

Binary Space Partition Trees

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Overview

- Previous list priority algorithms fail in a number of cases, non of them is completely general
- BSP tree is a **general** solution, but with its own problems
 - Tree size
 - Tree accuracy

Binary Space Partitioning Trees

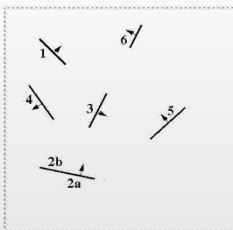
(Fuchs, Kedem and Naylor '80)

- More general, can deal with inseparable objects
- Automatic, uses partition planes defined by the scene polygons
- Method has two steps:
 - building of the tree independently of viewpoint
 - traversing the tree from a given viewpoint to get visibility ordering

Binary Space Partitioning Trees

- BSP tree: organize all of space (hence *partition*) into a binary tree
 - *Preprocess*: overlay a binary tree on objects in the scene
 - *Runtime*: correctly traversing this tree enumerates objects from back to front
 - Idea: divide space recursively into half-spaces by choosing *splitting planes*
 - Splitting planes can be arbitrarily oriented

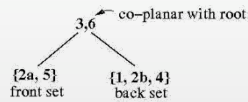
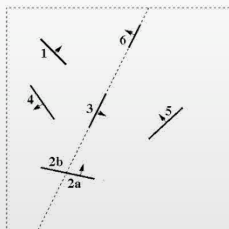
Building a BSP Tree (Recursive)



The tree is empty at first

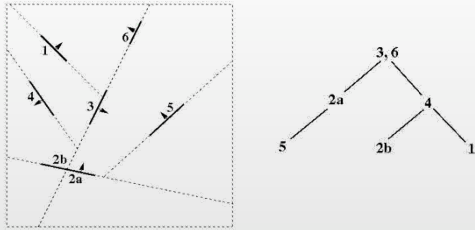
A set of polygons {1, 2, 3, 4, 5, 6}

Building a BSP Tree (Recursive)



Select one polygon and partition the space and the polygons

Building a BSP Tree (Recursive)



Recursively partition each sub-tree until all polygons are used up

Building a BSP Tree (Recursive)

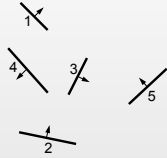
- Start with a set of polygons and an empty tree
- Select one of them and make it the root of the tree
- Use its plane to divide the rest of the polygons in 3 sets:
 - Front, back, coplanar
 - Any polygon crossing the plane is split
- Repeat the process recursively
 - with the front and back sets
 - creating the front and back subtrees respectively

Building a BSP Tree (Incremental)

- Start with a set of polygons and an empty tree
- Insert the polygons into the tree one at a time
 - Insertion is done by comparing it against the plane at each node, and
 - propagating it to the correct side, splitting if necessary
- When the polygon reaches an empty cell, make a node with its supporting plane
- Results depends on insertion order

Building a BSP Tree (Incremental)

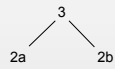
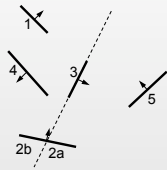
- Randomly start with a polygon, e.g., #3



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Building a BSP Tree (Incremental)

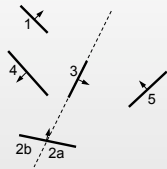
- Randomly, select next polygon, e.g., #2, insert into tree



(left: front, right: back)

Building a BSP Tree (Incremental)

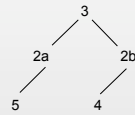
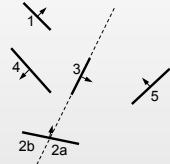
- Next one: #4



(left: front, right: back)

Building a BSP Tree (Incremental)

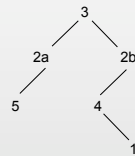
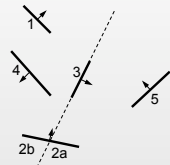
- Next one: #5



(left: front, right: back)

Building a BSP Tree (Incremental)

- Last one: #1



(left: front, right: back)

BSP Tree Traversal

- Why is a BSP tree useful at all?
 - Enumerate all polygons back-to-front for given viewpoint
 - (Use to accelerate ray-tracing)
- Java demo at:
 - <http://www.symbolcraft.com/graphics/bsp/>

BSP Tree Traversal

- How do we traverse the tree back to front for a given viewpoint?
 - Viewpoint given as position
- Recursive traversal:
 - If viewpoint is in front of plane (node)
 - Traverse its back first, then front
 - Otherwise
 - Traverse its front first, then back

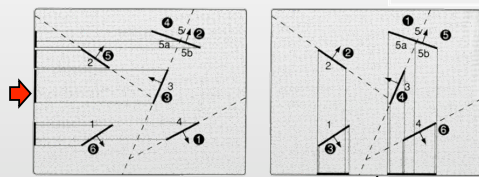
Back-to-Front Traversal

```
void traverse_btf(Tree *t, Point vp)
{
    if (t == NULL) return;
    endif

    if (vp in-front of plane at root of t)
        traverse_btf(t->back, vp);
        draw polygon of node t;
        traverse_btf(t->front, vp);
    else
        traverse_btf(t->front, vp);
        draw polygon of node t;
        traverse_btf(t->back, vp);
    endif
}
```

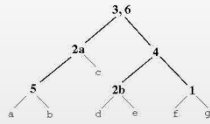
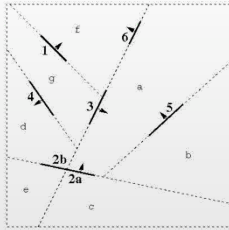
Back-To-Front Traversal for Given Direction

- Camera point as dynamic classification point
- Traversal order:
 - parts behind the plane (w.r.t. direction)
 - polygon of the plane
 - parts in front of the plane (w.r.t. direction)



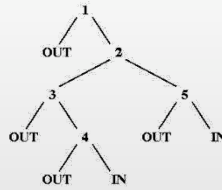
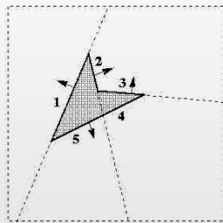
White numbers indicate drawing order.

BSP as a Hierarchy of Spaces

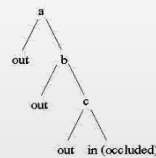
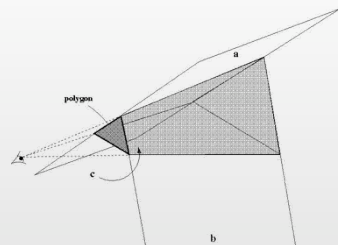


- Each node corresponds to a region of space
 - the root is the whole of R^n
 - the leaves are homogeneous regions

Representation of Polygons



Representation of Polyhedra



BSP Trees for Dynamic Scenes

- When an object moves the planes that represent it must be removed and re-inserted
- Some systems only insert static geometry into the BSP tree
- Otherwise must deal with merging and fixing the BSP cells (see the book!)

Recap

- A BSP is a sequence of binary partitions of space
- Can be built recursively or incrementally
- Choice of plane used to split is critical
- BSP trees are hard to maintain for dynamic scenes
