

COMP1008

Testing

Perfection

- Do your programs work perfectly?
- Are you perfect?



No!!



Perfection, or Lack of It

- No program is perfect.
- Programs will have errors.
- Often see quotes like:
 - “On average program code has 10 errors per 1000 lines...”

Two V's

- Verification
 - “Are we building the system right?”
 - Testing code.
- Validation
 - “Are we building the right system?”
 - Testing behaviour against requirements.

Testing

- Testing is really about trying to find bugs.
 - By actually running the code.
- Testing *cannot* show your program will always work properly — only the deluded believe this can be done!
- But it can remove sufficient bugs to make your program “good enough”.
- Testing allows you to gain confidence in your code.

Testing and Proof

- To prove something we must show:

$$\forall x \cdot P(x)$$

- This implies we have to explore every possible state a program can be in.
- But...

Testing and Proof (2)

- Take, for example, the sqrt method.
- To “prove” it works we would have to call it with every possible floating point value.
- So if $2^{64} = 18446744073709551616 \approx 10^{19}$ and we do 10^6 operations per second then this is 10^{13} seconds, which is 10^6 years.



Testing and Proof (3)

- The philosophy behind all testing should be the finding of errors.
 - Need to identify tests most likely to uncover errors.
- No “proof” can be constructed that no errors exist.
 - Just have the situation that no tests find any errors.
 - The next test you add may find an error...

Making testing sqrt manageable

- We still have the problem of 10^{19} possible values that could give us an error.
- So, we need to focus on floating point values that:
 - Are representative of typical input values.
 - Might cause an error.
- But how do you find them?

Testing the sqrt Method

- We can start by studying the domain of the method.
 - sqrt partitions the floating point numbers into 3 sets:

$$x < 0$$

$$x = 0$$

$$x > 0$$
- And by looking at the method to see what the code does and where potential errors might be.

Equivalence Classes

$$\begin{array}{c}
 \forall x \cdot x < 0 \wedge \text{sqrt}(x) \in \text{C} \quad 0 \quad \forall x \cdot x > 0 \wedge \text{sqrt}(x) \in \text{R} \\
 \hline
 \forall x \cdot x = 0 \wedge \text{sqrt}(x) = 0
 \end{array}$$

- Select values that are representative of the distinct classes of input values.
 - $x \geq 0$ looks OK to test.
 - $x < 0$ is a problem as we need to represent complex numbers...
 - Ignore it.
 - Return an error value.

Boundary Conditions

- Want to also focus on boundary conditions:
 - 0.0, 1.0, 2.0, 3.0
 - MIN_DOUBLE, MAX_DOUBLE
 - .3, .33, .333, etc.
 - 0.000000000000001, 0.111111111111111, etc.
 - -0.0, -1.0
 - numbers that might cause under/overflow in sqrt algorithm.
- Can use the code itself to help identify boundaries.
 - If and loop statements.
 - Maths expressions.
- But what level of accuracy (decimal places)?

Running Tests

- Select representatives from each of the sets to construct the test data set.
- Create a test harness — a program to call `sqrt` with the elements of the data set.
 - Or use a test framework.
- Run the program and compare the results with what was expected (which you need to work out some other way!).

Most Basic Approach (not recommended in general)

```
public void testSqrt()
{
    System.out.println("sqrt(1.0) = " + Math.sqrt(1.0));
    System.out.println("sqrt(2.0) = " + Math.sqrt(2.0));
    System.out.println("sqrt(3.0) = " + Math.sqrt(3.0));
    System.out.println("sqrt(10.0) = " + Math.sqrt(10.0));
    System.out.println("sqrt(100.0) = " + Math.sqrt(100.0));
    System.out.println("sqrt(1000.0) = " + Math.sqrt(1000.0));
    System.out.println("sqrt(0.0) = " + Math.sqrt(0.0));
    System.out.println("sqrt(-1.0) = " + Math.sqrt(-1.0));
    // etc...
}
```

Most Basic Approach (2)

```
sqrt(1.0) = 1.0
sqrt(2.0) = 1.4142135623730951
sqrt(3.0) = 1.7320508075688772
sqrt(10.0) = 3.1622776601683795
sqrt(100.0) = 10.0
sqrt(1000.0) = 31.622776601683793
sqrt(0.0) = 0.0
sqrt(-1.0) = NaN ?!
```

NaN?

- Not a Number.
- Value used when result of floating point operation cannot be represented.
- This version of `sqrt` will return NaN for any argument < 0 .
- For this equivalence class, have “solved” problem by updating specification of method.
 - Implies method must check for input less than zero.

Using a different `sqrt` method implementation

```
sqrt(1.0) = 1.0
sqrt(2.0) = 1.4142135623746899
sqrt(3.0) = 1.7320508100147274
sqrt(10.0) = 3.162277665175675
sqrt(100.0) = 10.000000000139897
sqrt(1000.0) = 31.622776601684336
sqrt(0.0) = NaN !!!
sqrt(-1.0) = NaN
```

Different results!
Which are correct?

But

- This is quickly going to get boring and error prone.
 - Manual checking process.
 - OK for 10 tests,
 - Tedious for 100 tests,
 - Mind-numbing for 1000 tests.
 - Mistakes will be made.
- Need an automated approach.

Automate

- Write a test harness program that reads data from data structure or file.
- Get program to run tests and check the results.

```
public void test(double input, double expected, double delta)
{
    double sqrtValue = Math.sqrt(input);
    double diff = Math.abs(sqrtValue - expected);

    if (diff > delta)
    {
        System.out.print("Invalid result for sqrt("+input+"),");
        System.out.print(" expected: " + expected);
        System.out.println(", got: " + sqrtValue);
    }
}
```

Note how doubles
are compared.

```
public void testDataSet(double[][] data)
{
    for (int i = 0 ; i < data.length ; i++)
    {
        test(data[i][0], data[i][1], 0.00001);
    }
}

public void run()
{
    double[][] d1 = new double[][]
    {{1.0,1.0}, {2.0,1.4142135}, {3.0,1.7320508},
    {10.0,3.1622776}, {100.0,10.0}, {0.1,0.316227},
    {0.0,0.0}, {-1.0,Double.NaN}};
    testDataSet(d1);
}
```

Or read data
from a file.

But can do better than
this using a proper
testing framework

So, just how do you write sqrt anyway...

```
public static double sqrt(final double x) {
    final double precision = 0.0000001;
    if (x < 0.0) {
        return Double.NaN;
    }
    if (x <= precision) {
        return 0.0;
    }
    double a = 1.0;
    while (Math.abs(a*a - x) > precision) {
        a = (a + x/a)/2;
    }
    return a;
}
```

Newton Raphson approximation

Obvious boundary conditions

Potential overflow

Summary

- Test to find errors.
- Use a test harness program.
 - Let it do the repetitive hard work.
- Do enough tests to be confident in your code.

What does this mean for your code?

- Each method should be tested.
 - Check value returned for given parameter values.
 - For a void method, call a second method to observe the results.
 - e.g., adding an object to a data structure using void add(...), results in the size increasing by one.
- Need accurate specification of what method is meant to do.
- Use method implementation to focus on potential problems.
 - e.g., loop counting one too many/few times.