains and variability in fitness trajectories in the long-term evolution experiment with *Escherichia coli*](#). Proc. Royal Soc.

Artificial Evolution of Programs



Creating new child programs: crossover



Crossover is symmetric.

That is, on average size after crossover = size before crossover

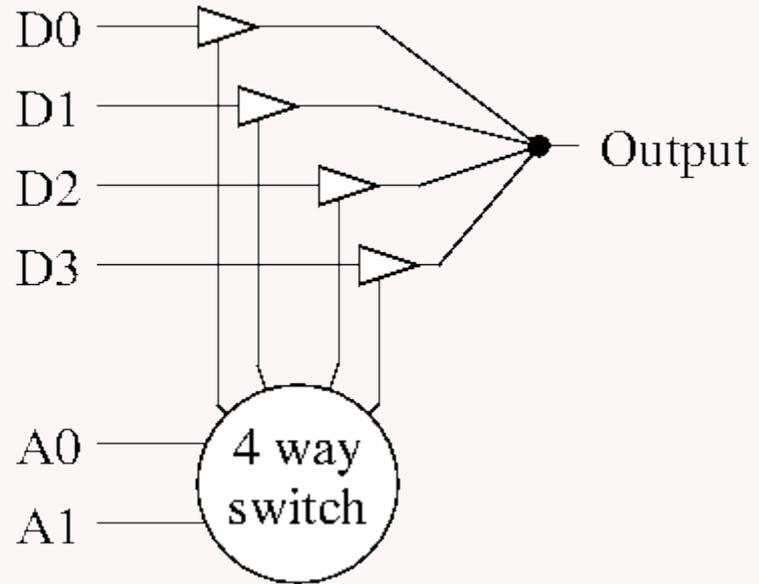
Genetic Programming and Long-Term Evolution Experiments

- GP system able to run thousands of generations. (Do not stop when solved)
 - Expect bloat (tree growth)
 - Compact representation of trees
 - Fast fitness evaluation
- Submachine code genetic programming

GPquick

- GPquick C++, written by Andy Singleton
 - ≈ two bytes per tree node
- Submachine code GP
 - Boolean (bit) problems.
 - AND, NAND, OR, NOR operate simultaneously in parallel on bits in word (e.g. 32 or 64 bits)
 - 64 bit computer can do 64 test cases in parallel

6 Multiplexor



- GP bench mark.
- Six inputs:
 - Use two (D4 D5) as binary number to connect corresponding data lines (D0-D3) to the output
- Test on all $2^6=64$ possible combinations
- Fitness score (0-64) is number correct

Genetic Programming to solve 6-Mux

- Terminals (tree leafs)
 - D0,D1,D2,D3 D4,D5
- Function set: 2 input gates → binary trees
 - AND, NAND, OR, NOR. No side effects
- Generational population of 500 trees
- Tournament selection: choose best of 7
- 100% subtree crossover
- Initially hard limit on tree size (10^6)

Impact of Subtrees

- Subtree like whole tree.
- Output of subtree is via its root node
- **Intron**: subtree which has no effect on overall fitness. I.e. its output does not impact on root node of whole tree.
- **Constant** subtree always has same output, i.e. same output on all 64 test cases.
- Remaining **effective code** has an impact on root node. Typically it is next root node

Example Intron: AND Function



A	B	Out
0	0	0
0	1	0
1	0	0
1	1	1



A	B	Out
0	0	0
0	1	0
1	0	0
1	1	0

Left: two input AND node.

Right: same but input B is always 0.

So output always 0. Input A has no effect.

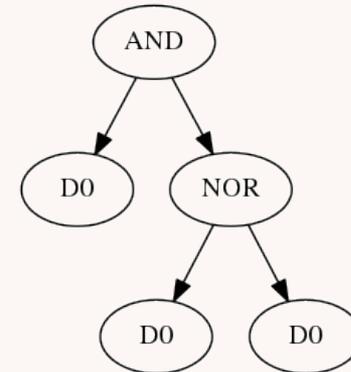
Subtree A is always ignored, even in child.

(NB no side effects)

Constants

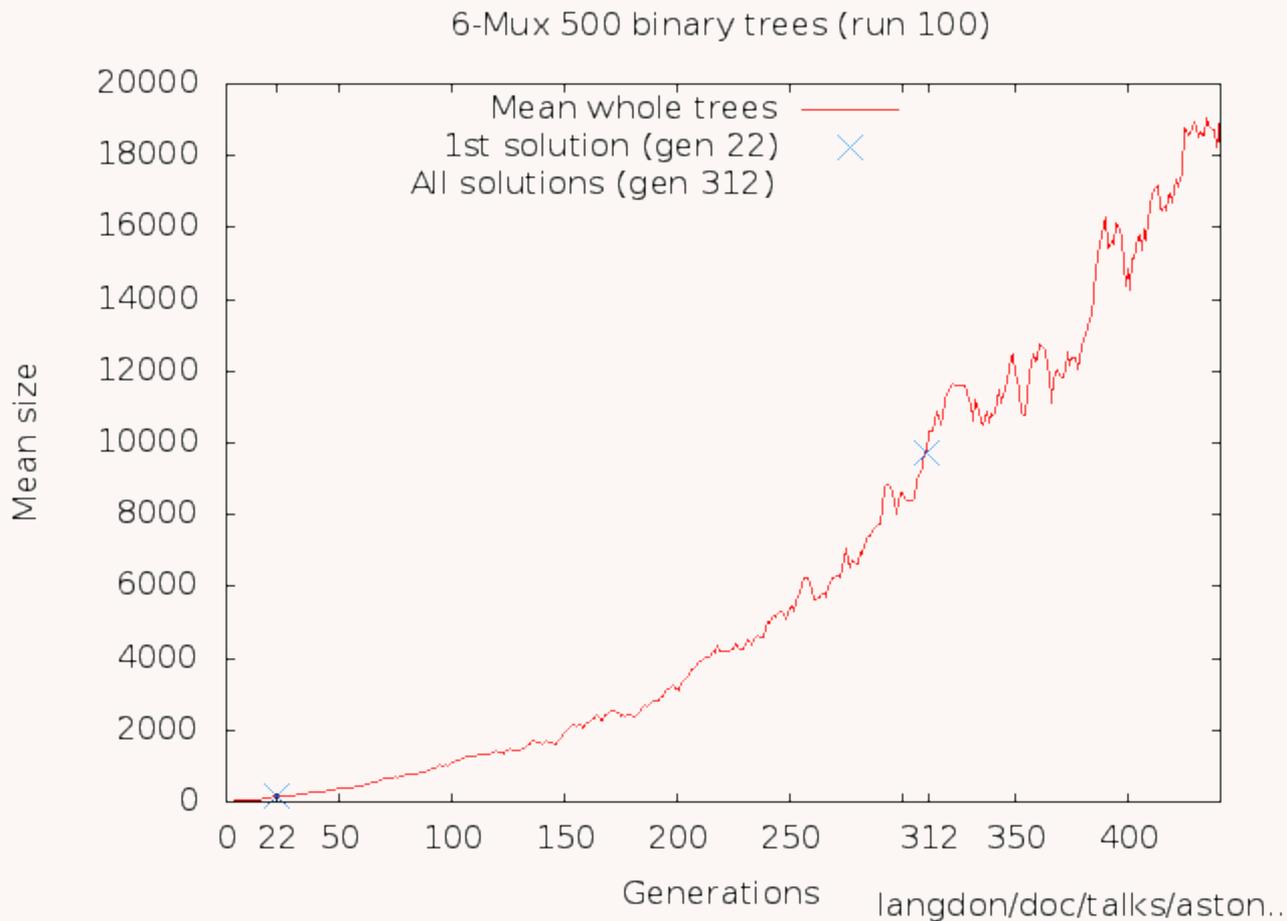
- Two constants: always 0 and always 1 (FFFFFFFFFFFFFFFF).
- E.g. evolve by negating input and ANDing with same input

$$(\text{AND } D0 (\text{NOR } D0 D0)) = 0$$



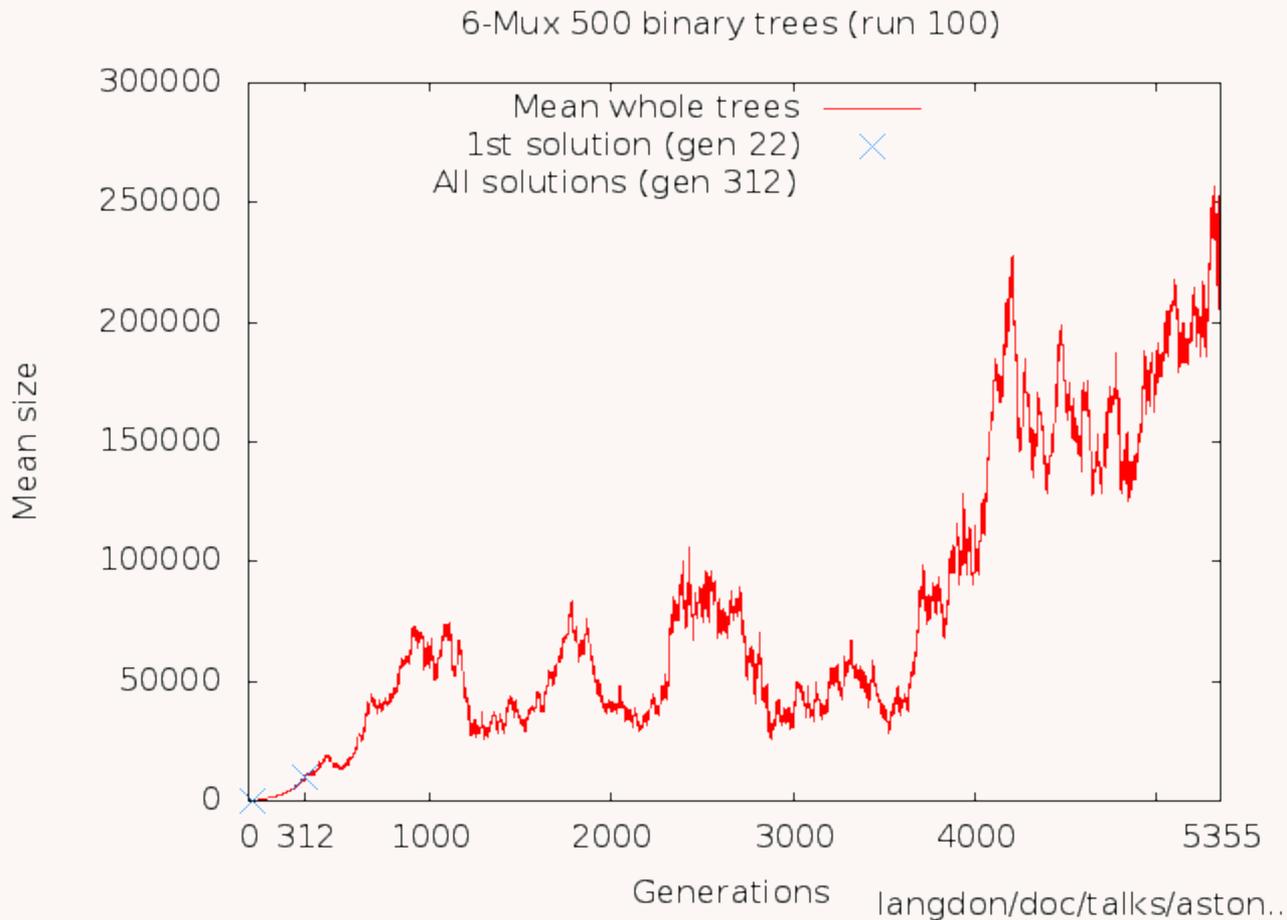
- Constants help form introns but may be disrupted by crossover.
- However large subtrees which always output either 0 or 1 tend to be resilient to crossover

LTEE evolution of size



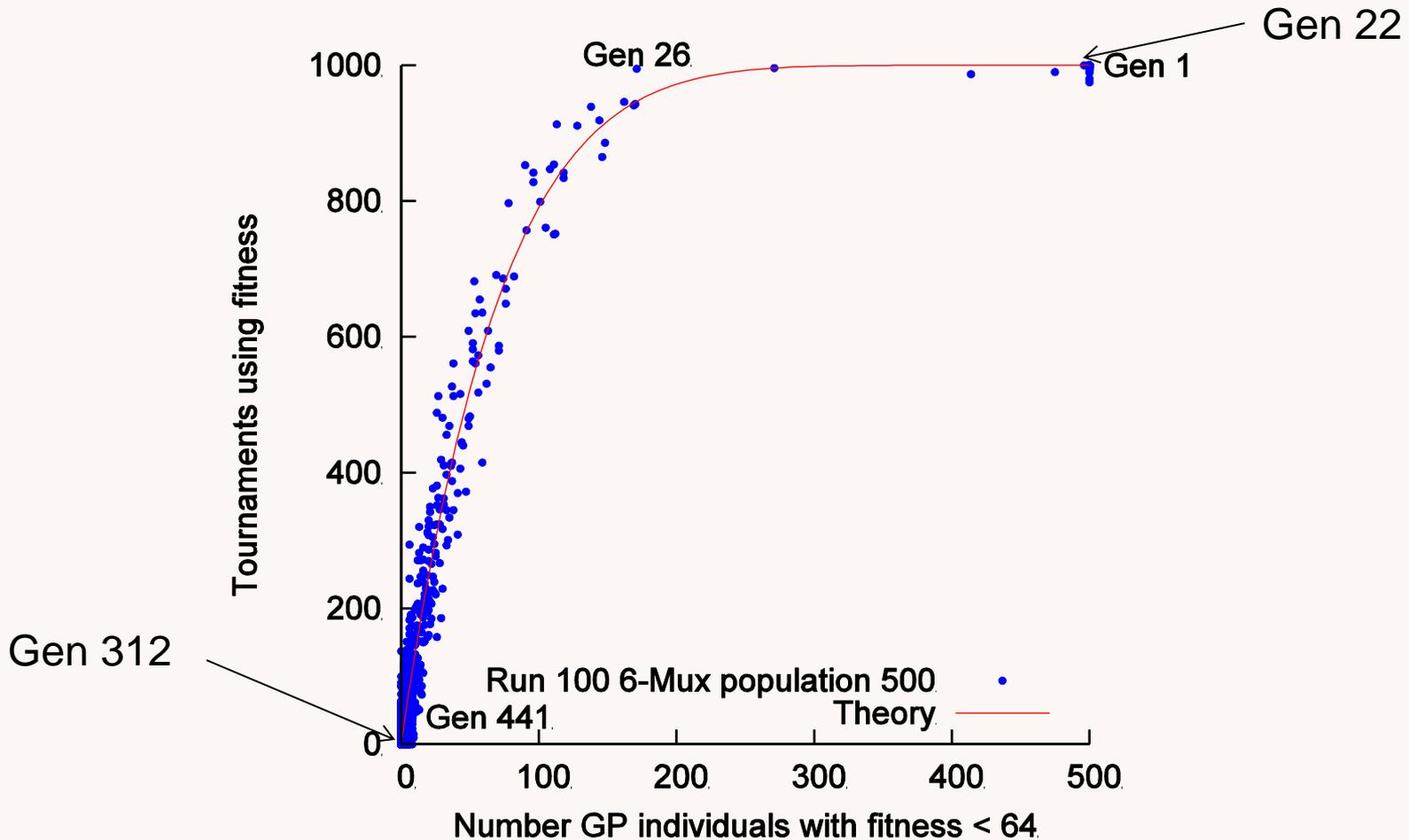
Note evolution continues after 1st solution found in generation 22 and even after 1st population where everyone has maximum fitness (generation 312).

LTEE evolution of size



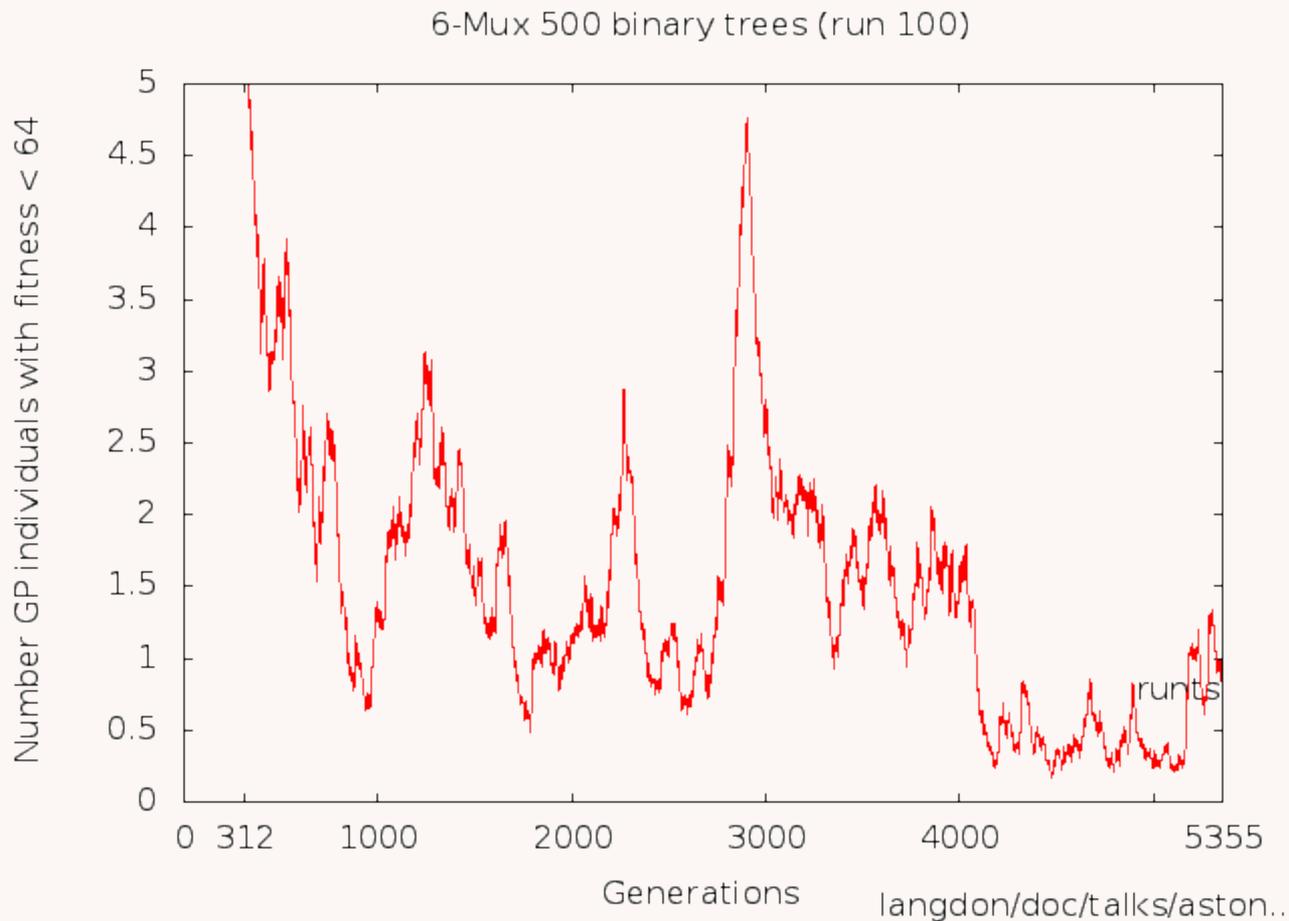
Note evolution continues even after 1st population where everyone has maximum fitness (generation 312) but falls as well as rises.

6-Mux Fitness Convergence



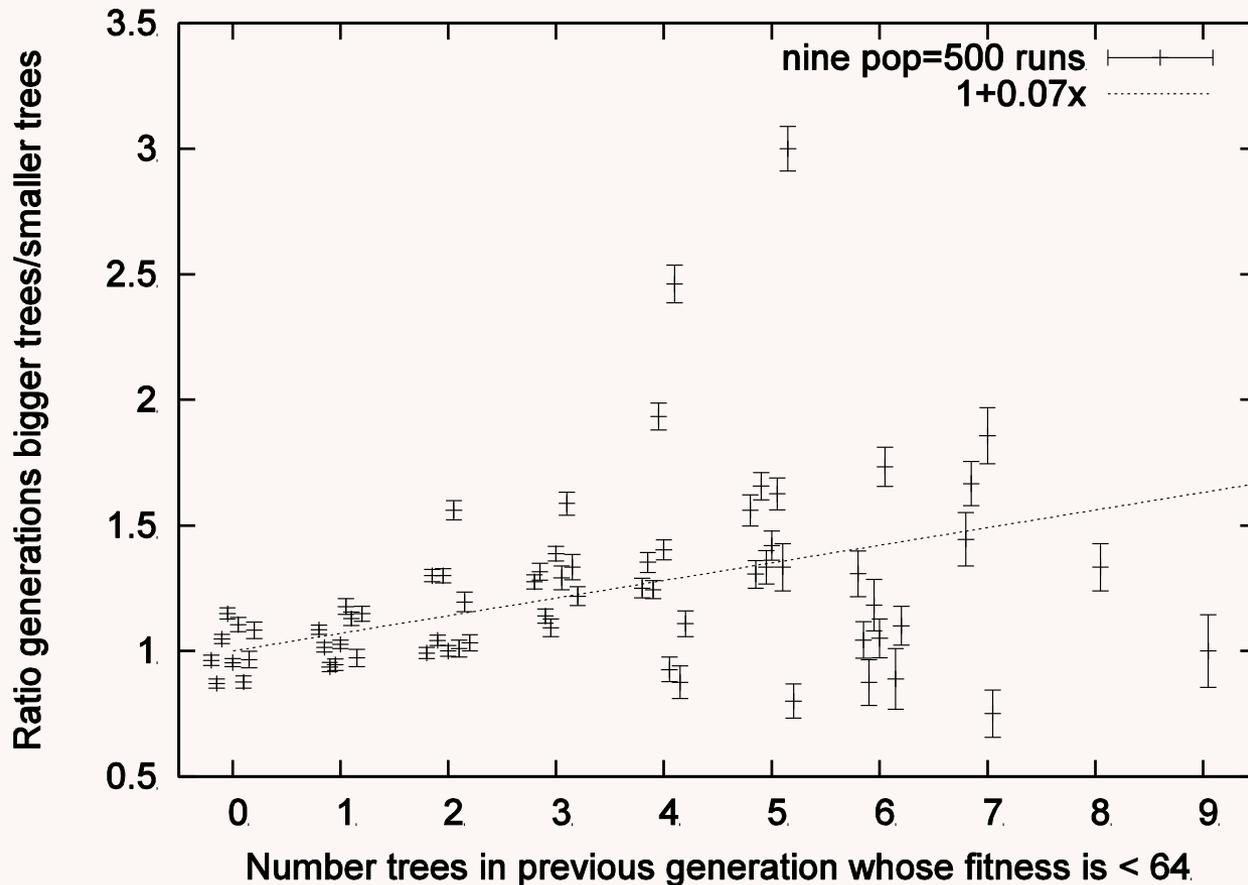
Theory $y = 2\text{popsize}(1-(1-x/\text{popsize})^7)$ matches experiment

6-Mux Fitness Convergence



Plot smoothed by taking running average over 30 generations

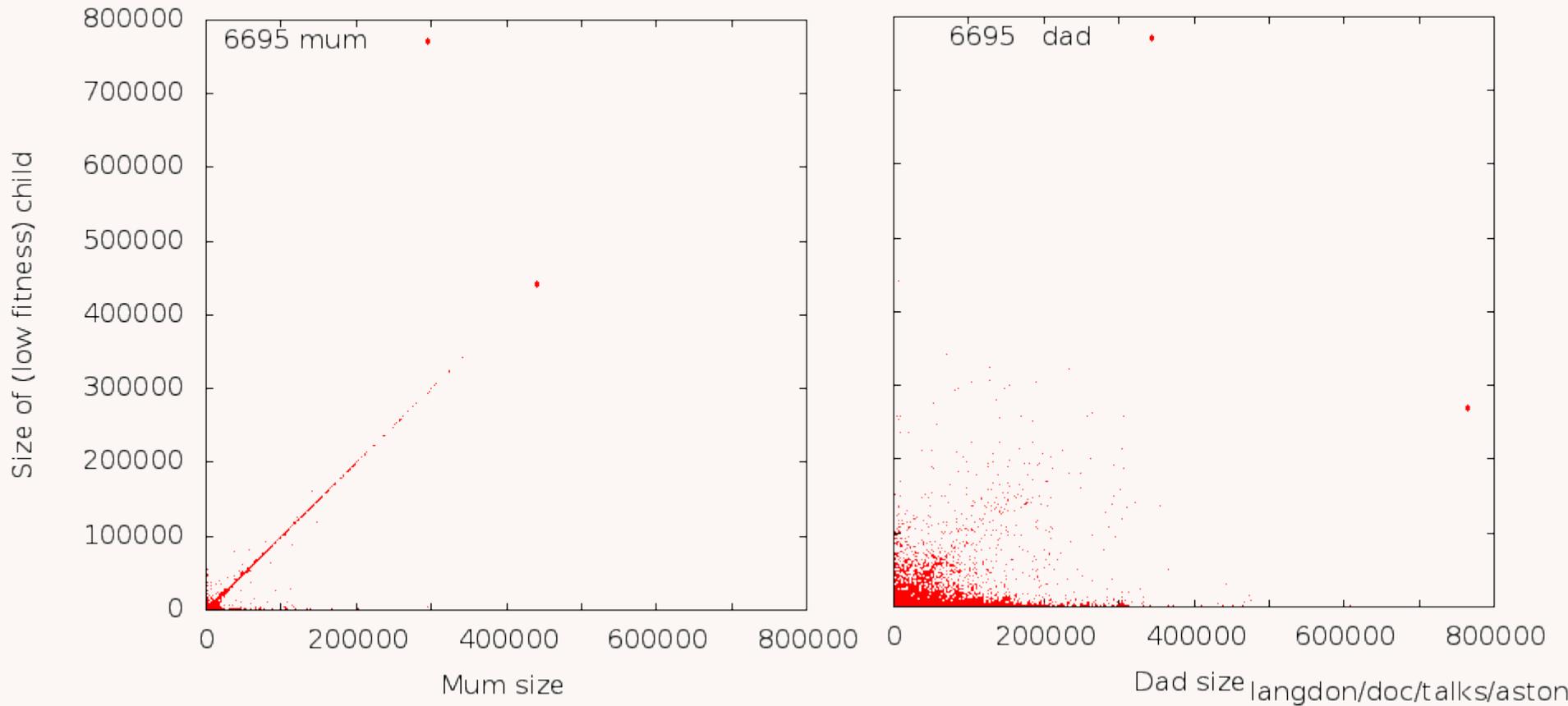
Runts Drive Evolution



Don't plot ratio if less than 5 data

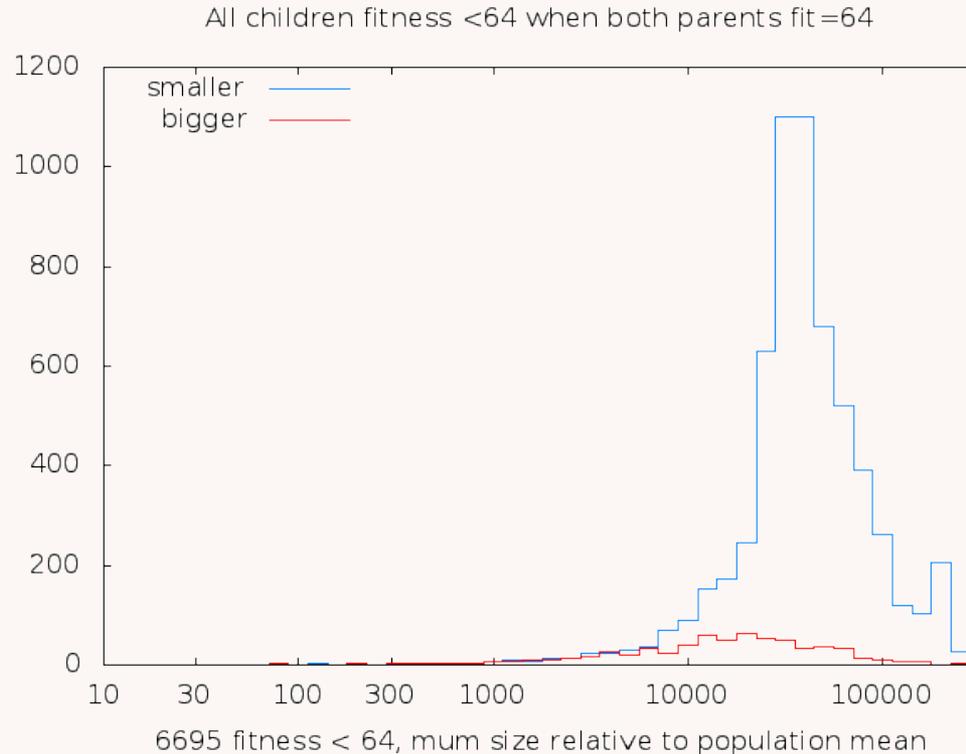
Importance of Mothers

All children fitness <64 when both parents fit=64 All children fitness <64 when both parents fit=64



Size of poor fitness children closely related to parent who they inherit root from (mum).

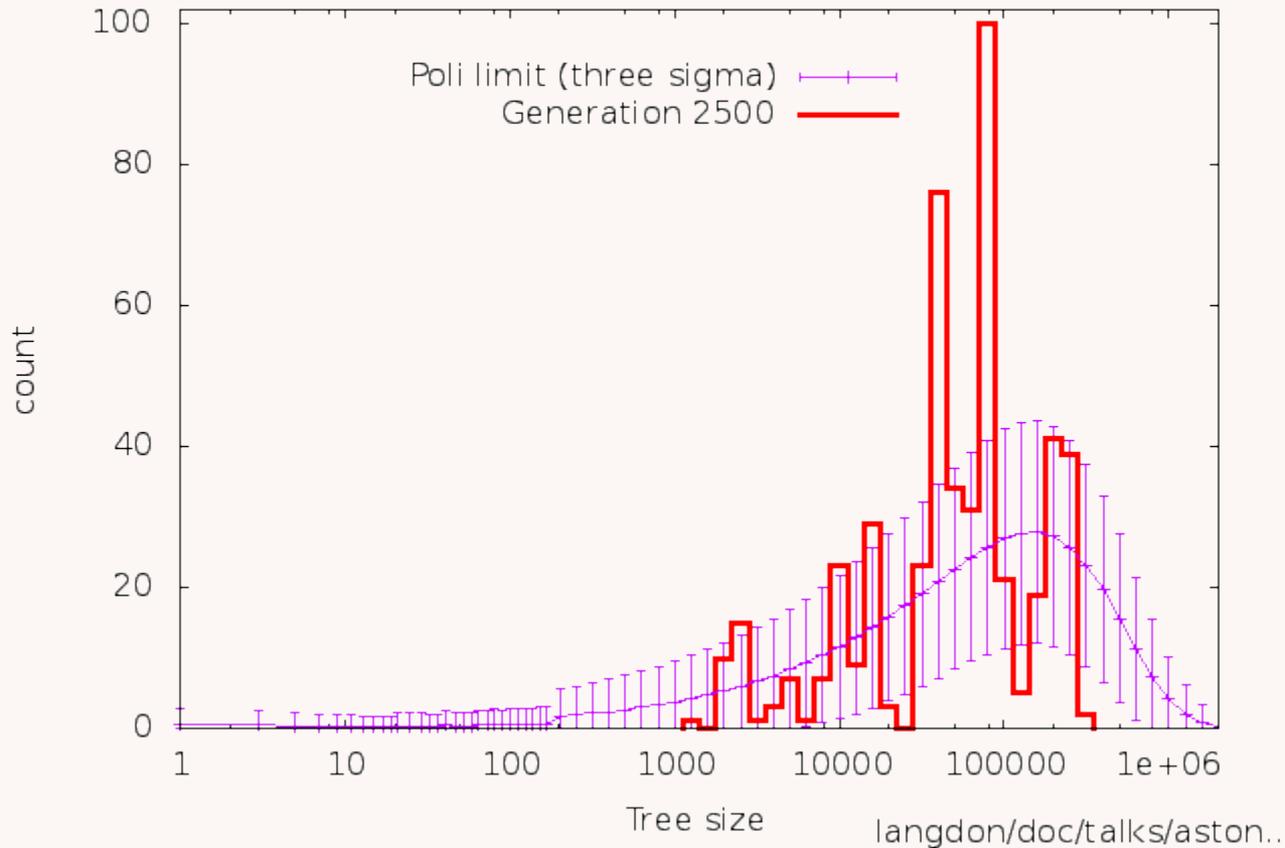
A few runts drive size increase



- Many mothers of runts are smaller than average (blue)
- Selection removes all low fitness children (runts)
- Since these are smaller than average
- Although there is noise, on average size increases

Testing Theory

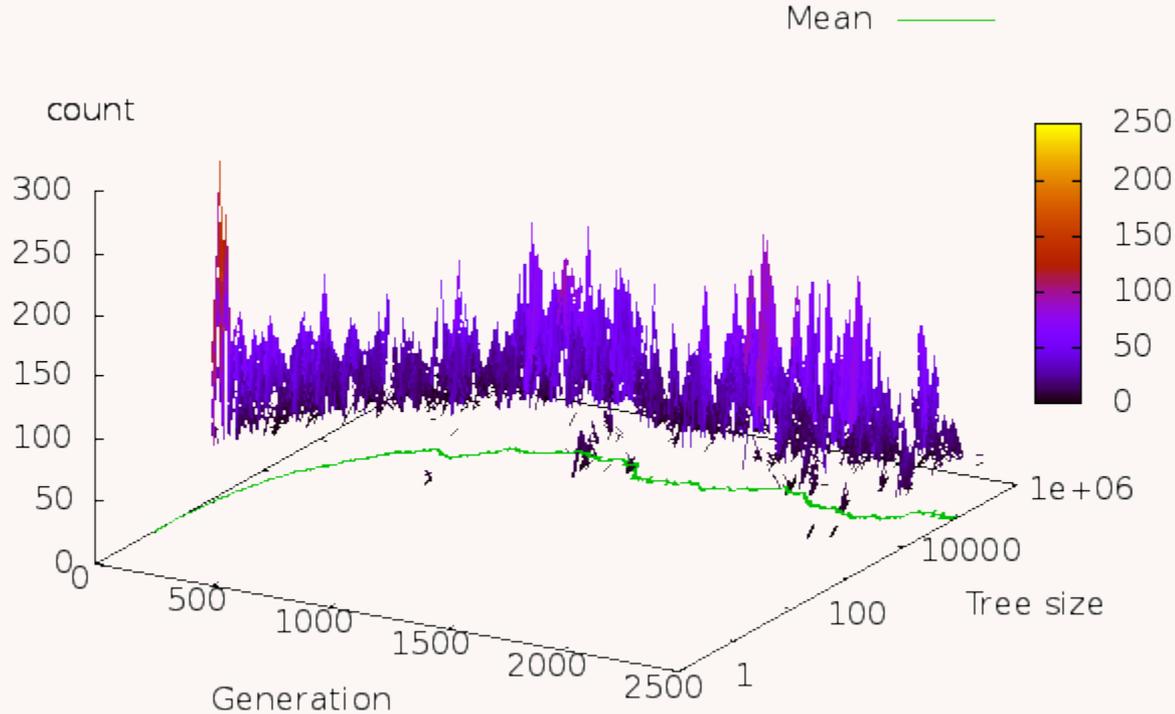
6-Mux 500 binary trees (run 100 at Gen 2500)



- Theory assumes crossover only (no selection). In earlier work distribution of sizes converged to limit rapidly.
- Selection caused by a few runts modifies size distribution

Testing Theory

6-Mux 500 binary trees (run 100 up to Gen 2500)



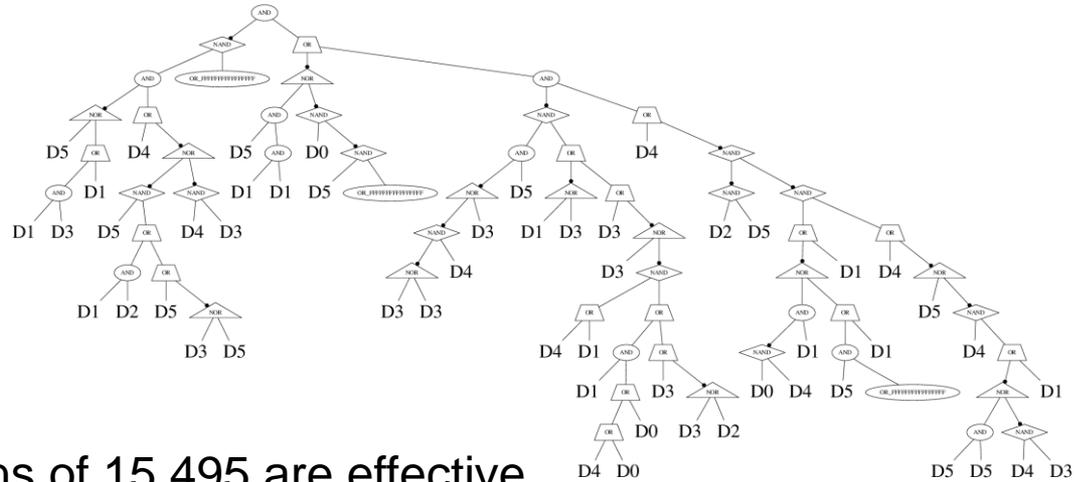
- Same as testing theory plot but do every generation
- Colour only part of histogram $\geq 3\sigma$
- Small tree and large tree tails ok (not coloured)

CREST Convergence in Genetic Programming

- GP genotypes typically do not converge. Even after many generations every tree in the population is different, BUT...
- Every (or almost all) trees give the same answers (phenotypic convergence)
- Effective code, i.e. code to solve problem, does converge.

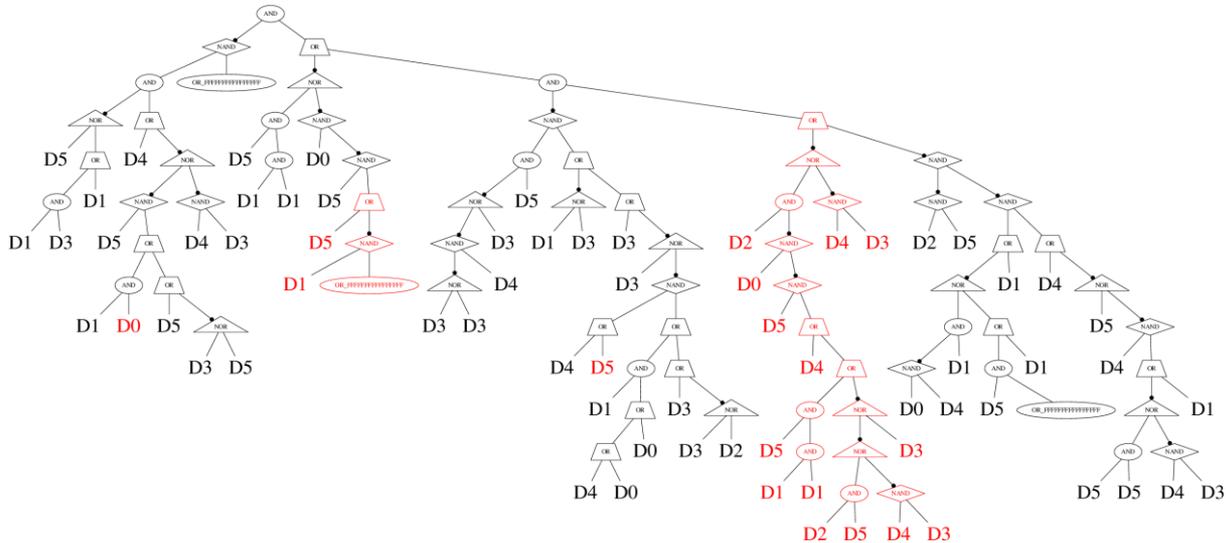
Effective code other runs converges differently

Convergence of typical Effective Code



Gen 400

Only 111 instructions of 15,495 are effective



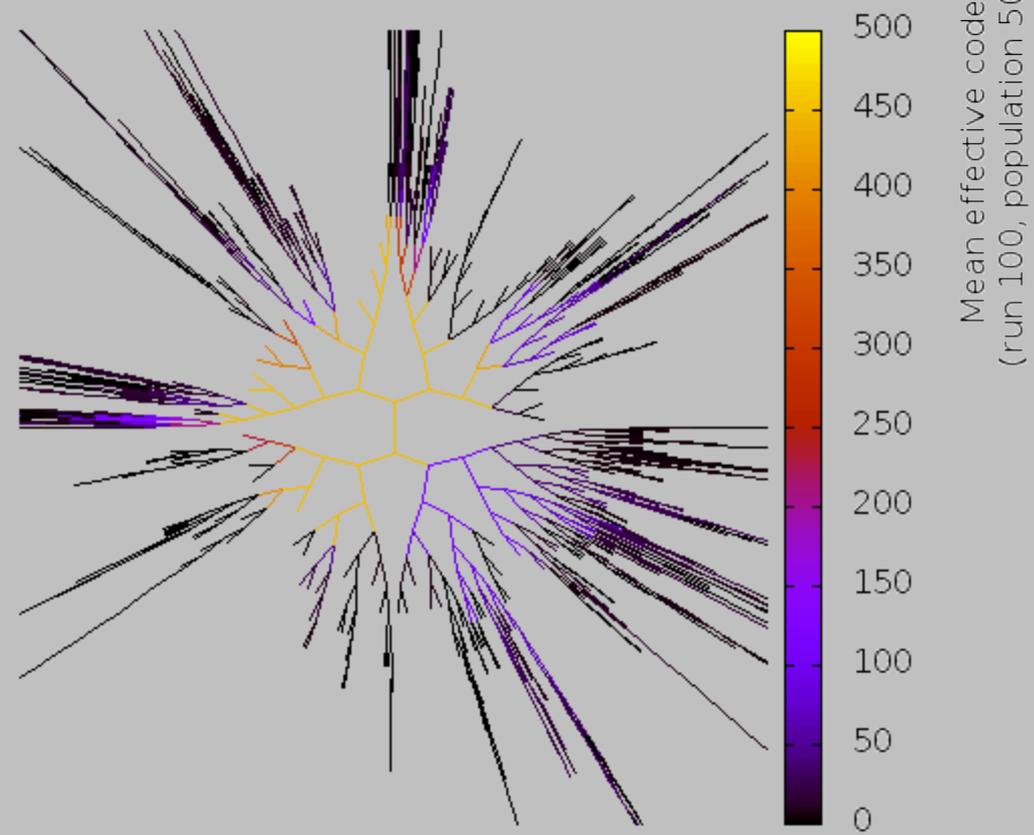
Gen 500

Only 141 instructions of 16,831 are effective

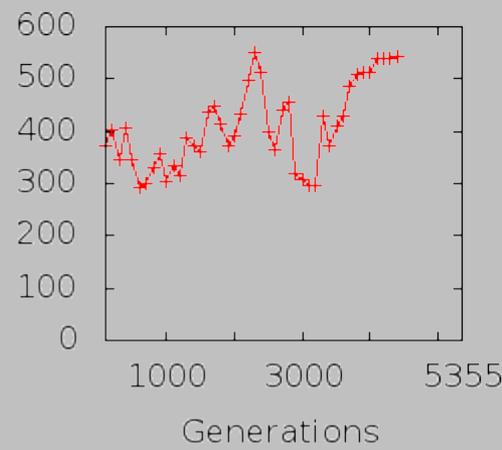
Tree drawing code lisp2dot.awk

Convergence of Effective Code

6-Mux (binary tree) population at generation 100



Mean effective code (run 100, population 500)

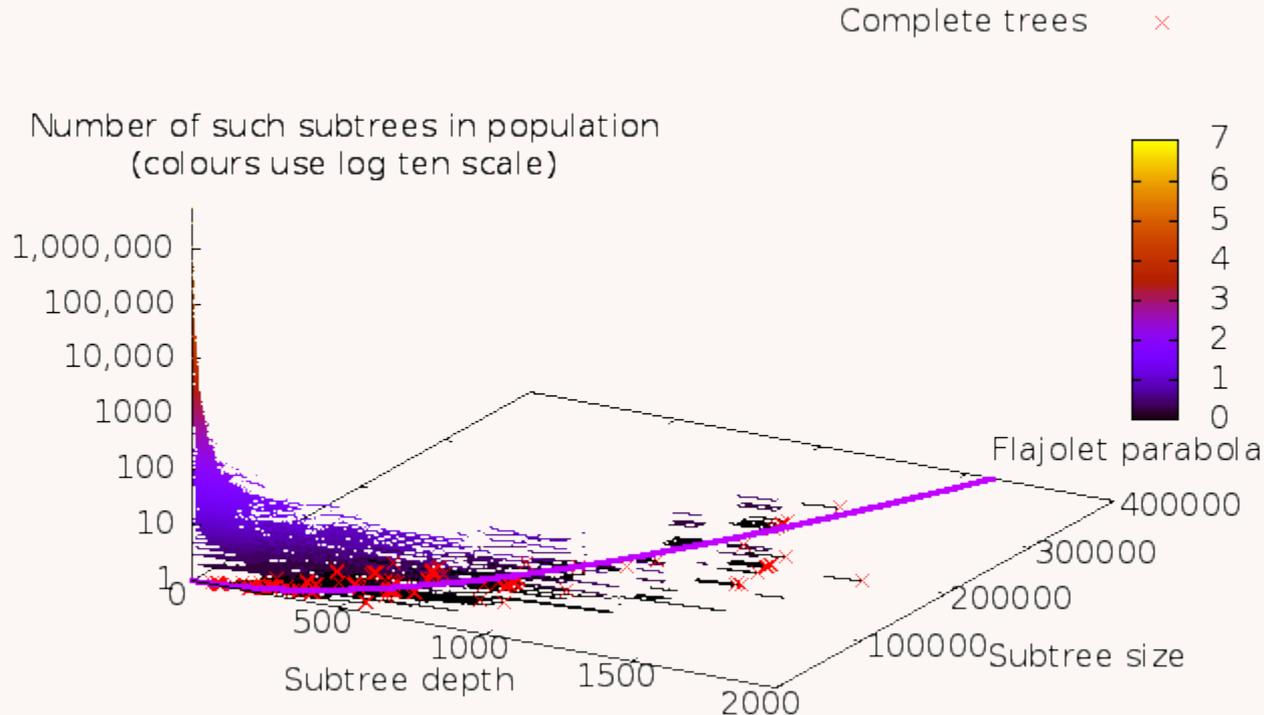


Effective code only. Yellow highly converged.
 Black unique code

Circular lattice code gp2lattice.awk

Shapes of Evolved Trees

6-Mux 500 binary trees (run 100 Gen 2500)



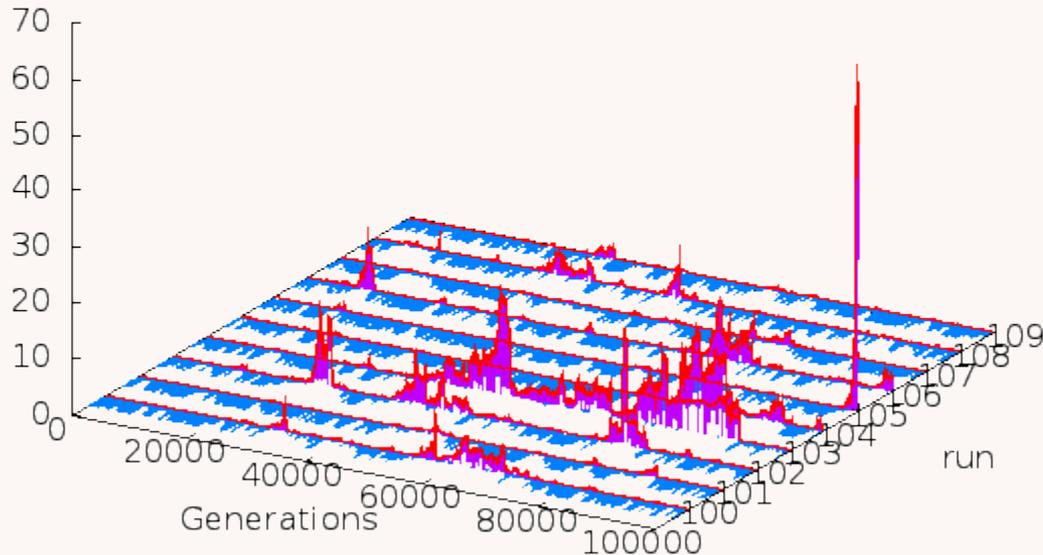
Both whole trees × and subtrees lie near Flajolet $\text{Depth} \approx 2 \left(\frac{\pi \text{size}}{2} \right)^{1/2}$ limit¹ for random trees

Bloat limited by Gambler's ruin

- Tiny fraction of disrupted (low fitness) children sufficient to drive evolution towards every bigger trees.
- As trees get bigger chance of hitting protected effective code near root node falls.
- In a finite population eventually no child will be disrupted.
- Size, without fitness, difference just wanders at random.
- Crossover cannot escape from population of tiny trees.
- So we have a lower limit on the random fluctuation.
I.e. a Gambler's ruin.
- But wondering towards lower limit will re-establish the conditions for bloat.
- Very approximate limit on tree size:
tree size \approx number of trees \times core code size

Bloat limited by Gambler's ruin

Mean size (millions). Ten runs, population 50 trees

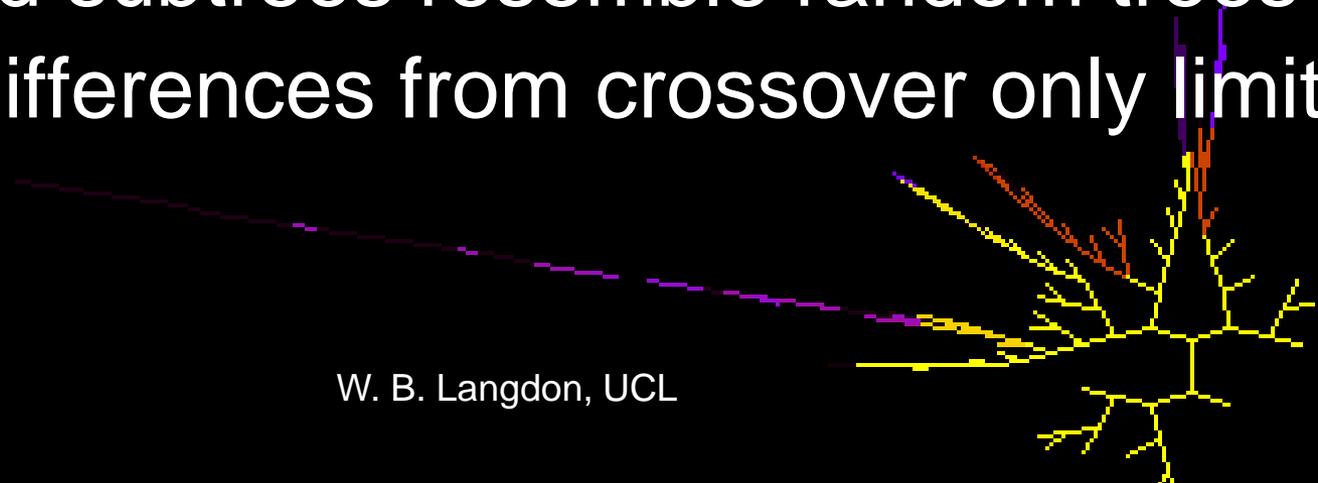


- tree size \approx number of trees \times core code size
- tree size $\approx 50 \times 497 \approx 25000$
- Across ten runs and 100,000 generation, median mean size 42,507 (smallest tree in pop size=10,513)

In all ten runs the whole population repeatedly collapses towards smaller trees

Conclusions

- Studied long term evolution (>>any other GP)
- 100s gens where everyone has same fitness
- No selection to drive size increase
- Gambler's ruin with size falling as well as rising
- Evolved effective code surrounded by ring of sacrificial constants and introns
- Trees and subtrees resemble random trees
- But still differences from crossover only limit



END

<http://www.cs.ucl.ac.uk/staff/W.Langdon/>

<http://www.epsrc.ac.uk/> 

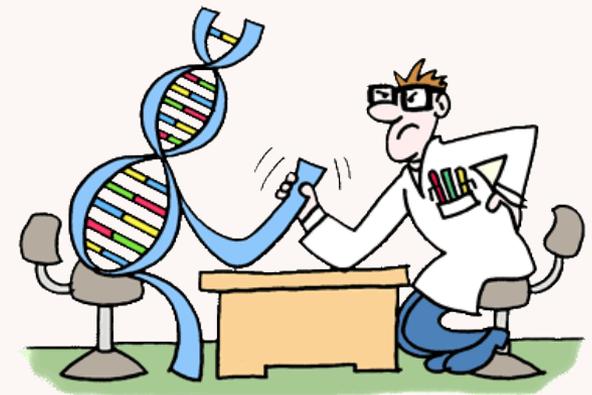
GECCO-2017 15th-19th July 2017 in Berlin

- Genetic Improvement workshop at Submissions by **29th March**
<http://geneticimprovementofsoftware.com/>
- Total \$10 000 prizes for human competitive results. Entries by 7th June
<http://www.human-competitive.org/call-for-entries>

Genetic
Improvement
2017

[GI 2017](#), Berlin,
15/16 July 2017
GECCO workshop

[Humies](#)
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Results



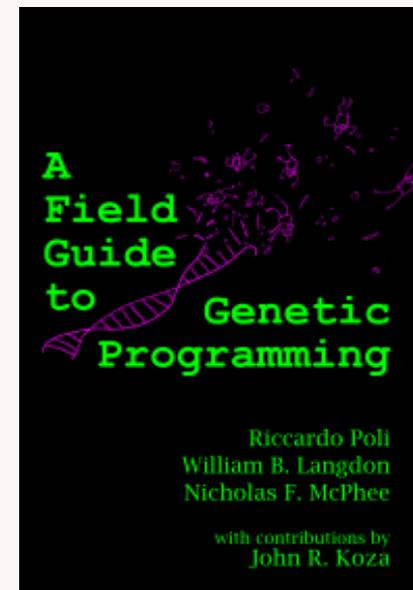
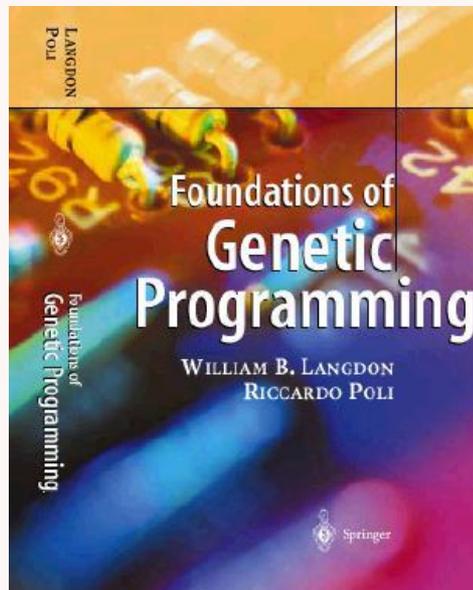
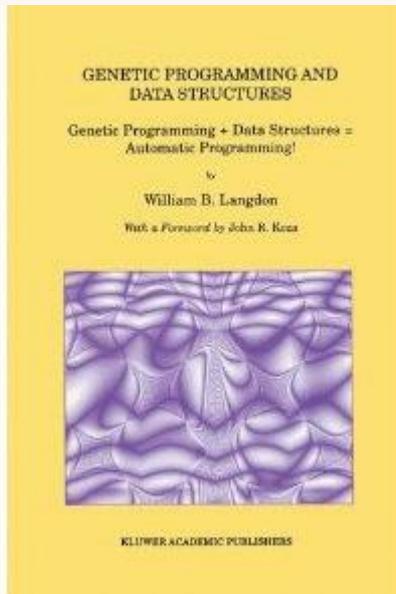
Genetic Programming



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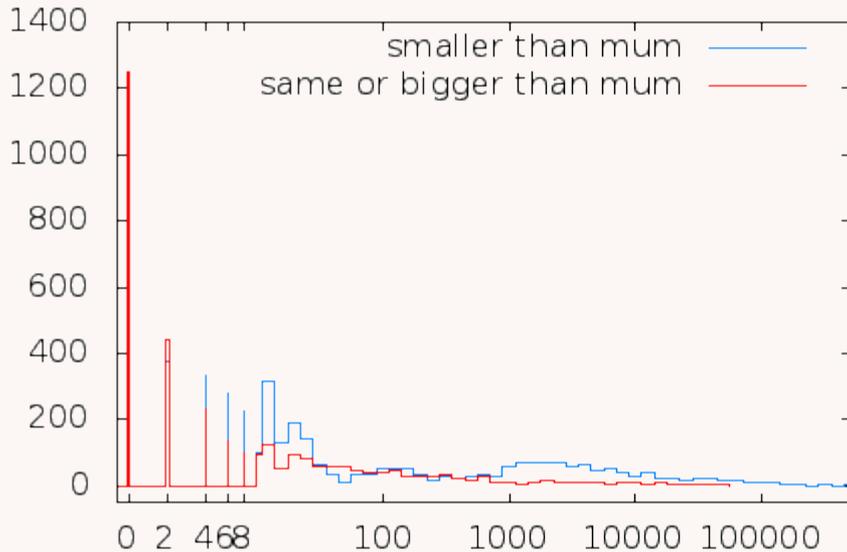
CREST

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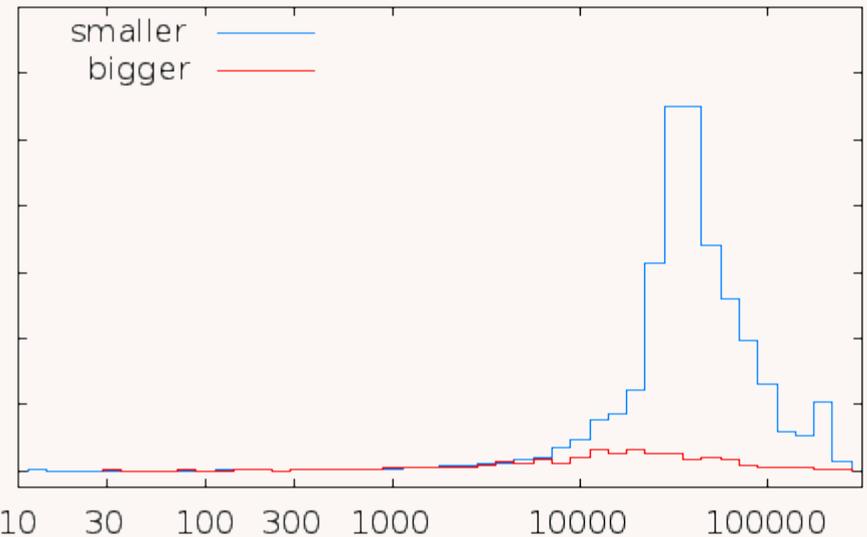
Importance of Mothers

All children fitness < 64 when both parents fit = 64



6695 fitness < 64 , Change in size from mum

All children fitness < 64 when both parents fit = 64



6695 fitness < 64 , mum size relative to population mean

- Although many runts are smaller than their mum,
- many mothers of runts are smaller than average.
- Selection removes all low fitness children,
- Since these are smaller than average, the average size increases

The Genetic Programming Bibliography

<http://www.cs.bham.ac.uk/~wbl/biblio/>

11322 references

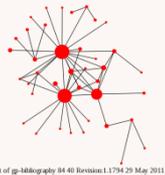
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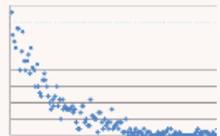
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