



***C340 Concurrency:
Modelling Concurrency in FSP***

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What do we have to model?

- ***Relative or absolute speed?***
 - *Neither!*
- ***Concurrency or parallelism?***
 - *Interleaved model of concurrency!*
- ***Relative order of actions?***
 - *Arbitrary interleaving!*
- ***We use an asynchronous model of execution!***



FSP: Parallel Composition

- *If P and Q are processes then $(P \parallel Q)$ denotes the parallel execution of P and Q*
- *\parallel is used to model parallel composition of processes*
- *Names of concurrent processes are preceded by \parallel*

- *Example:*

`CONVERSE = (think->talk->STOP).`

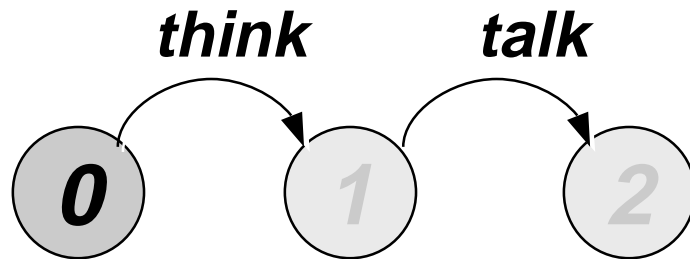
`ITCH = (scratch->STOP).`

`\parallel CONVERSE_ITCH = (ITCH \parallel CONVERSE).`

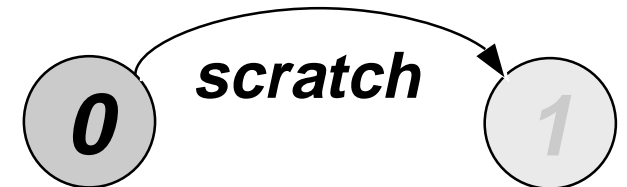


Equivalent LTSs

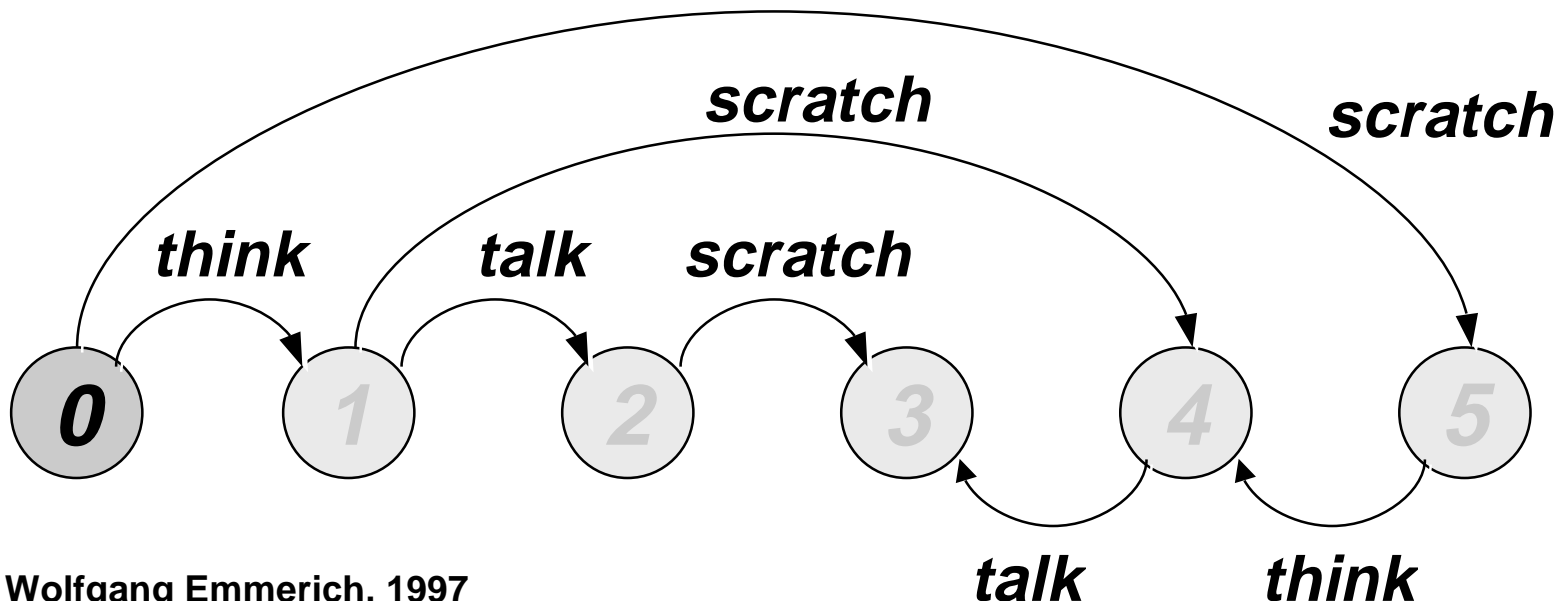
CONVERSE = (think->talk->STOP) .



ITCH = (scratch->STOP) .



|| CONVERSE_ITCH = (ITCH || CONVERSE) .





Properties of Parallel Composition

- *Parallel composition operator has two important algebraic properties*
- *Commutativeness*
 - $(P \mid \mid Q) = (Q \mid \mid P)$
 - *ordering is not important!*
- *Associativeness*
 - $((P \mid \mid Q) \mid \mid R) = (P \mid \mid (Q \mid \mid R)) = (P \mid \mid Q \mid \mid R)$
 - *brackets can be omitted!*



FSP: Process Interactions

- *Concurrent processes that share actions interact with each other*

- *Used to model synchronisation*

- *Example:*

MAKER = (make->ready->MAKER) .

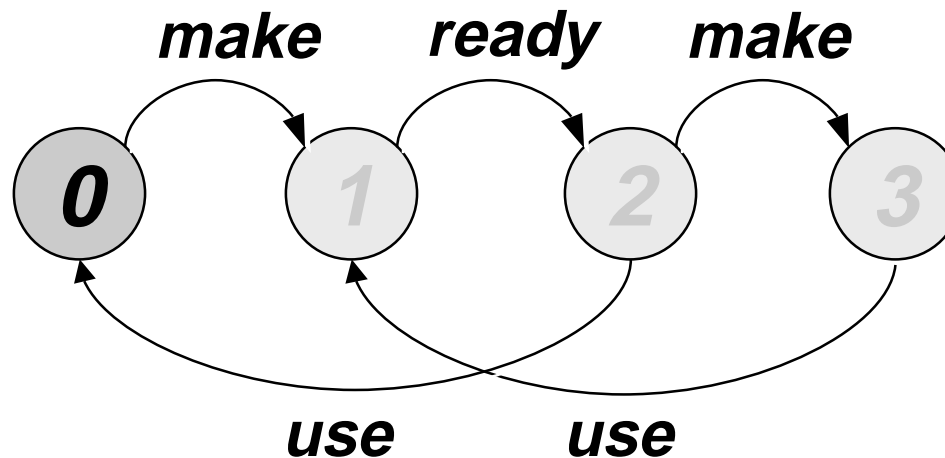
USER = (ready->use->USER) .

|| MAKER_USER = (MAKER || USER) .

- *Product has to be ready before it can be used.*

Equivalent LTS

```
MAKER = (make->ready->MAKER) .  
USER  = (ready->use->USER) .  
|| MAKER_USER = (MAKER || USER) .
```



Handshake

- **An action that is acknowledged by another action is referred to as handshake**
- **Widely used to structure process interactions**

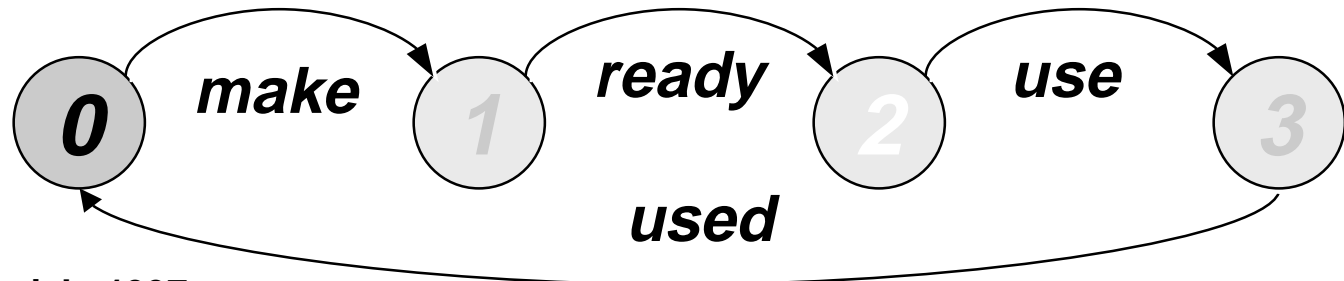
- **Example:**

`MAKERv2 = (make -> ready -> used -> MAKERv2) .`

`USERv2 = (ready -> use -> used -> USERv2) .`

`|| MAKER_USERv2 = (MAKERv2 || USERv2) .`

- **LTS:**





FSP: Process Labelling

- *The process label $a:P$ prefixes each label in the alphabet of P with a*
- *Avoids name clashes in different instantiations of processes and enables reuse.*
- *Example:*
 $SWITCH = (on \rightarrow off \rightarrow SWITCH) .$
 $|| TWOSWITCH = (a:SWITCH || b:SWITCH) .$
- *Alphabet of $|| TWOSWITCH$:*
 $\{a.on, a.off, b.on, b.off\}$



FSP: Process Labelling (cont'd).

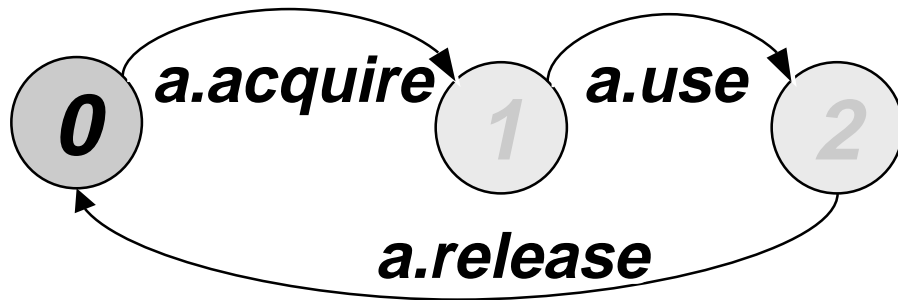
- ***The process label $\{a_1, \dots, a_x\} :: P$ replaces every label n in the alphabet of P with label $a_1.n, \dots, a_x.n$.***

- ***Example:***

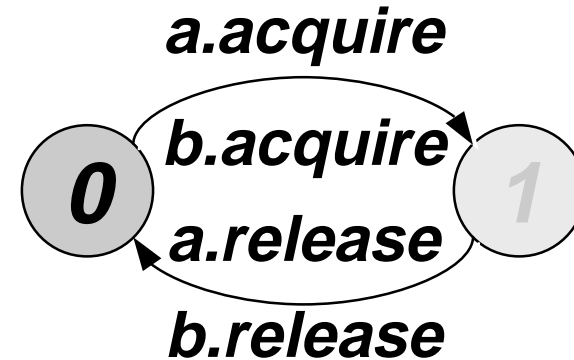
```
RESOURCE=(acquire->release->RESOURCE).  
USER = (acquire->use->release->USER).  
|| RESOURCE_SHARE =  
  (a:USER || b:USER || {a,b}::RESOURCE).
```

Equivalent LTSs

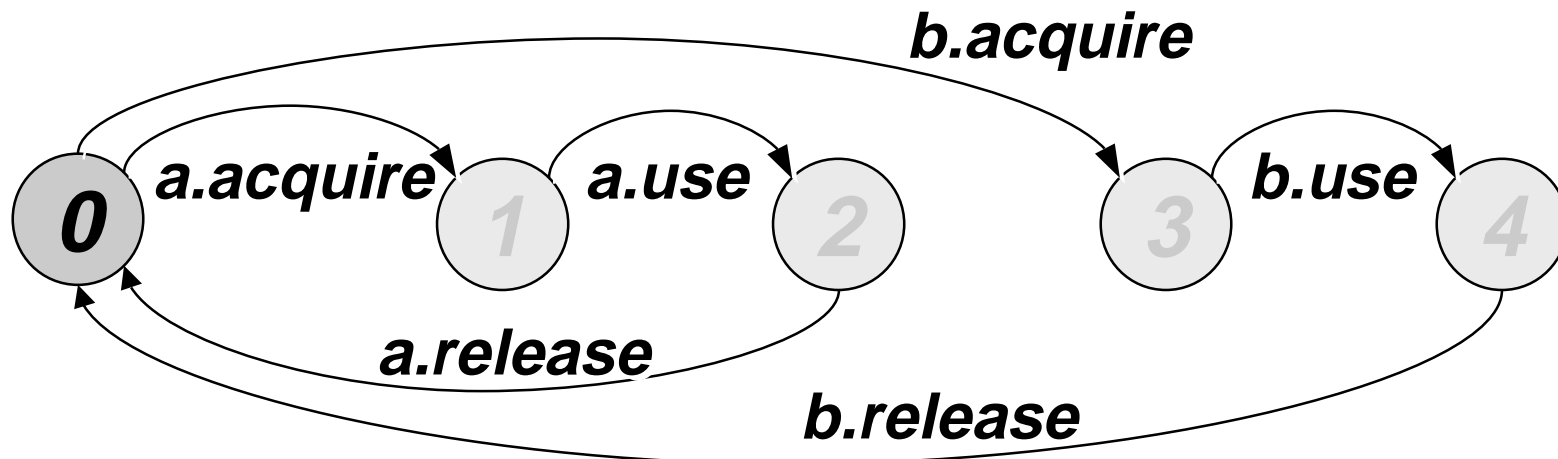
a : USER



{a,b} :: RESOURCE



a : USER || b : USER || {a,b} :: RESOURCE





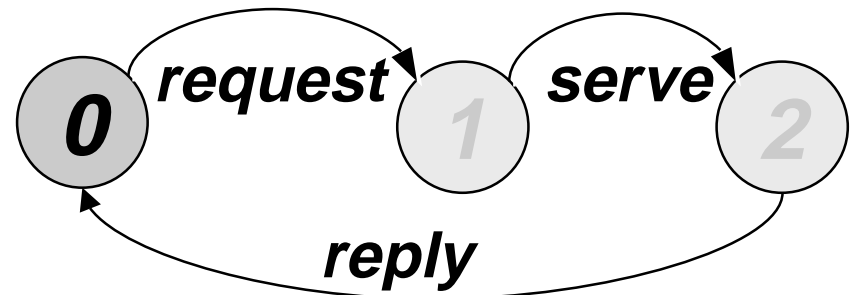
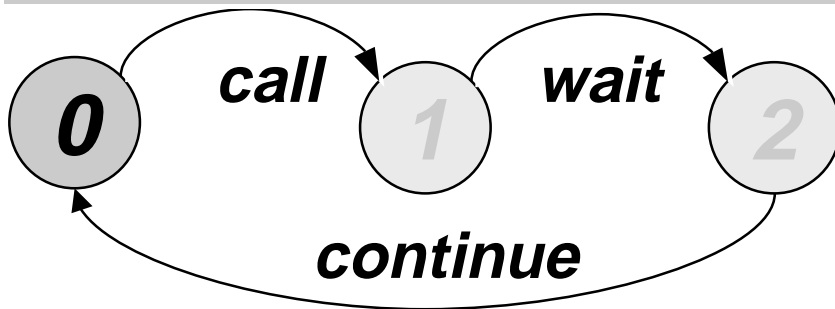
FSP: Relabelling

- ***Relabelling functions change names of action labels. The relabelling function is:***
 $/\{\text{new1/old1}, \dots \text{newn/oldn}\}.$
- ***Used to synchronise actions with different names in composite processes.***
- ***Example:***

```
CLIENT=(call->wait->continue->CLIENT).  
SERVER=(request->serve->reply->SERVER).  
||CLIENT_SERVER = (CLIENT || SERVER)  
  /{call/request, reply/wait}.
```

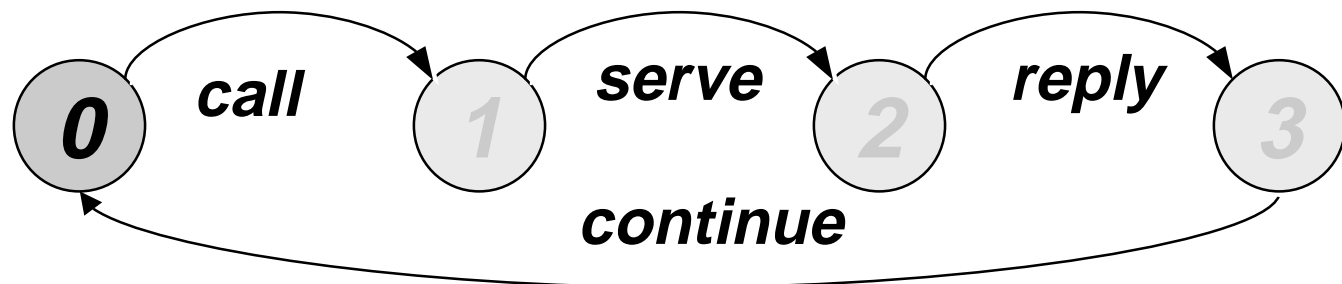
Equivalent LTSs

CLIENT = (call -> wait -> continue -> CLIENT).



SERVER = (request -> serve -> reply -> SERVER).

|| CLIENT_SERVER = (CLIENT || SERVER) / {call/request, reply/wait}.





FSP: Hiding

- *The hiding operator / $\{a_1 \dots a_x\}$ removes action labels $a_1 \dots a_x$ from alphabet of P and hides them*
- *Hidden actions are labelled τ*
- *Hidden actions in different processes are not shared*

- *Example:*

`USER = (acquire->use->release->
USER) \ {use}.`

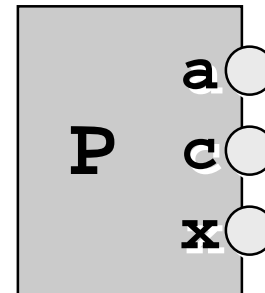


FSP: Interfaces

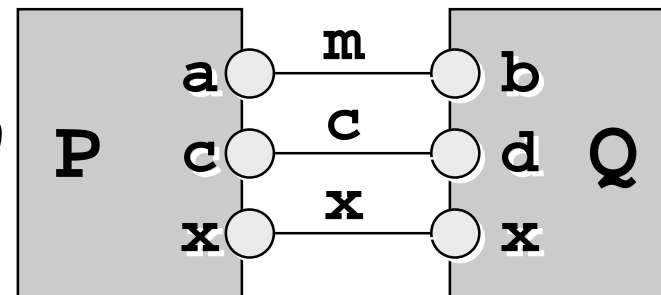
- ***The interface operator $@\{a_1 \dots a_n\}$ hides all actions in the alphabet of \mathbb{P} that do not occur in the set $a_1 \dots a_n$.***
- ***Complementary to hiding***
- ***Like hiding used to reduce complexity of resulting LTS.***
- ***Example:***
***USER = (acquire->use->release->
USER)@{acquire,release}.***

FSP: Structure Diagrams

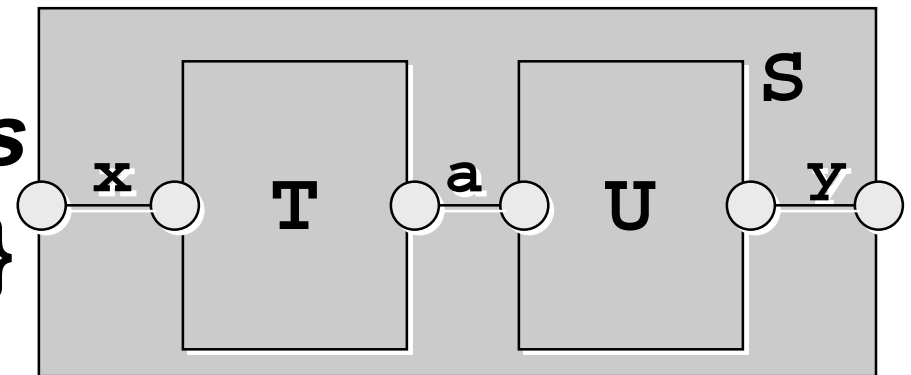
**Process P with
alphabet $\{a, c, x\}$**



**Parallel Composition
 $(P \parallel Q) / \{m/a, m/b, c/d\}$**



**Composite Process
 $S = (T \parallel U) @ \{x, y\}$**





Summary

- ***Parallel Composition***
- ***Process Interactions***
- ***Process Labelling***
- ***Process Relabelling***
- ***Hiding / Interfaces***
- ***Structure Diagrams***
- ***Next session: Tutorial on FSP modelling***
- ***Solve Exercises 3 and 4 of tutorial sheet***