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Rendering

An introduction to global illumination

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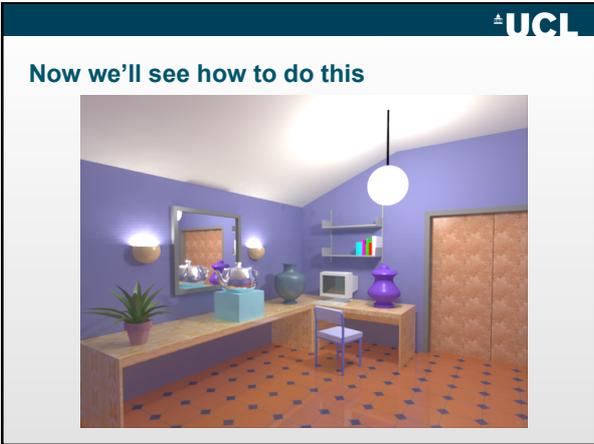
Rendering Recap

- Ray-tracing
 - For each pixel, for each object
- Graphics pipeline, scan conversion
 - For each object, for each pixel
- Local lighting models
 - Diffuse, Phong
- Shadows
 - Ray casting
- Reflection, refraction

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You've learned how to do this





Focus

- Graphics hardware
 - Can render scenes with hundreds of thousands of polygons in real-time (>20 fps)
 - Typically surfaces have only simple direct illumination
- Ray tracing
 - Has indirect illumination but for specular surfaces only
- Reality:
 - Most of the light is from diffuse illumination
 - Simulating proper diffuse illumination adds enormously to realism.

Types of Light Transport

- Specular-specular
 - Ray tracing
- Specular-diffuse

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Types of Light Transport

- Diffuse-specular
- Diffuse-diffuse
 - Radiosity

The diagram shows two scenarios of light transport. In the 'Diffuse-specular' case, several blue arrows representing light rays originate from a point on the left and strike a vertical red line representing a specular surface. The reflected rays are shown as red arrows that are perfectly mirrored across the surface normal. In the 'Diffuse-diffuse' case, blue arrows strike a red surface that is represented as a collection of many small facets. The reflected rays are shown as red arrows that are scattered in various directions, representing a diffuse reflection.

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In the next weeks

- Physically based rendering
- Simulation of light transport
 - The radiance equation
 - Radiosity

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Let's Start: Physically Based Rendering

- Simulation of light transport
- Light
 - The nature of light, how it travels in the environment
- Material
 - Anything that interacts with light, how it reflects, refracts or scatters light
 - Bidirectional Reflectance Distribution Function



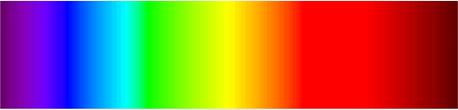
We will use the Radiance Equation

- Radiance Equation
 - Integral equation
 - Describes the energy (light) in the scene
- A solution of this equation → a solution to the whole rendering problem
- Each approach to computer graphics
 - Is different type of numerical solution or approximation to this equation
- Numerical and Monte Carlo sampling methods are used.



Light

- Visible light is electromagnetic radiation with wavelengths approximately in the range from 400nm to 700nm



400nm 700nm



Light: Photons

- Light can be viewed as
 - wave or
 - particle phenomenon
- Particles are photons
 - packets of energy which travel in a straight line in vacuum with velocity c (~300,000 mps)
- The problem of how light interacts with surfaces in a volume of space is an example of a transport problem.

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Light Sources

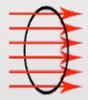
- Types of light sources
 - Point lights
 - Spot-lights
 - Cone of light
 - Radiation characteristic of $\cos^2\theta$
 - Point light sources with non-uniform directional power distribution
 - Area light sources
- Other parameter
 - Attenuation with distance (r) for point light sources
 - $1/(ar^2+br+c)$
 - Physically correct would be $1/r^2$
 - Correction of missing ambient light

Diffuse emitter	
Point light	
Directional light	
Goniometric diagram	
Spot light	

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Light: Radiant Power

- Φ denotes the radiant energy or **flux** in a volume
- The flux is the **rate of energy flowing** through a surface per unit time ([Watts] = [J/s]).
- The energy is **proportional to the particle flow**, since each photon carries energy.
- The flux may be thought of as the **flow of photons per unit time.**



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Light: Flux Equilibrium

- Total flux in a volume in dynamic equilibrium
 - Particles are flowing
 - Distribution is constant
- Conservation of energy
 - Total **energy input** into the volume = total energy that is **output** by or absorbed by matter within the volume.



Light: Fundamental Equation

- Input
 - Emission – emitted from within volume
 - Inscattering – flows from outside
- Output
 - Streaming – without interaction with matter in the volume
 - Outscattering – reflected out from matter
 - Absorption – by matter within the volume
- Input = Output



Light: Equation

- $\Phi(p, \omega)$ denotes flux at $p \in V$, in direction ω
- It is possible to write down an integral equation for $\Phi(p, \omega)$ based on:
 - Emission+Inscattering = Streaming+Outscattering +Absorption
- Complete knowledge of $\Phi(p, \omega)$ provides a complete solution to the illumination problem.
- Rendering is about solving for $\Phi(p, \omega)$.



Simplifying Assumptions

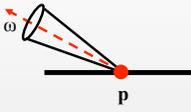
- Wavelength independence
 - No interaction between wavelengths (no fluorescence)
- Time invariance
 - Solution remains valid over time unless scene changes (no phosphorescence)
- Light transports in a vacuum (non-participating medium)
 - ‘free space’ – interaction only occurs at the surfaces of objects

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Rendering Equation – Overview

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The Rendering Equation

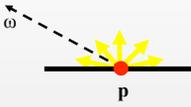


$L(p, \omega) = L_e(p, \omega) + \int f(p, \omega_i, \omega) L(p^*, -\omega_i) \cos\theta_i d\omega_i$

$L(p, \omega)$ is the radiance from a point on a surface in a given direction ω

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The Rendering Equation

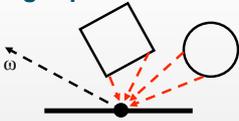


$L(p, \omega) = L_e(p, \omega) + \int f(p, \omega_i, \omega) L(p^*, -\omega_i) \cos\theta_i d\omega_i$

$L_e(p, \omega)$ is the emitted radiance from a point: L_e is non-zero only if p is emissive (= a light source)

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The Rendering Equation

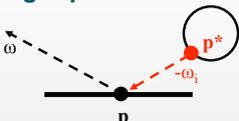


$$L(p, \omega) = L_e(p, \omega) + \int f(p, \omega_i, \omega) L(p^*, -\omega_i) \cos\theta_i d\omega_i$$

Sum the contribution from all of the other surfaces in the scene

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The Rendering Equation

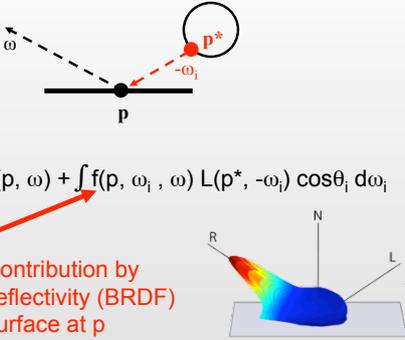


$$L(p, \omega) = L_e(p, \omega) + \int f(p, \omega_i, \omega) L(p^*, -\omega_i) \cos\theta_i d\omega_i$$

For each ω_i , compute $L(p^*, -\omega_i)$: the radiance at point p^* in the direction $-\omega_i$ (i.e., radiance arriving at p)

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The Rendering Equation



$$L(p, \omega) = L_e(p, \omega) + \int f(p, \omega_i, \omega) L(p^*, -\omega_i) \cos\theta_i d\omega_i$$

Scale the contribution by $f(x, \omega_i, \omega)$, the reflectivity (BRDF) of the surface at p

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Questions?



Museum simulation. Program of Computer Graphics, Cornell University.
50,000 patches. Note indirect lighting from ceiling.

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Details

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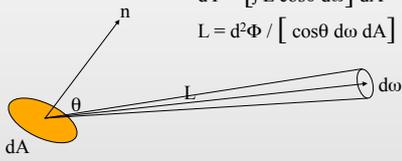
Radiometric terms

- Radiant energy Q , measured in joules (J)
 - This is the basic unit of energy, each particle can be thought of carrying some number of joules of energy
- Radiant power or flux Φ , measured in watts (W)
 - The flux is the rate of energy flowing through a surface per unit time
 - $\Phi = dQ/dt$

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Radiance

- Radiance (L) is the **flux** that leaves a surface, **per unit projected area** of the surface, **per unit solid angle** of direction. Its unit is: [W/(m² sr)].



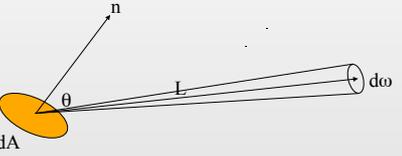
$$d\Phi = [rL \cos\theta \, d\omega] \, dA$$

$$L = d^2\Phi / [\cos\theta \, d\omega \, dA]$$

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Radiance

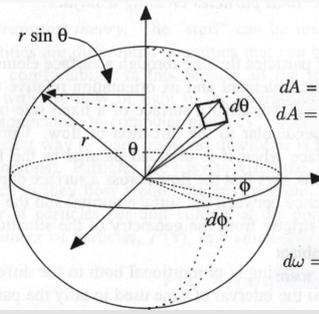
- For computer graphics the basic particle is not the photon and the energy it carries but the ray and its associated radiance.



Radiance is constant along a ray.

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Solid Angle



$$dA = r^2 \sin \theta \, d\theta \, d\phi$$

$$dA = (r \, d\theta) (r \sin \theta \, d\phi) = r^2 \sin \theta \, d\theta \, d\phi$$

$$d\omega = \frac{dA}{r^2} = \sin \theta \, d\theta \, d\phi$$

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Solid Angle

$$d\omega_b = \frac{dB \cos \theta_B}{r^2}$$

The diagram illustrates two differential area elements, dA and dB , represented as small orange ellipses. A line of length r connects the centers of the two areas. Normal vectors n_A and n_B are shown at each area. The angle between n_A and the line r is θ_A , and the angle between n_B and the line r is θ_B .

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Radiosity and Irradiance

- **Radiosity** is the **flux per unit area that radiates** from a surface, denoted by B , measured in $[W/m^2]$
 - $d\Phi = B dA$
- **Irradiance** is the **flux per unit area that arrives** at a surface, denoted by E , measured in $[W/m^2]$
 - $d\Phi = E dA$

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Radiosity and Irradiance

- $L(p, \omega)$ is radiance at p in direction ω
- $E(p)$ is irradiance at p
- $E(p) = (d\Phi/dA) = \int L(p, \omega) \cos\theta d\omega$

~~(or: $L = dE/dA$)~~

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Reflectance

- BRDF
 - Bi-directional
 - Reflectance
 - Distribution
 - Function
- Relates
 - Reflected radiance to incoming irradiance

$$f_r(p, \omega_i, \omega_r) = \frac{dL}{dE}$$

$f_r(p, \omega_i, \omega_r)$ Unit: 1/sr

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BRDF

- Boils down to: How much light is reflected for a given light/view direction at a point?
- Defines the "look" of the surface
- Important part for realistic surfaces:
 - Variation (in texture, gloss, ...)

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Describing the reflectance

- As for the light, we simplify the physical reality
- We consider in computer graphics the following properties
 - Diffuse, Specular
 - Isotropic, Anisotropic
- But
 - This is a sample of the real complexity
 - No fluorescence, phosphorescence, diffraction, etc...
 - Often approximated for an area or a full object, although in reality different in every point!

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BRDF

- In practice BRDF's hard to specify
- Rely on ideal types
 - Perfectly diffuse reflection
 - Perfectly specular reflection
 - Glossy reflection
- BRDFs taken as additive mixture of these

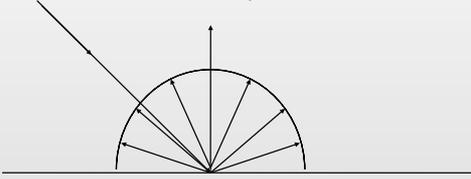
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Perfectly diffuse

- Radiance reflected equally in every direction independently of the incoming direction

$$f_r(\omega_i, \omega_r) = \rho / \pi$$

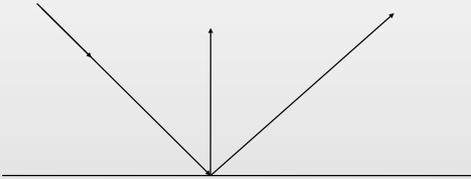
ρ is the reflectance



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Perfectly specular

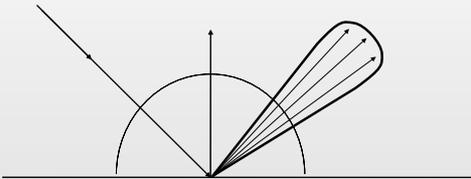
- Reflected dependently of the incident light



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BRDF

- Glossy

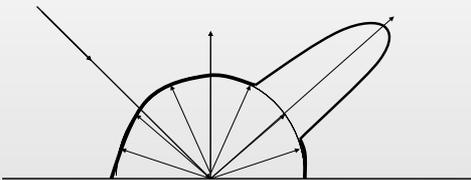


The diagram shows a horizontal surface with a vertical normal vector. An incident ray from the upper left hits the surface. The reflected rays are shown as a narrow, elongated lobe centered around the specular reflection direction, characteristic of a glossy material.

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BRDF

- Diffuse + Glossy



The diagram shows a horizontal surface with a vertical normal vector. An incident ray from the upper left hits the surface. The reflected rays form a broad, semi-circular lobe (diffuse) and a narrow, elongated lobe (glossy) centered around the specular reflection direction.

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How to define a BRDF

- Define
 - By hand (difficult)
 - Data basis (measured)
 - Estimate from photographs (inverse illumination)
- How to visually compensate for rough approximation?
 - Define the same BRDF for a whole surface
 - Apply a texture



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Properties of BRDFs

- Non-negativity
 $f_r(\omega_i, \omega_r) \geq 0$
- Energy Conservation
 $\int_{\Omega} f_r(\omega_i, \omega_r) d\omega_r \leq 1$ for all ω_i
- Reciprocity
 $f_r(\omega_i, \omega_r) = f_r(\omega_r, \omega_i)$

– Aside: actually does often **not** hold for real materials
 [see Eric Veach's PhD Thesis!]

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How to compute amount of reflected light?

- Integrate all incident **light** * **BRDF**

The diagram illustrates a light source emitting rays that strike two objects, Object 1 and Object 2. The reflected rays then hit a surface labeled 'Object', which is represented by a wavy line with green dots. A blue shaded area indicates the incident light cone.

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The Radiance Equation

- Radiance $L(p, \omega)$ at a point p in direction ω is the sum of
 - Emitted radiance $L_e(p, \omega)$
 - Total reflected radiance

Radiance =
Emitted Radiance + Total Reflected Radiance

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The Radiance Equation: Reflection

- Total **reflected radiance** in direction ω :

$$\int f(p, \omega_i, \omega) L(p^*, -\omega_i) \cos\theta_i d\omega_i$$
- Full Radiance Equation: (p^* is closest point in direction ω_i)

$$L(p, \omega) = L_e(p, \omega) + \int f(p, \omega_i, \omega) L(p^*, -\omega_i) \cos\theta_i d\omega_i$$
 - (Integration over the illumination hemisphere)

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The Radiance Equation

- Light incident at p from direction ω_i , is in fact light that is reflected from p^* in direction $-\omega_i$:
 - $L_{\text{incident}}(p, \omega_i) = L(p^*, -\omega_i)$

$L(p, \omega)$ depends on all $L(p^*, -\omega_i)$ which in turn are recursively defined.

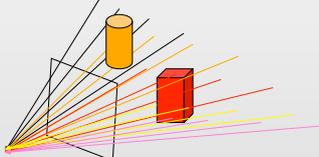


The radiance equation models global illumination.

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Traditional Solutions to the Radiance Equation

- The radiance equation embodies totality of all views (2D projections).
- Extraction a 2D projection to form an image is called rendering.



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Traditional Solutions

	Local Illumination	Global Illumination
View Dependent	'Real time' graphics: OpenGL	Ray tracing Path tracing
View Independent	Flat shaded graphics (IBR)	Radiosity (Photon Tracing)

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OpenGL

- In OpenGL, we can define the reflectance with different material properties
 - `glMaterialf(GL_FRONT, GL_DIFFUSE, r,g,b);`
 - `glMaterialf(GL_FRONT, GL_DIFFUSE, 0.3, 0.3, 0.4);`
 - `glMaterialf(GL_FRONT, GL_SPECULAR, 0.3, 0.4, 0.4);`
- You can add a transparency coefficient α
 - `glMaterialf(GL_FRONT, GL_DIFFUSE, R,G,B,A);`
 - `glMaterialf(GL_FRONT, GL_DIFFUSE, 0.3, 0.3, 0.4, 1);`
 - $\alpha \in [0..1]$, 1 for completely opaque, 0 for completely transparent
- But OpenGL does not provide a global illumination solution!

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Other Solutions

- Will be the topic over the next few lectures
