

# Digital Signatures



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#### Roadmap

- Legal aspects
- What are Digital Signatures?
- How Secure they are ?
- Main realizations known
- Applications





1.

# What is a [Digital] Signature?

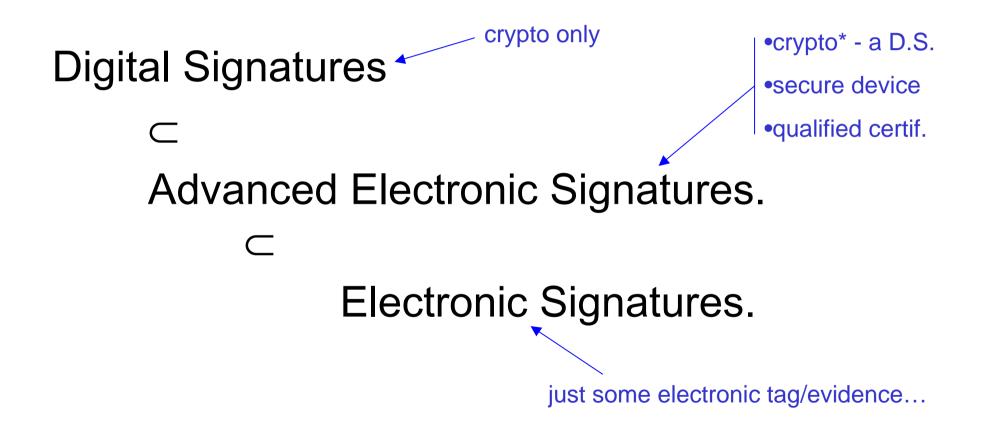
# Legal Aspects





#### Vocabulary

frequently confused







# **Electronic Signatures**

Idea: some electronic data associated to an electronic document that proves (?) sth. (not much)...

Goal: Electronic records and signatures should be admissible in court. Can even be just a PIN code (!). How strong are solutions and in what context secure enough – different problem. Usually admitted, have to challenge them in court.

# Electronic Signature: Def:

<u>Definition [US]:</u> an <u>electronic sound, symbol, or process</u>, <u>attached</u> to or logically associated with a record and executed or adopted by a person with the <u>intent</u> to sign the record. [Uniform Electronic Transactions Act, US].

<u>Definition [EU]:</u> data in <u>electronic</u> form which are <u>attached</u> to, or logically associated with, other electronic data and which serve as a method of authentication.

=> (apparently no "intent")





# Digital Signature.



<u>Idea:</u> cryptographic technique.

<u>Definition:</u> 3 algorithms...

<u>Security Goals/Properties:</u> Message Authenticity, Unforgeability, Non-repudiation, Third-party Verifiability...





#### The European Directive on Electronic Signatures

The European Directive of December 13, 1999

#### Main goals:

- free movement of signatures between the EU countries to accompany free movement of goods and services.
- Recognition as evidence in court.

Effect: Member states are required to implement the Directive => translate into national law.





# Electronic and Advanced Signatures (in The European Directive)

#### 1. Electronic Signature.

<u>Definition [EU]:</u> data in <u>electronic</u> form which are <u>attached</u> to, or logically associated with, other electronic data and which serve as a method of authentication.

=> (apparently no "intent" like in the US)

#### 2. Advanced Electronic Signature.



An electronic signature that:

- is uniquely linked to a signatory and capable of identifying the signatory, and created by means the signatory can maintain under his sole control,
- and linked to the data being signed such that any change of the data is detectable.





#### Electronic == Handwritten?

Equivalence (as strong in terms of law) under two conditions:

- 1. Produced by a <u>secure</u> signing device. [hardware device!]
- 2. Based on a qualified certificate.

"Advanced Signature" a.k.a. "Qualified Signature"

Is it normal, good or bad?

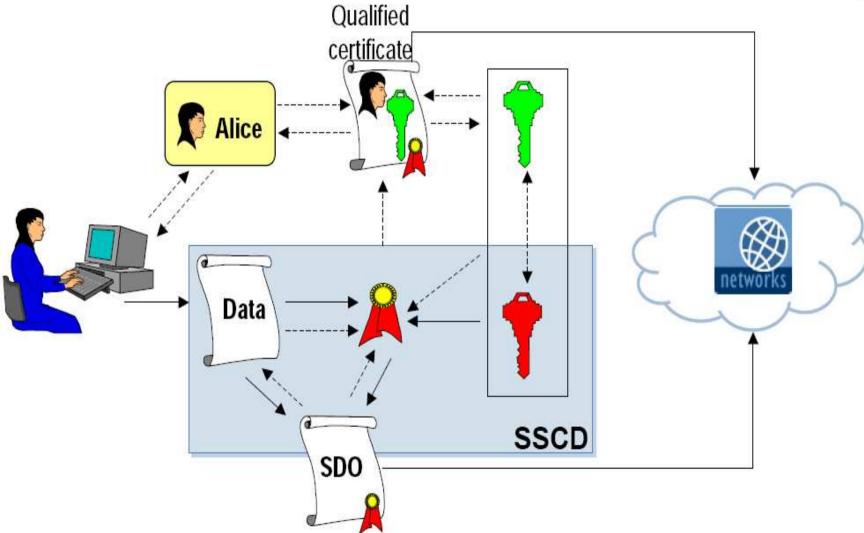
Handwritten signatures can be "perfectly" imitated as well. In some aspects electronic signatures are much more secure...





## SSCD = Secure Signature Creation Device









#### The European Directive on Electronic Signatures

CSPs = Certification Service Providers more than just CA (Certification Authorities).

- They have the right to issue QC (Qualified Certificates) on some territory.
  - QC can contain arbitrary limitations provided standardized/recognized [e.g. <= 1000 €].</li>
- CSPs are LIABLE for damage (for negligence e.g. to revoke) - potentially huge liability!.
  - ⇒ have to implement tough [physical,IT,...] security.
  - ⇒ Explains why one has to pay for signatures... (e.g. 50 £ per year for a string of bits...).

(<u>Technical solution:</u> (not done) rely on several CAs, check all the certificates. Impossible to corrupt everyone...)



# Electronic Signatures in the UK

EU Directive => Translation into national law.

- 1. The Electronic Communications Act 2000.
  - Section 7(1). Electronic signatures are admissible in evidence about the authenticity or integrity of a communication or data.
- 2. The Electronic Signatures Regulations 2002 (SI 2002 No. 318).
  - Regulation 3: QC and CSPs.





## [Manual and Digital] Signatures

#### Two main functions:

- 1. Identify the signer
- 2. Approbation of the document.







## Manual ≠ Digital Signatures

Two main functions

1. Identify the signer

2. Approbation

...in electronic word:

1. Easy to copy!

2. Easy to alter the document!

Consequence => A digital signature does depend on the document.

(need to protect document integrity, did not exist before!)





## **Digital Signatures**

#### Three main functions?

- 1. Identify the signer (solved)
- 2. Approbation (*not easy...*)
- Integrity of the message (solved)







#### Requirements so far:

#### Three main functions:

- 1. Identify the signer (solved)
- 2. Approbation (*not easy*...)
- Integrity of the message (solved)







## Digital Signatures - Bonus

#### **Another main function!**

- 1. Identify the signer (certify origin, solved)
- 2. Approbation (hard to get!)
- 3. Integrity of the message (solved)
- 4. Automatic verification, and better:

```
Public Verifiability
```

(easy => became mandatory)





2.

# **Towards Technical Solutions**





#### How These Problems are Solved?

- Identify the signer doable
   => solved by crypto + trusted key infrastructure /PKI/ + secure hardware)
- 2. Approbation hard => by crypto + law + policy + trusted hardware/software
- 3. Integrity of the message=> solved by crypto only
- 4. Public Verifiability=> solved by crypto only





#### How These Problems are Solved?

1. Identify the signer

## Non-repudiation:

(French: Non-répudiation, Imputabilité).

The signer is the ONLY and UNIQUE person that can create the (signed) document.





# Non-Repudiation (== "Imputability")

# The signer is the ONLY UNIQUE person that can create the document.

- ⇒ Existed already for manual signatures.
- ⇒ CAN ONLY BE DONE with PUBLIC KEY CRYPTOGRAPHY!



- ⇒ Impossible with DES or AES.
- ⇒ Secure hardware is ALSO NECESSARY



- ⇒ Impossible without a smart card (or other kind of trusted and closed hardware).
- ⇒ Source of trust necessary
  - ⇒ One authentic public key: ROM, CD-ROM sth. that cannot be altered.





3.

# Cryptographic Signatures







# \*\*\*Message Authenticity – Goals

#### Different security levels:

- 1. Correct transmission no (random) transmission error. A malicious attacker can always modify it.
  - Achieved with CRC and/or error [correction]/detection codes.
- 2. Integrity no modification possible if the "tag/digest" is authentic. If we cannot guarantee the authenticity of the tag, a malicious attacker can still modify and re-compute the hash.
  - Achieved with cryptographic hash functions (= MDC). (e.g. SHA-1).
- 3. Authenticity specific source. Authentified with some secret information (key).
  - Achieved with a MAC (= a hash function with a key = a secret-key signature).
- 4a. Non-repudiation very strong requirement. Only one person/entity/device can produce this document.
  - Achieved with Digital Signatures. The strongest method of message authentication.
- 4b. Public verify-ability. Everybody can be convinced of the authenticity (trust the bank?).
  - Achieved with Digital Signatures. The strongest method of message authentication.





# Digital Signatures vs. Authentication

- Strongest known form of Message Authentication.
- Allows also authentication of a token/device/person (e.g. EMV DDA, US Passport):
  - challenge –response (just sign the challenge)
- The reverse does not hold:
  - Not always possible to transform authentication into signature. More costly in general!

Sym. encryption << P.K. authentication < signature



Nicolas T. Court



#### \*\*Signatures

Can be:

#### Public key:

•Real full-fledged digital signatures.

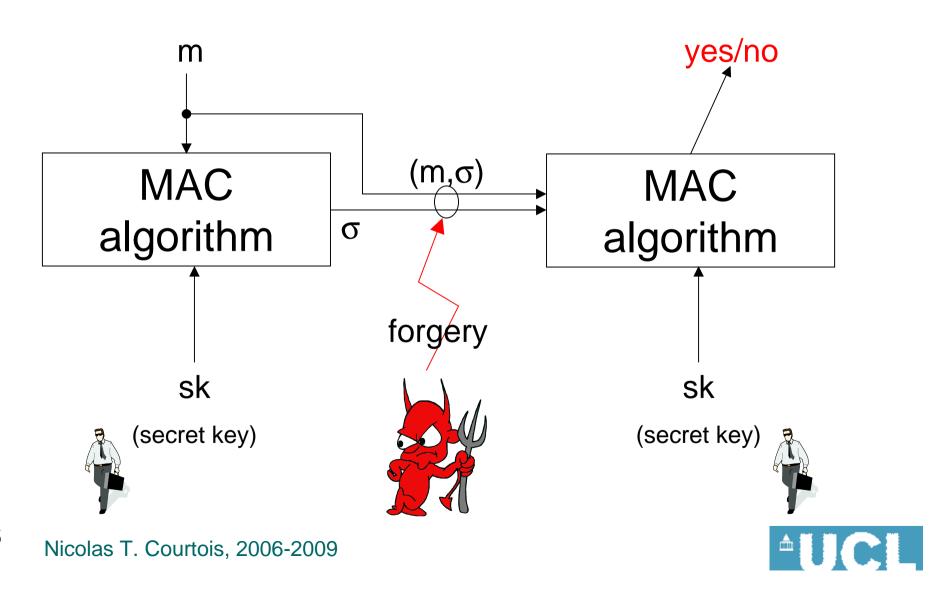
#### Secret key:

- •Not « real signatures » but MACs.
- •Widely used in practice, OK if you trust the verifier...



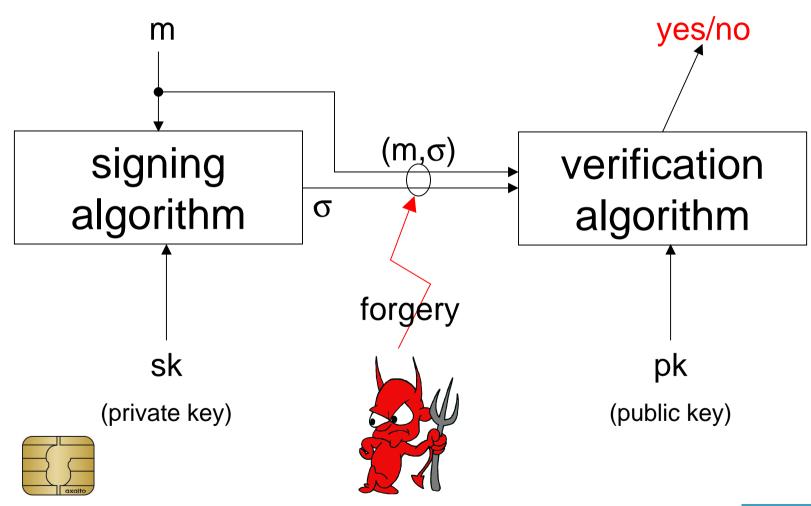


#### MACs = "Secret-Key Signatures"





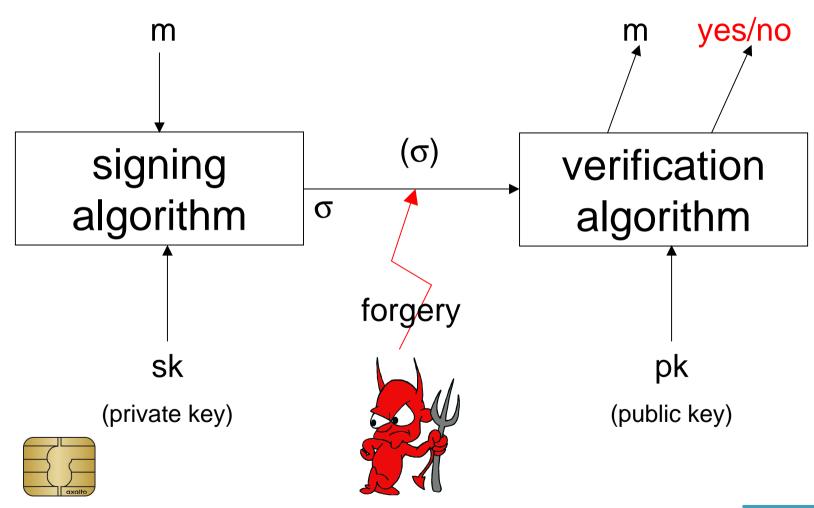
## **Digital Signatures**







#### Digital Signatures with Message Recovery





#### \*\*\*\*Signatures - Requirements

- Authenticity guarantees the document signed by...
- 2. Non-repudiation normally only possible with public-key signatures.
- 3. Public verify-ability normally only possible with public-key signatures.





# 4. How to Do It Right?

Until around 2001, nobody knew exactly!
Some international standards were broken.







# Modern Cryptography:

First: Understand what we want:

Formal security definitions.

2. Then: Try to achieve it:

Prove the Security w.r.t. a hard problem.

There is no other way known.







# Many security notions, but...

#### Take the STRONGEST POSSIBLE version:

Adversarial Goal.
 the weakest possible!



- 2. Resources of the Adversary: The strongest possible: 10 G\$.
- 3. Access / Attack: The strongest possible, total adaptive "oracle" access.







# Secure Public Key Signature

The "good" definition [Golwasser-Micali-Rivest 1988]:

[Strong] **EUF - CMA** (Existential Unforgeability under CMA)

1. Adversarial Goal.

Find any new pair (m,σ) (new m)!

Strong version: even if M is old (signed before).

- 2. Resources of the Adversary:
  Any Probabilistic Turing Machine doing 280 computations.
- Access / Attack:
   May sign any message except one (target),
   (Adaptively Chosen Message Attacks).







# \*Attacks on Signature Schemes

- Adversarial Goal.
- BK Recover the private key,
  - ullet e.g. factor N=pq .
- UF Universal forgery sign any message, may be easier ! e.g. compute:  $x \mapsto x^{1/e} \mod N$
- SF Selective Forgery sign some messages
- EF Existential Forgery just sign any message, even if it means nothing useful.
- Malleability: sign a message that has been already signed by the legitimate user.





# \*Signatures – Unforgeability-CMA2 Game

# One-more signature principle.

[Goldwasser, Micali, Rivest 1988].

$$\mathsf{ADV}_{PK}$$

 $\mathsf{ADV}_{PK}$  ORACLE $_{SK,\,PK}$ 

The Adversary gets a signature of any message.

B) He wants to find a new valid pair message signature:  $(m, \sigma)$ ,  $m \neq m_i$ 

A scheme is 
$$(T, \varepsilon)$$
 -UEF-CMA if...

Version 1: P vs. NP asymptotic security. if 
$$T=n^{\mathcal{O}(1)}$$
 then  $\varepsilon=o(1/n^{\mathcal{O}(1)})$ 

Version 2: Concrete security.

if 
$$T < 2^{80}$$

then 
$$\varepsilon < 2^{-40}$$





# 4.1. First Try





#### Access (3.) - Basic Attacks on Signatures

Again assume that the public key is indeed known...

- Public Key Only === a.k.a. Key Only Attack.
- Known Message Attack. Access to several pairs (m,σ).
- Directed [==Non-Adaptive] Chosen Message Attack. (DCMA).
  - Single Occurrence Chosen Message Attack. (SOCMA).
- Fully Adaptive Chosen Message Attack. (CMA).





#### Textbook RSA Signature

- Signature: σ = m<sup>d</sup>.
- Verification:  $m ?= \sigma^e$ .

#### Never use it.





#### What do We Sign? The Problem:

Public key crypto is very slow.

Sign a long message with RSA, impossible, even on a 4 GHz CPU!

- ⇒Use hash function.
- ⇒Sign a short « digest » of the message.

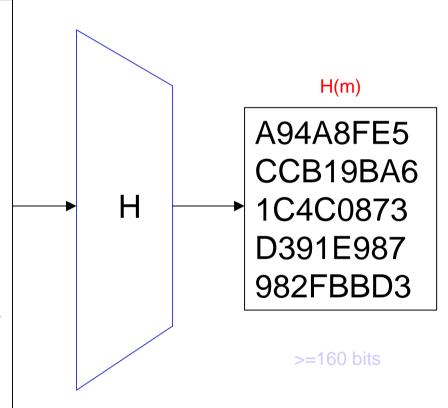




#### [Cryptographic] Hash Function:

m

A hash function (or hash algorithm) is a reproducible method of turning data (usually a message or a file) into a number suitable to be handled by a computer. These functions provide a way of creating a small digital "fingerprint" from any kind of data. The function chops and mixes (i.e., substitutes or transposes) the data to create the fingerprint, often called a hash value. The hash value is commonly represented as a short string of random-looking letters and numbers (Binary data written in hexadecimal notation).



0-∞ bits

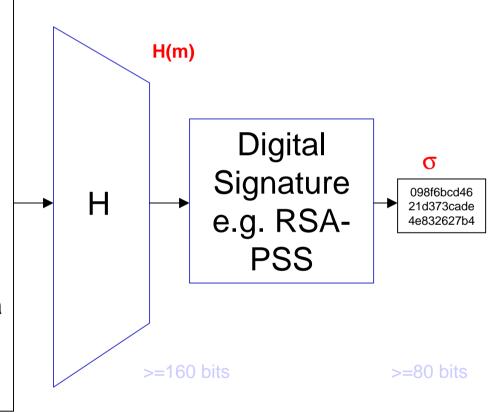




#### Hash-then-Sign

m

A hash function (or hash algorithm) is a reproducible method of turning data (usually a message or a file) into a number suitable to be handled by a computer. These functions provide a way of creating a small digital "fingerprint" from any kind of data. The function chops and mixes (i.e., substitutes or transposes) the data to create the fingerprint, often called a hash value. The hash value is commonly represented as a short string of random-looking letters and numbers (Binary data written in hexadecimal notation).



0-∞ bits





#### Full Domain Hash RSA Signature

- Signature: σ =H(m)<sup>d</sup>.
- Verification: H(m) ?= σ<sup>e</sup>.

Please use it.

Provably secure ("tight" security).

#### Slight problem:

- There is no standardised hash function that produces a hash on 1024 or 2048 bits.
- So RSA-FDH is not very widely used.





5.

#### Best Known Techniques





#### How Secure Are Secure Signatures?

#### All these are necessary ingredients:

- Secure signing environment (know what you sign).
- Secure hash function.
- Secure PK cryptographic system (e.g. RSA) - key size!
- Secure padding! Many were broken
   => provable security.
- All this protected against side-channel attacks.
- A complete certification chain:
   all data have to be certified
   (e.g. the elliptic curve a, b, p,G, etc...).
- Source of trust: have one trusted key (e.g. in ROM).

c r y p t





#### How do you Achieve Security

First: Understand what we want.

Then: Try to achieve it.



How?

Cryptography: We just try.

Cryptology: Prove it mathematically.





#### **Provable Security:**

# Reduce the security to a hard problem.





#### Possible ?:

### Became possible PRECISELY BECAUSE we understood what is a secure digital signature. [GMR88 definition]





#### Textbook RSA Signature

- Signature: σ =m<sup>d</sup>.
- Verification:  $m ?= \sigma^e$ .

#### Never use it.





#### Provable Security – Recommended Solutions

#### Signature (easier):

- RSA-PKCS #1 v1.5. insecure (no proof yet, not broken, variants broken)
  - (exists also in PKCS #1 v2.0 and 2.1 cf. www.rsasecurity.com)
- RSA-FDH: perfectly OK. Except how to find hash function on 2048 bits?
- RSA-PSS: current recommended standard, part of PKCS #1 V.2.x.
  - The best method to sign with RSA >=1024 bits

#### Hash functions broken =>:

- Very serious for signing exe, doc ,pdf, ps, and other complex formats.
- Not serious AT ALL for signing messages in simple text.

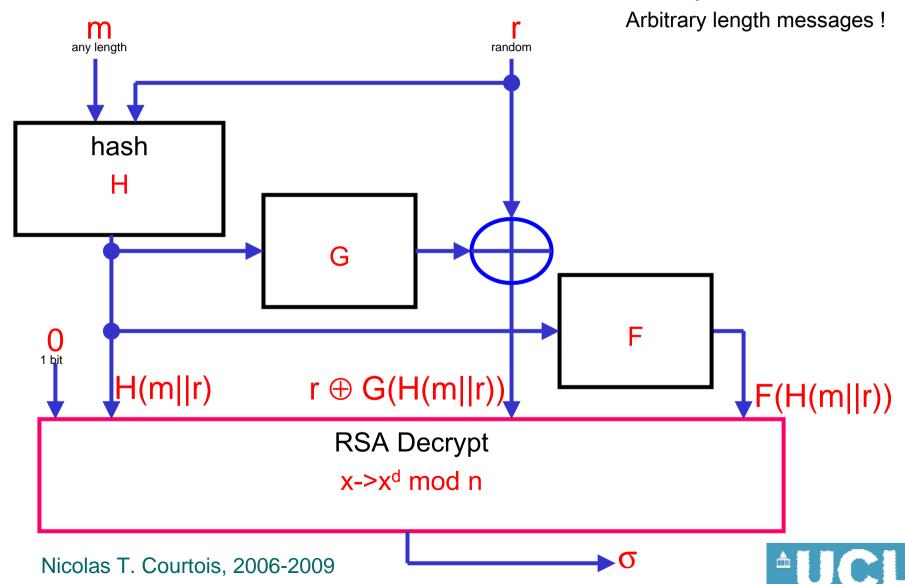
BTW. Recall that CR is not necessary for digital signatures [UOWHF, Boneh result]. Nobody uses this unhappily...





#### Probabilistic Signature Scheme [Bellare-Rogaway'96]

Uses a hash function H and two one-way functions F and G.





#### Provable Security - Example:

#### Any attack on RSA-PSS

=> Extract e-th roots mod N.





#### Secure Signatures – Time Scale

Time to break

Authentication: 1 hour. After it is too late!

Signature: 20 years and more...

#### Must think about future attacks!

E.g. EMV cards: almost certainly broken due to the key sizes, 1024 bits @ year 2010.





#### **Further Security**

## Use timestamping, or forward-secure D.S. or destroy the private key.





#### \*\*But is it hard?

## Any attack on RSA-PSS => Extract e-th roots mod N.

Does not imply factoring! (nobody knows if there is a difference..)





#### Guarantees Solution...

- If one can factor RSA-2048 bits, RSA Security offers 200 000 US\$.
- Breaking Elliptic Curves: 725 000 \$. \*\*\* certicom certicom certific com certific
- =>nobody can claim these are broken...

BTW. Not even 1 dollar for AES...





6.

## Signature Schemes in Practice





#### Some Signature Schemes





✓ RSA-OAEP – only with long keys [>4096 bits]







- ✓ Main DSA standard out of date, 80-bit security.
- ✓ Switch to ECDSA Elliptic Curve, <u>recommended</u>.







#### Some Signature Schemes on a Smart Card

Cryptosystem	SFLASH	NTRU	RSA-1024	RSA-1024	ECC-191
Platform	\$LE-66	Philips 8051	SLE-66	ST-19X	SLE-66
ROM [Kbytes]	3.1	5	NA	NA	NA
Frequency [MHz]	broken in 2007	16	10	13	10
Co-processor	no	no	no	yes	yes
Length of S	259	1757	1024	1024	382
Timing [ms]	59	160	many s	111	180
Timing × Frequency	590	2560	big	1443	1800





#### Which One Should Use?



#### MSA suite B [2005]:

http://www.nsa.gov/ia/industry/crypto\_suite\_b.cfm

• ECDSA + SHA-256. NST



- ⇒The NSA has acquired a licence for 23 Certicom patents. Can sub-licence.
- ⇒RSA is no longer recommended!
- ⇒DSA is dead too.





#### Cheap Alternative:

#### RSA-PSS 2048 bits.

- No patents.
- OK if you have enough computing power and RAM…





#### Signatures

- MACs are widely used, 100s of times faster. Yet symmetric => fundamentally not very secure...Public key solutions are a MUST. Will slowly become ubiquitous.
  - PK crypto everywhere!
- 2. Consequence: Secure Hardware Devices are a MUST (keep private thing private).

All these developments are ahead. Very little of this is in fact used today...





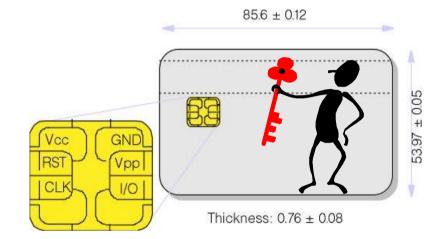
#### **Secure Hardware Devices**

KEEP private keys private all the time!

Must be securely



- Generated
- Stored
- Used
- Backup
- Destroyed

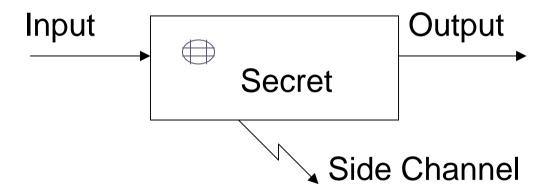


- No real security with a PC.
- Example: Smart Cards.





## Note: the cards must still be protected against channel attacks!



cost: +30 % ?





7.

## Applications of Digital Signatures





#### Main Applications of Digital Signatures

- Bank cards
- Web SSL
- Software authentication (Microsoft, Java Card0 Apple, Google Aps, Nokia)





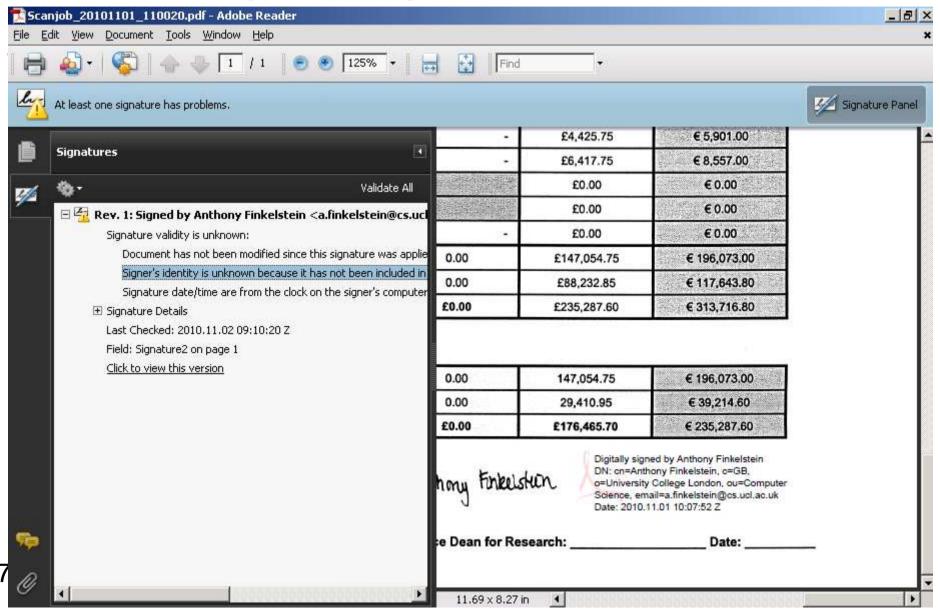
#### More Applications of Digital Signatures...

- e-ID cards, e-Passports
- All public key solutions (even encryption only !) require PKI, requires signatures !
- Secure email, authenticity and anti-spam
- Data and disk authenticity
- Signing notary acts
- Signing medical prescriptions: CPS signs data before sending to Caisse d'Assurance Maladie.
- Vitale 2 will sign when you buy medicines at a pharmacy shop.





#### Digitally Signed pdf @UCL





#### Is It Secure?

