

Genetic Improvement of Data gives double precision $\text{invsqrt} \frac{1}{\sqrt{x}}$

GI @ GECCO 2019 workshop, Saturday 13 July, Prague. [doi:10.1145/3319619.3326800](https://doi.org/10.1145/3319619.3326800)

W. B. Langdon

Department of Computer Science



Genetic Improvement of Data gives double precision invsqrt $\frac{1}{\sqrt{x}}$

W. B. Langdon

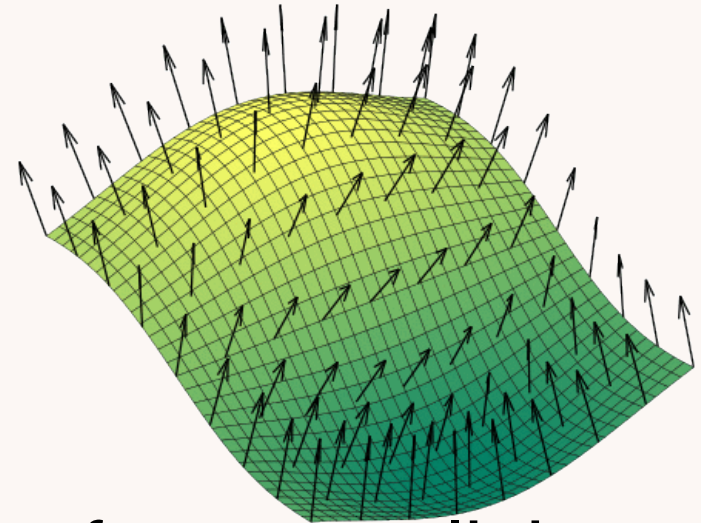
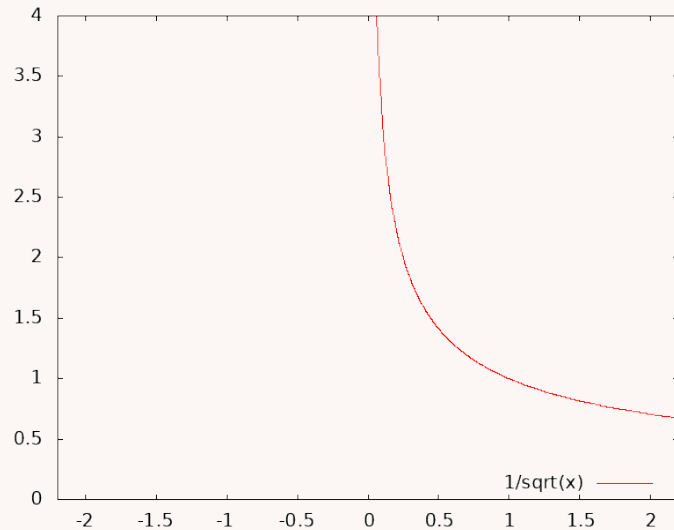
Department of Computer Science



Fluid Genetic Improvement Programming

- Invsqrt $\frac{1}{\sqrt{x}}$ inverted square root
- New type of Genetic Improvement
- Update fluid embedded literals i.e. data
 1. New functionality
 2. Better non-functionality (e.g. faster)?
- Why
 1. FGIP is a new way to do GI, tackle data driven code
 2. Minimal code changes may be more acceptable?

Why invsqrt $\frac{1}{\sqrt{x}}$



- Reciprocal of square root for normalising vectors. E.g. in games, image processing and neural networks
- Before hardware support in GPU invsqrt was computationally heavy. Hence Quake used own approximation, Quare root.

FGIP New type of Genetic Improvement

- New functionality via data changes
 - RNAfold better predictions
 - New maths functions, e.g. convert \sqrt{x} into $\frac{1}{\sqrt{x}}$
- Can we do non-functionality (e.g. faster)?
- How is this different from:
 - Deep parameter tuning? Change functionality
 - No mutation testing
 - Emphasis on data rather than values in code
 - Scale: hundreds even thousands of values
 - Multiple examples

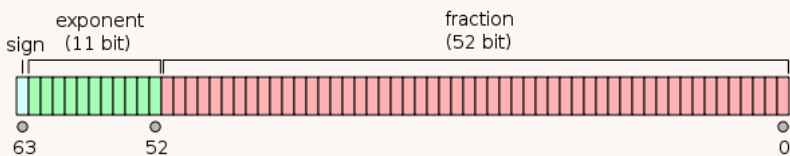
Maintaining Embedded Constants

- [EuroGP 2018](#)
 - RNAfold 7000 lines of code 50000 numbers
 - On average better predictions of RNA folding.
 - Shipped since 2.4.7
- CMA-ES evolves data in a GNU C library sqrt to give new functionality with double precision accuracy. sqrt converted to
 - cube root, cbrt
 - square root converted to \log_2 (poster monday)
 - **invsqrt** $\frac{1}{\sqrt{x}}$
 - division less division

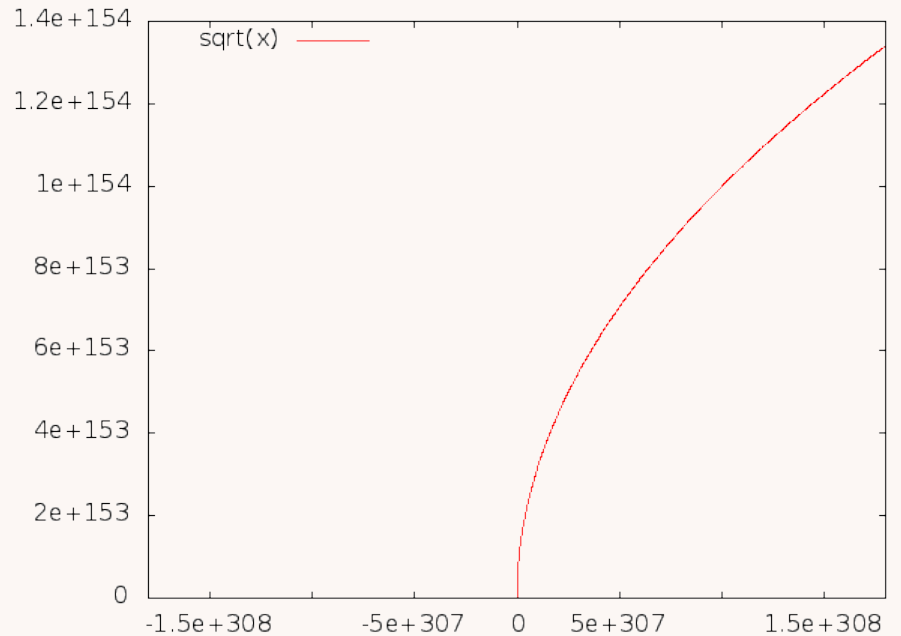
Use CMA-ES to
convert sqrt into $\frac{1}{\sqrt{x}}$

By updating table of
512 floats

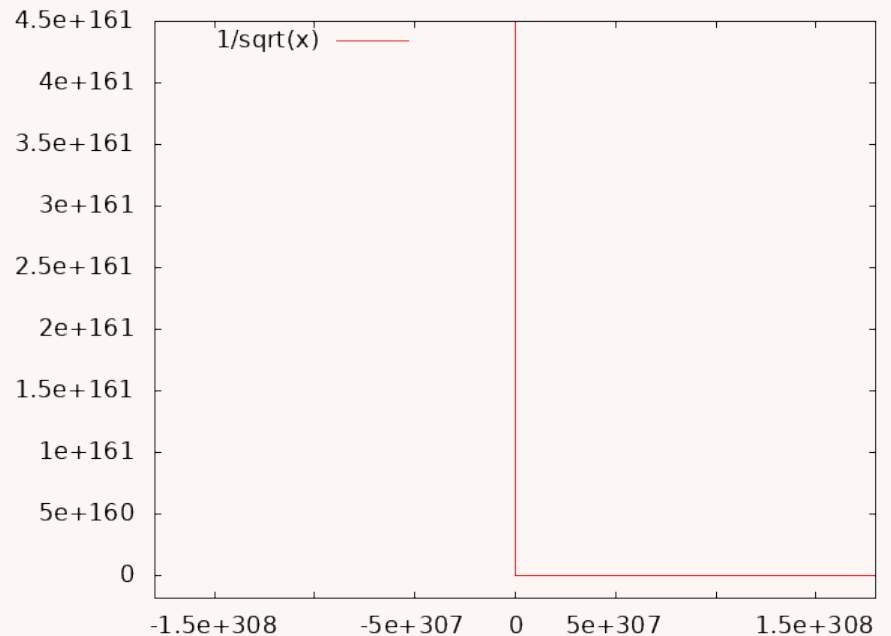
IEEE 754 Double Precision



C double precision square root function



C double precision reciprocal square root function



GNU C library sqrt converted to $\frac{1}{\sqrt{x}}$

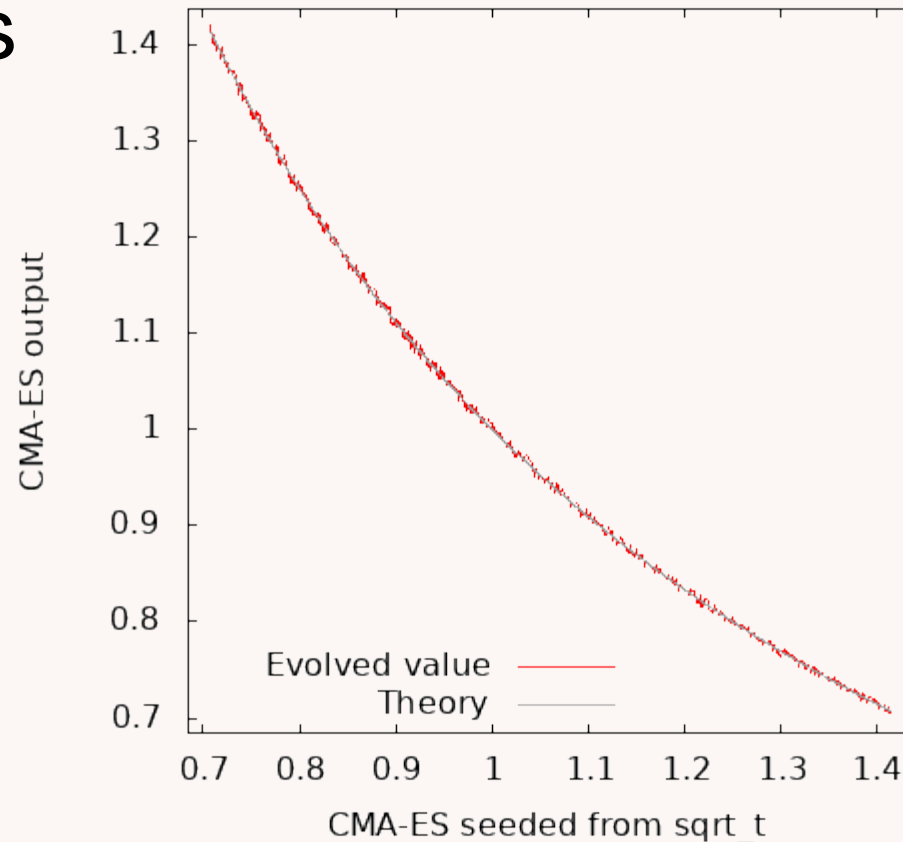
- Chosen implementation of sqrt divides normalised input into 512 bins.
- Each bin holds start point for Newton-Raphson and initial derivative (two floats)
- Run CMA-ES per table element:
 - Seed with square root value, ignore 2nd float
 - Run code with CMA-ES generated test value
 - **Fitness = $\log |1/(c*c) - x|$** where $c = \text{'invsqrt'}(x)$
x takes three test values: smallest, mid, max in bin
 - Random restart if search fails to find value for which 3 diffs are smallest possible

CMA-ES

sqrt seed values
close to invsqrt

Evolved value
very close to
theory.

512 float values found by CMA-ES for GI invsqrt



Evolved $\frac{1}{\sqrt{x}}$

Evolved cbrt tested many thousands of times

- Always within DBL_EPSILON
- Almost always gives best possible double

Compared to Quake (single precision approximation)

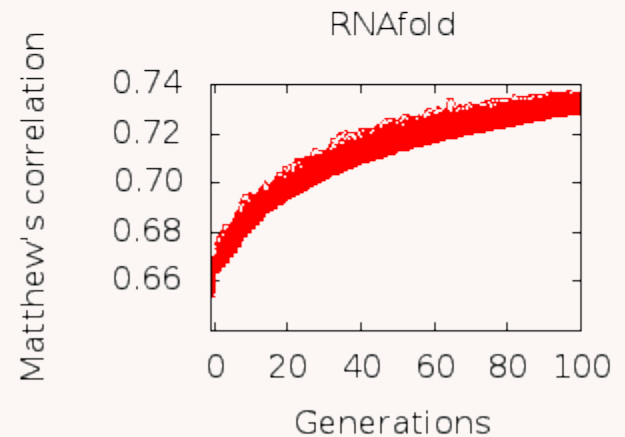
- Quake seldom gives exact answer
- Quake can be 0.17% wrong (0.43/256)
- Quake does not trap negative numbers, sometimes fails, sometimes just wrong
- Quake odd behaviour $<1.5 \cdot 10^{-37}$ or $>3.3 \cdot 10^{38}$

Automatic Software Maintenance

- In a world addicted to software, maintenance is the dominant cost of computing.
- Need to keep parameters up to date. E.g.
 - New science, new laws or regulations, new users, new user expectations
 - Change of load, new hardware (e.g. bigger RAM), automatic porting
 - Search can be fast (total CMA-ES runtime 6 secs)
- Little SBSE research
- Great scope for automation

Summary: FGIP

- Problem of maintaining data in code ignored
- GI can optimize data in programs
- Rapidly generated maths (cbirt, \log_2 , $\frac{1}{\sqrt{x}}$, $1/x$)
 - Frame work open to evolve new functions
- http://www.cs.ucl.ac.uk/staff/W.Langdon/ftp/gp-code/gi_cbirt.tar.gz
- **Software is not fragile**



END

<http://www.cs.ucl.ac.uk/staff/W.Langdon/>

<http://www.epsrc.ac.uk/> 

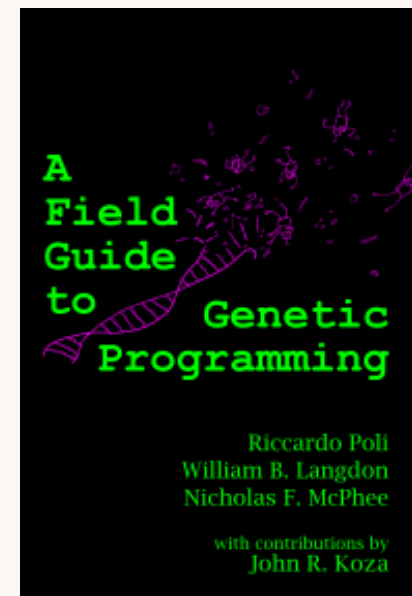
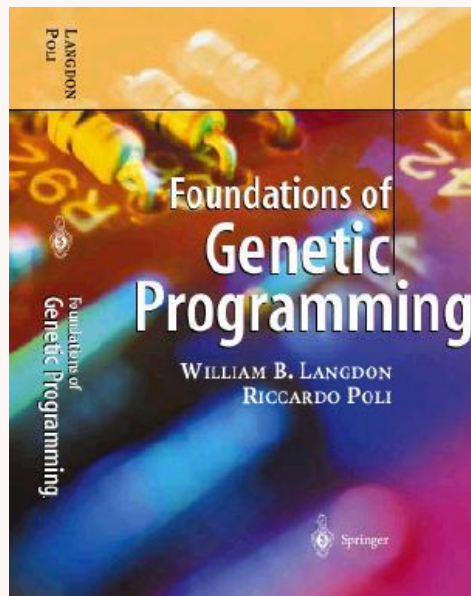
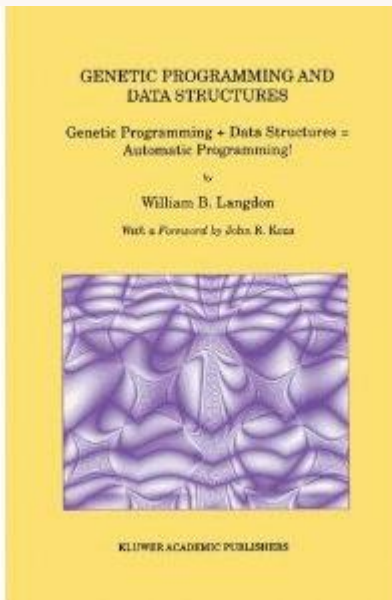
Genetic Programming



W. B. Langdon

CREST

Department of Computer Science



Improving RNAfold parameters

[EuroGP-2018](#)

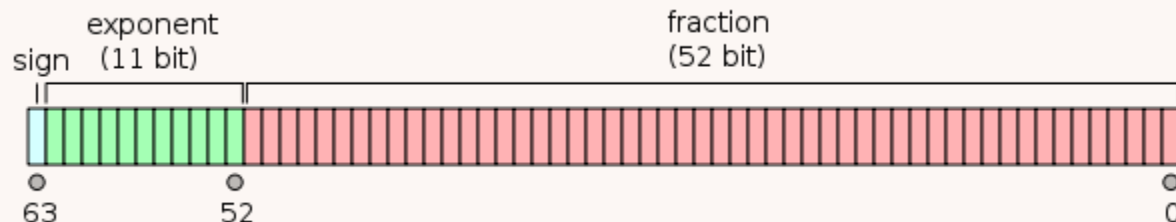
- RNAfold 7100 lines of C source code, 51521 parameters.
- Fitness correlation between prediction and true structure (MCC).
- Post evolution tidy
- 14732 (29%) parameters changed
- Holdout set significant increase in MCC
- Also better than constrained optimisation
- GI parameters [rna_langdon2018.par](#) shipped with ViennaRNA since 13 Jun 2018

Manual Changes I

- Most implementations of square root use hardware support.
- GNU C library glibc 2.29 also includes Newton-Raphson iterative solution
- Trap bad values, e.g. negative
- Normalise double input to 0.5 .. 2.0
- Guaranteed convergence in three steps:
 - Update both estimate of \sqrt{x} and derivative
- Apply square root to exponent, ie divide by 2

Code Changes II

- Normalise double precision input to 1.0..2
 - Update estimate of $x^{-1/2}$
 - Use reciprocal of derivative, i.e. $x^{3/2}$, directly
- Apply invsqrt to exponent, i.e. divide by 2 and make negative.
- Could we use code G1 to further improve?

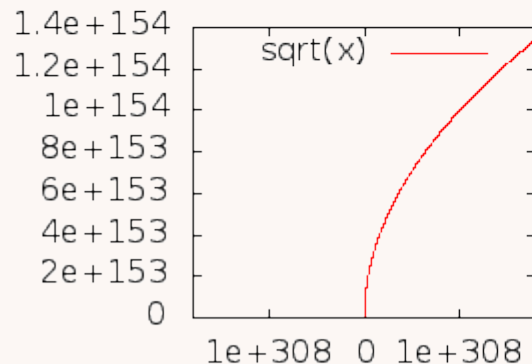


Square root to binary log [GECCO-2019](#)

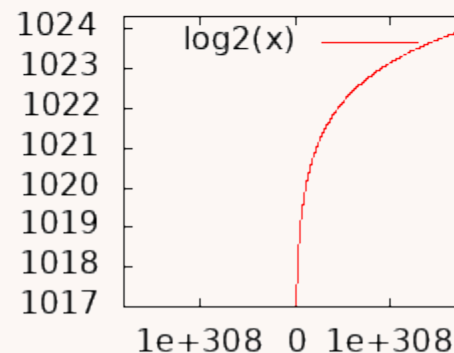
Frame work as sqrt to cbrt but

- Derivative known
- CMA-ES one dimension at a time (512 times)
very easy

C double precision square root function



C double precision binary logarithm function



The Genetic Programming Bibliography

<http://gpbib.cs.ucl.ac.uk/>

13217 references, [12000 authors](#)

Make sure it has all of your papers!

E.g. email W.Langdon@cs.ucl.ac.uk or use | [Add to It](#) | web link



RSS Support available through the [XML](#) [RSS](#) Collection of CS Bibliographies.

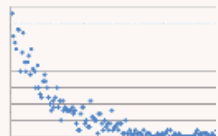
Co-authorship community.
Downloads

Downloads by day



A personalised list of every author's GP publications.

[blog](#)



Your papers

Search the GP Bibliography at

<http://iinwww.ira.uka.de/bibliography/Ai/genetic.programming.html>