

# Visualising the Search Landscape of the Triangle Program

EuroGP 2017, Mauro Castelli *et al.*, [LNCS 10196](#), pages 96-113, Amsterdam

- No failed test cases
- 1 failed test case
- 2 failed test cases
- 3 failed test cases
- 4 failed test cases
- 5 failed test cases
- Vertical edge

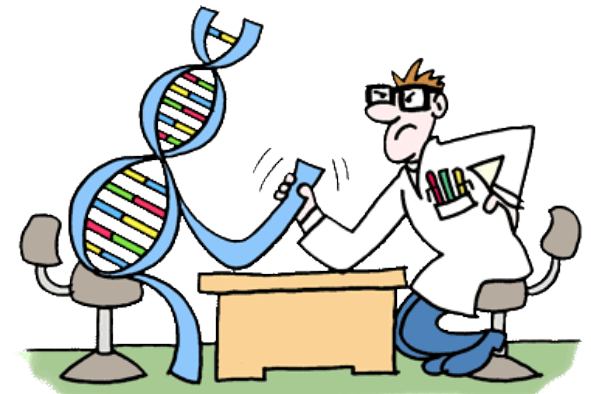
W. B. Langdon

Department of Computer Science



Humies

\$10,000 Human-Competitive Results



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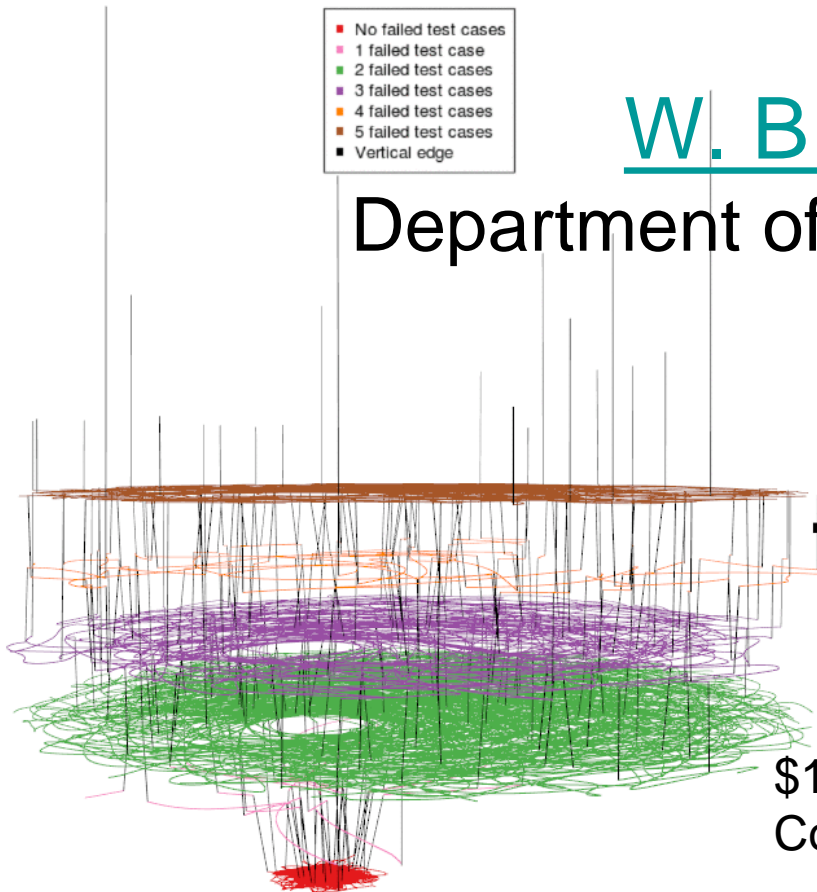
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# Fitness Landscape of the Triangle Program

- Background, what is Genetic Improvement
  - Fitness landscapes of genetic improvement
  - the Triangle program.
  - Constructing Triangle's fitness landscape
    - Two versions: binary and **all comparison changes**
- Results
  - searchspaces
  - schema analysis
  - Hill climbing and local optima visualisation
- Insight into Genetic Improvement?

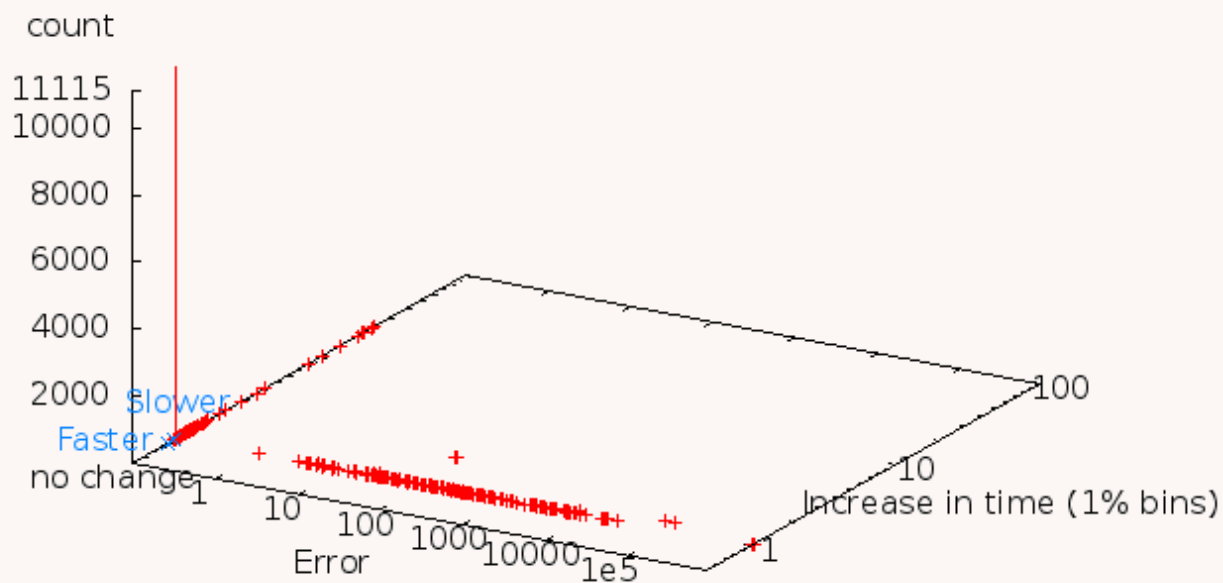
# Genetic Improvement

- Genetic Improvement is the application of search (often genetic programming) to improve existing software, e.g.
  - Fix bugs
  - Faster (CPU or on parallel hardware: GPU)
  - Less energy used
  - Less memory
- Real programs ( $10^4$  to  $10^6$  of lines of code)



# GI Mutation Fitness Landscapes

14,173 Successful single code mutations to BWA on execution path





89% mutations which compile make no change to test case [CS-DC'15](#)

BWA 0.7.12-r1039  
10958 lines of code

# GI Fitness Landscapes

- Real software is resilient to mutations.
- Schema (crossover) analysis.
- The Triangle program is a software engineering benchmark

# Triangle Program

- Given length of three sides what type is triangle?  
(Software Engineering benchmark)  
- Test suite (14) covers all paths [JSS 83\(12\) \(2010\) 2416–2430](#)
- Mutate conditionals
- Fitness is number of tests that fail (minimize)
- Code and datasets online  
<http://www.cs.ucl.ac.uk/staff/W.Langdon/egp2017/triangle/>
- whole landscape

All 17 comparisons are  
potential mutation sites.  
Shown in red

39 lines of C code

```

int gettri(int side1, int side2, int side3)
{
    int triang ;

    if( side1 <= 0 || side2 <= 0 || side3 <= 0){
        return 4;
    }

    triang = 0;

    if(side1 == side2){
        triang = triang + 1;
    }
    if(side1 == side3){
        triang = triang + 2;
    }
    if(side2 == side3){
        triang = triang + 3;
    }

    if(triang == 0){
        if(side1 + side2 <= side3 ||
side2 + side3 <= side1 || side1 + side3 <= side2){
            return 4;
        }
        else {
            return 1;
        }
    }

    if(triang > 3){
        return 3;
    }
    else if ( triang == 1 && side1 + side2 > side3) {
        return 2;
    }
    else if (triang == 2 && side1 + side3 > side2){
        return 2;
    }
    else if (triang == 3 && side2 + side3 > side1){
        return 2;
    }

    return 4;
}

```



## testcases\_oracle.txt

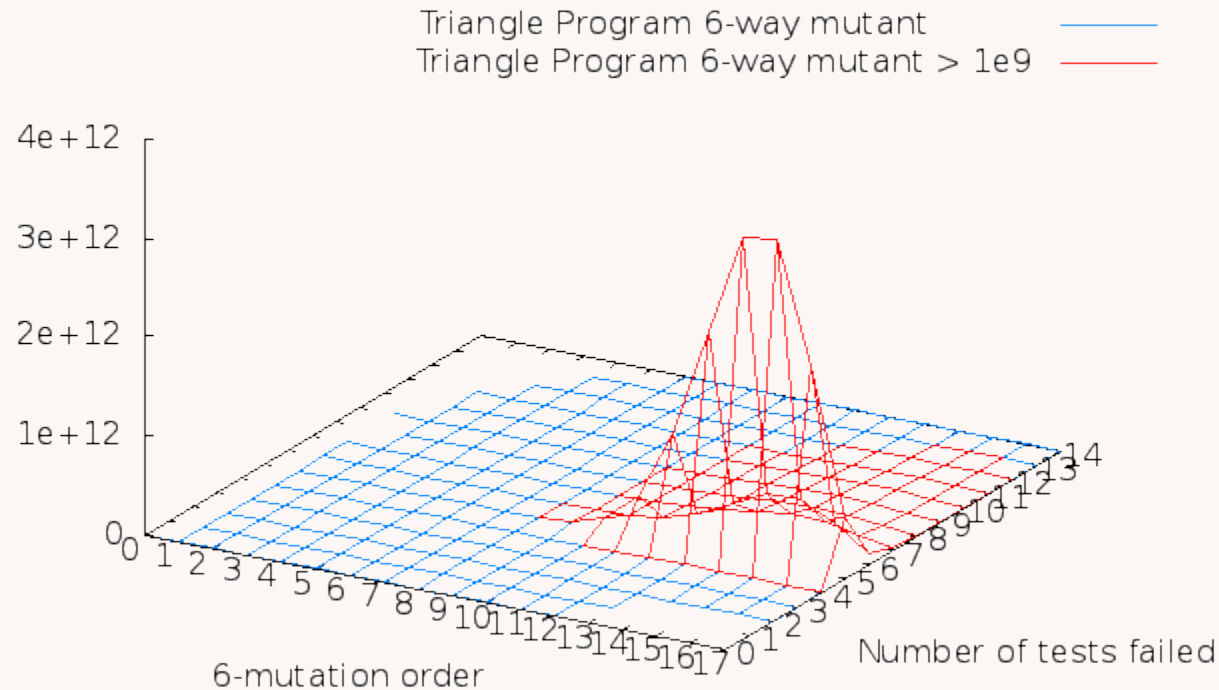
14 tests

	Three inputs	expected output
Inputs are the three sides of the triangle.	0 0 0	4
	1 0 0	4
	1 1 0	4
	1 1 1	3
Output is correct classification of the triangle.	2 2 1	2
	1 1 2	4
	2 1 2	2
	1 2 1	4
Test suite covers all paths but is not strong enough to detect all mutations.	2 1 1	4
	3 2 2	2
	3 2 1	4
	4 3 2	1
<a href="#">Dataset</a> gives whole test equivalent fitness landscape for 2-way comparisons.	2 3 1	4
	2 1 3	4

# Triangle Fitness Landscape

- Only mutate C comparison operators (17)
- Run all tests (14). For how many does new code give the wrong answer? (0-14)

# Triangle Program search space



wlangdon/eurogp2017

- Fitness distribution of all 16,926,659,444,735 mutations
- 78% of mutants fail five tests (mean 5.42, sd 1.05)
- 9215 global optima
- fitness distance correlation -0.070837

# Genetic Improvement Schema

Binary schema

**\*\*011\*0001\*0001\*\***      \* don't care

Triangle Program 17 locations

**\*\*\* == == == \*\*\*\*\* > \*\* == \* == \***

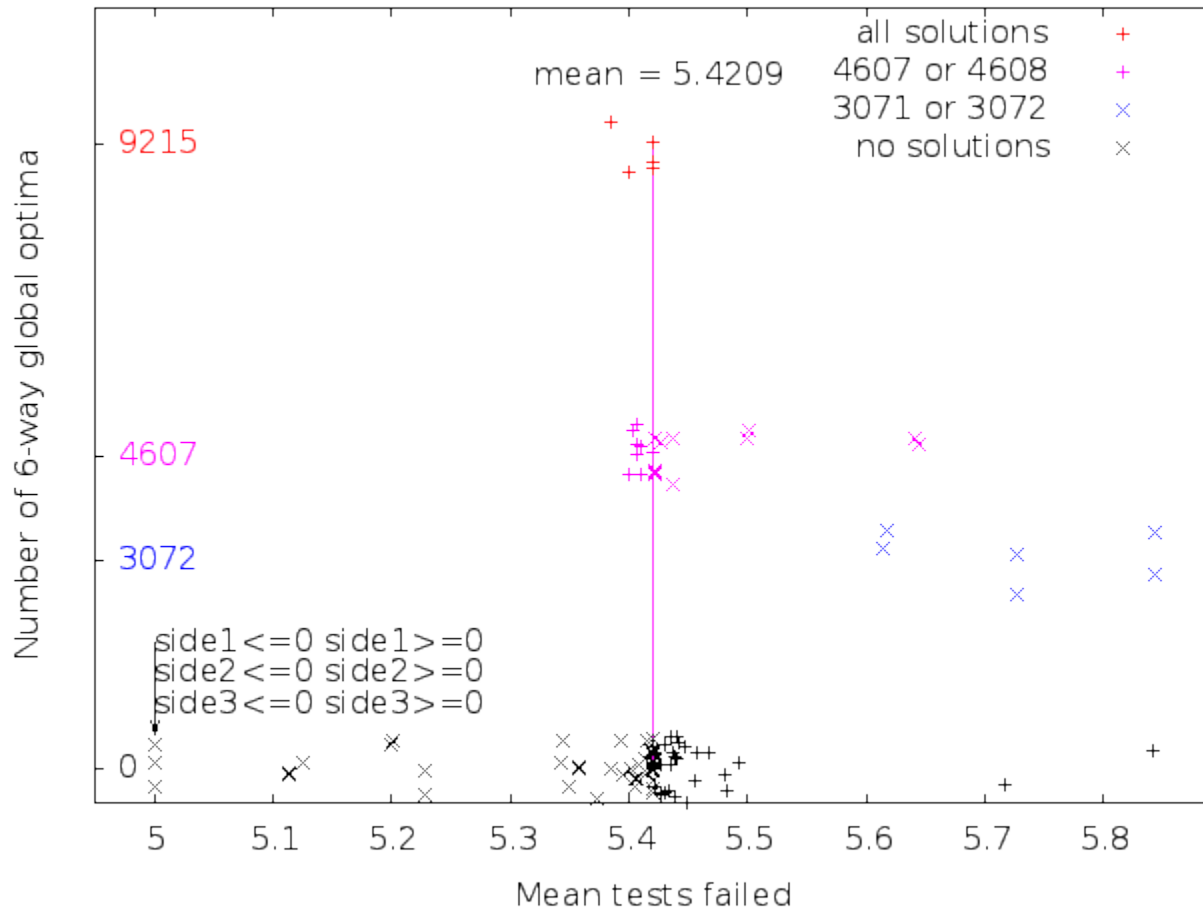
Example 1<sup>st</sup> order triangle schema

**>= \* \*\*\*\*\* \*\*\*\*\* \*\*\*\*\***

i.e. replace `if( side1 <= 0` with `if( side1 >= 0`

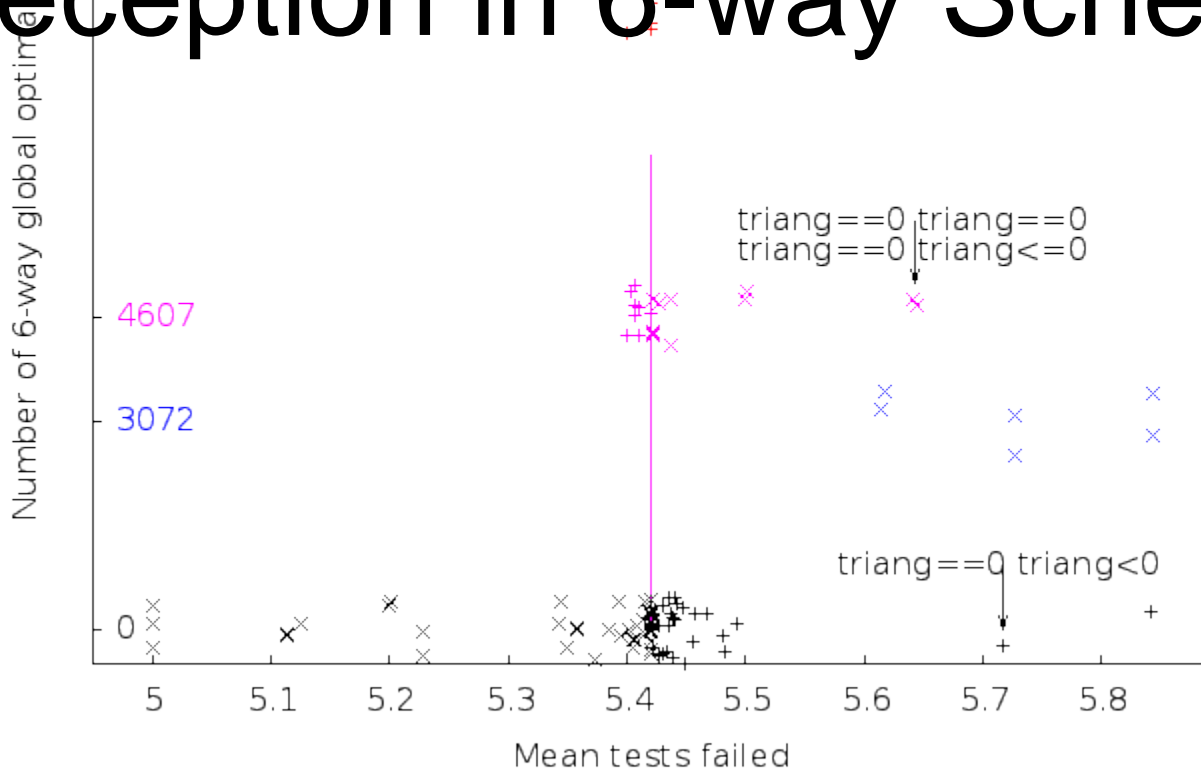
Deceptive schema has no solutions but its mean fitness is better than competing schema which contains solutions, vice-versa

# 102 First Order Schema



- $17 \times 6 = 102$  schema. 56 deceptive (x)
- 3 “best” get five tests wrong. This makes them better than average but contain no solutions
- (2-way, two alternatives only, schema are not deceptive)

# Deception in 6-way Schema

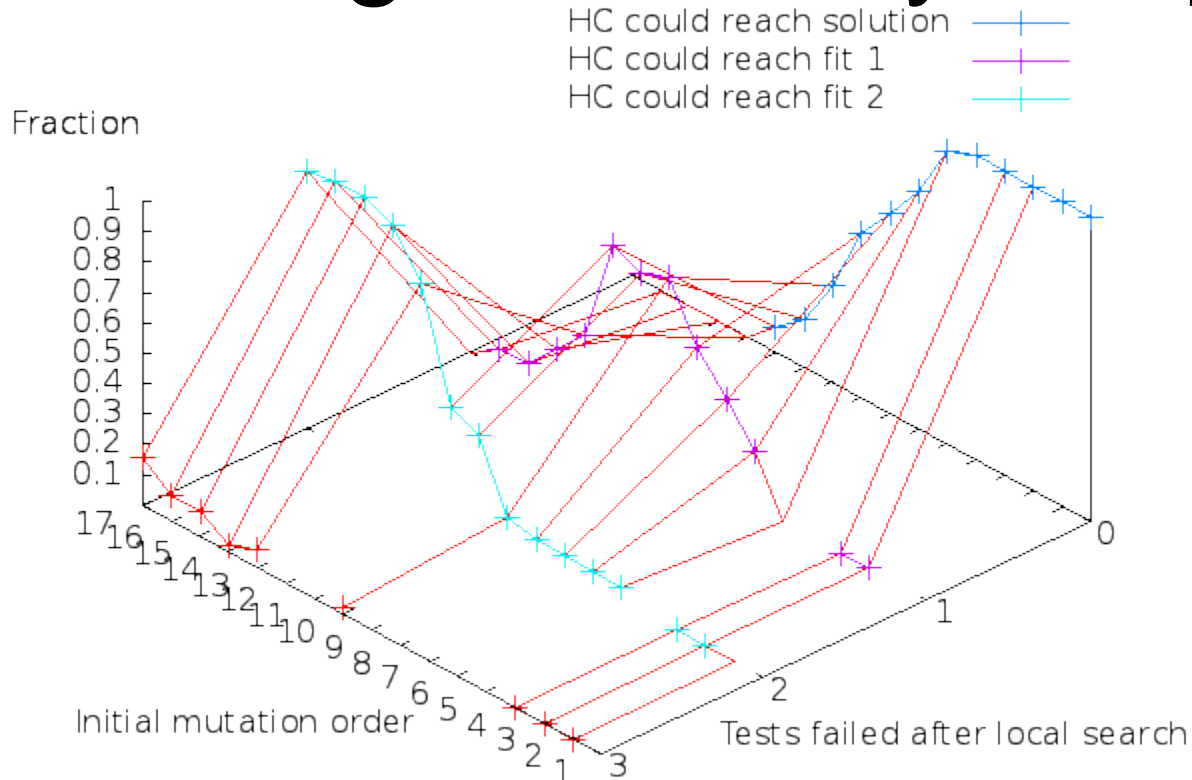


- 1<sup>st</sup> order cover the search space, i.e. far from start point. (two alternatives schema are closer to start point.)
- Strong epistasis so hard for naive GA and Hill Climbing.
- 1<sup>st</sup> order only have one defined position, often low signal to noise.  $\sigma \approx 1$  so  $\Delta/\sigma \ll 0.01$
- 20 schema where signal/noise  $\Delta/\sigma > 0.1$ , 18 are deceptive

# Summary 6-way 1<sup>st</sup> order Schema

- $17 \times 6 = 102$  schema. 56 deceptive( $\times$ )
- None with strong signal towards any solution
- Strong epistasis, low fitness distance correlation
- Hard for global search GA and Hill Climbing but GI starts search near solution
- 1<sup>st</sup> order only have one defined position, often low signal to noise.  $\sigma \approx 1$  so  $\Delta/\sigma \ll 0.01$
- 20 schema where signal/noise  $\Delta/\sigma > 0.1$ , 18 are deceptive
- 2-way case not deceptive. (Closer to solution?)

# Hill Climbing can always Improve

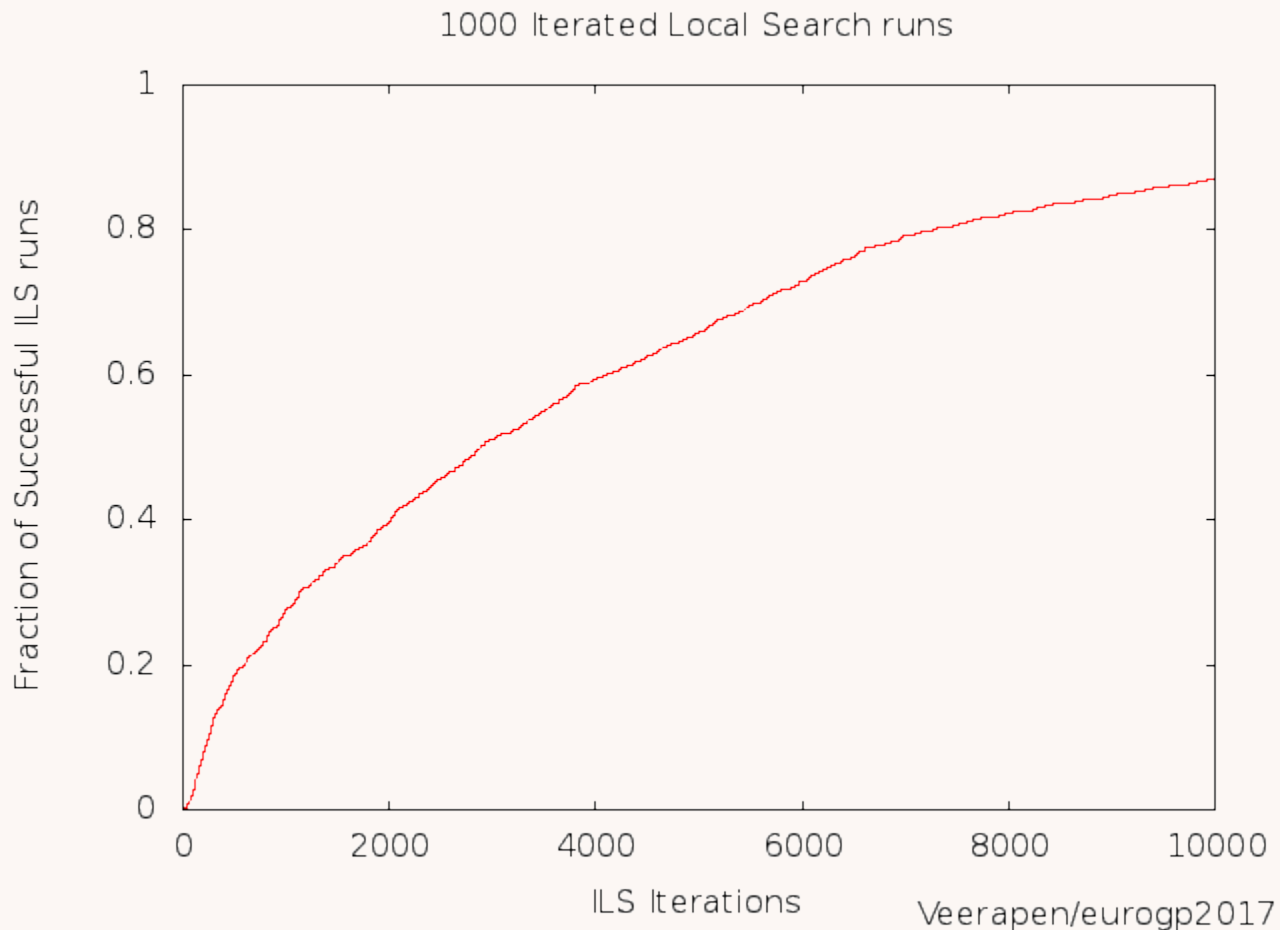


- Start from **7 mutations** or below, there probably is a route to **solution**.
- Start between **7 and 14** route to **fail just one test**
- Start between **11-17** fail at most **two tests**



# Iterated Local Search

87% of Iterated Local Search (ILS) find a program which passes all the tests.

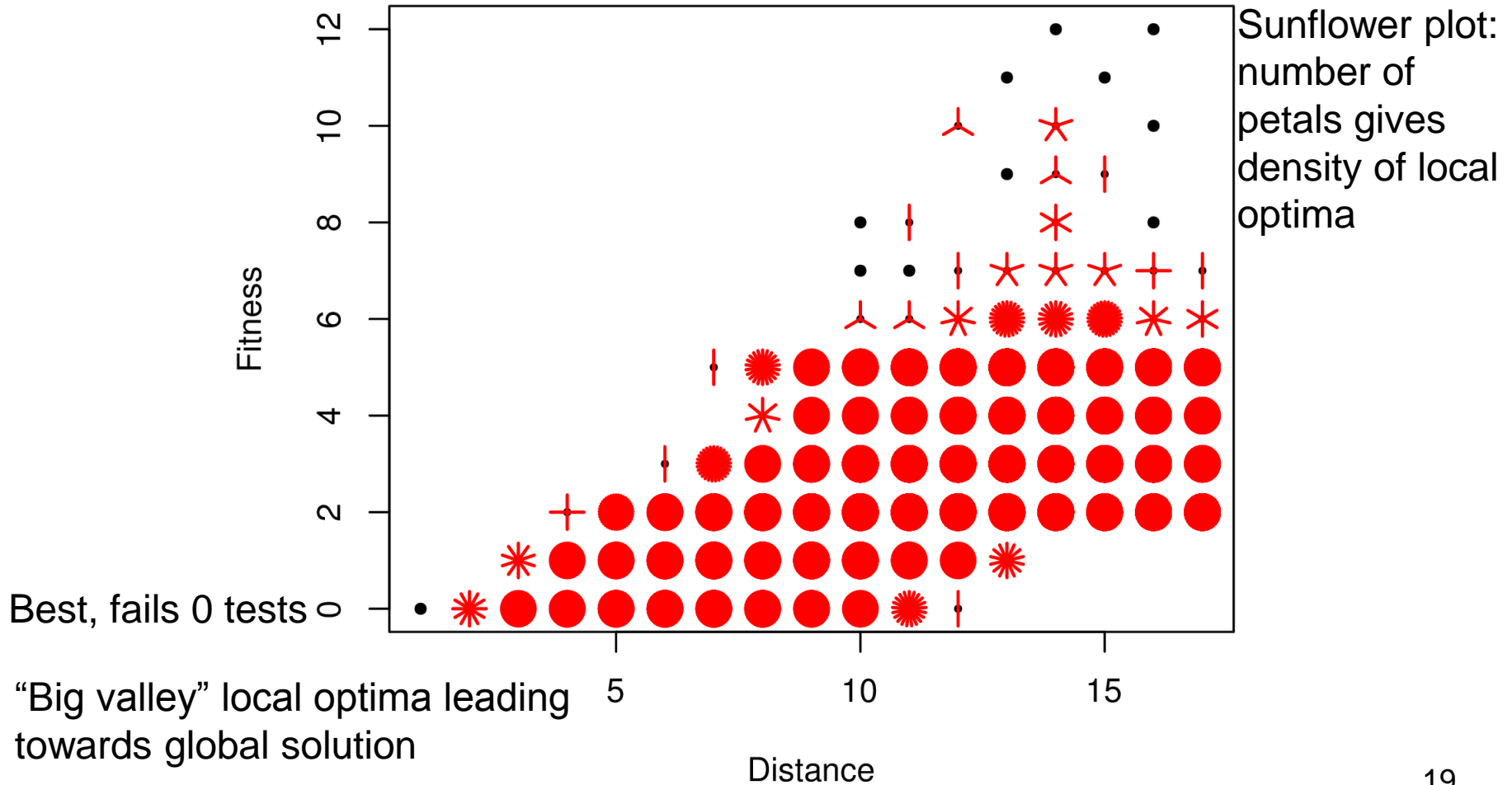


# Local Optima

- A solution is a local optimum if none of its neighbours have a better fitness value.
- In Triangle Program each mutant has  $5 \times 17 = 85$  neighbours.
- E.g. a mutants which fails 5 tests is a local optima if all of its 85 neighbours fail 5 or more tests.

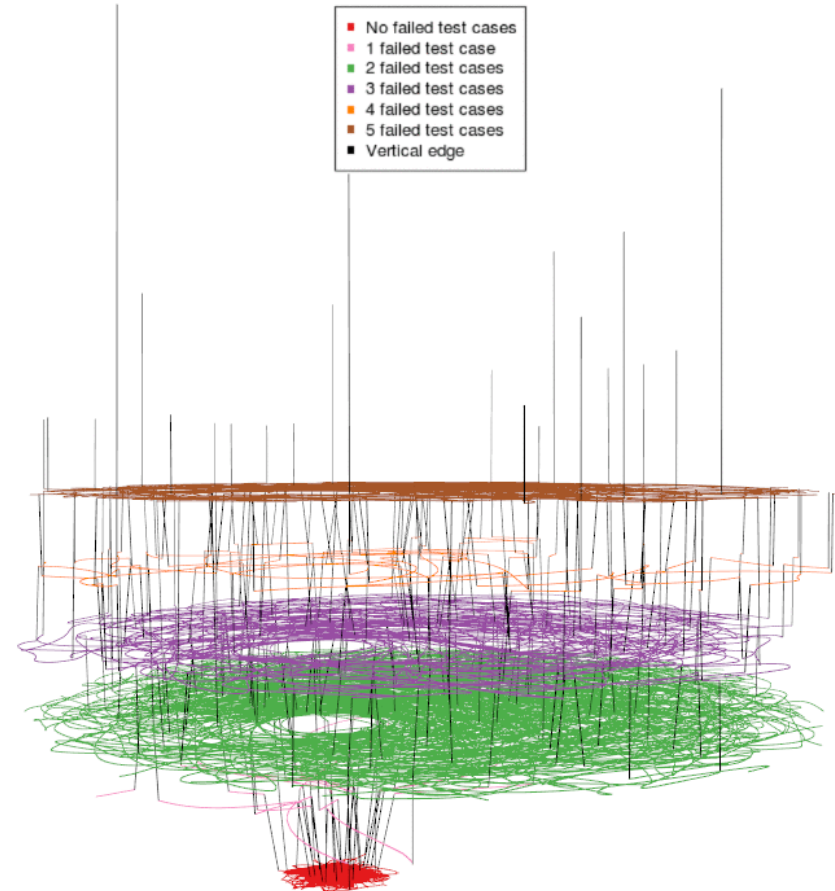
# Local Optima

1000 Iterated Local Searches (ILS) find  
2,372,805 unique local optima



# Path of 100 Iterated Local Searches

- First 1000 ILS iterations
- Only the edges shown.
- Black if fitness improves.
- Edges are coloured no fitness change.



# Conclusions

- Whole fitness landscape 16,926,659,444,735
  - 9215 pass all tests. Neutral moves & plateaus
- Global schema analysis
  - Low signal to noise, deceptive, epistasis.
  - 2-way closer to solution, no deception.
- “big valley” with many local optima, particularly close to global optima
- Hill climbing can always improve
- Iterated Local Search often finds solution.
- **Start near human code**

# White Queen



In Lewis Carroll's "Through the Looking-Glass..." the White Queen says she could believe "six impossible things before breakfast".

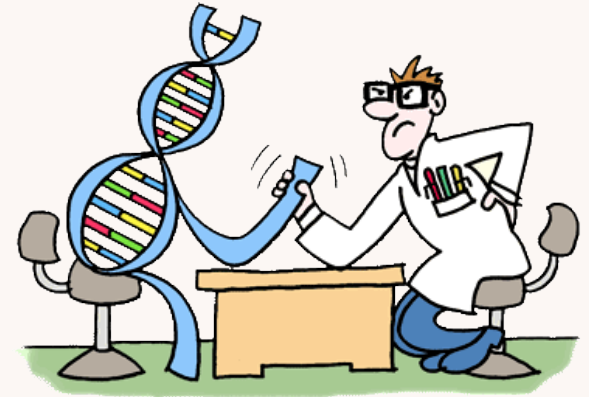
**Do** something impossible

**Evolve** something never attempted before

Humies

\$10000

Human-Competitive Results



END

<http://www.cs.ucl.ac.uk/staff/W.Langdon/>

<http://www.epsrc.ac.uk/> **EPSRC**

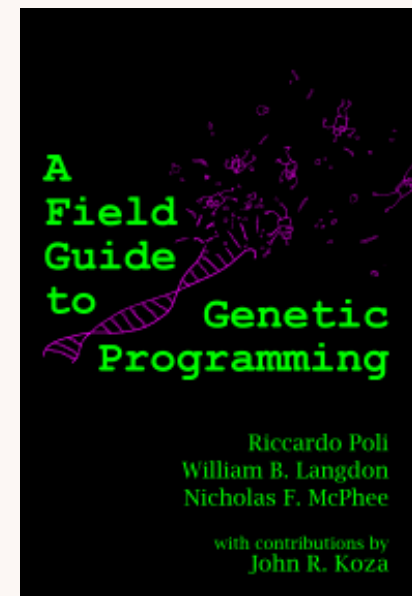
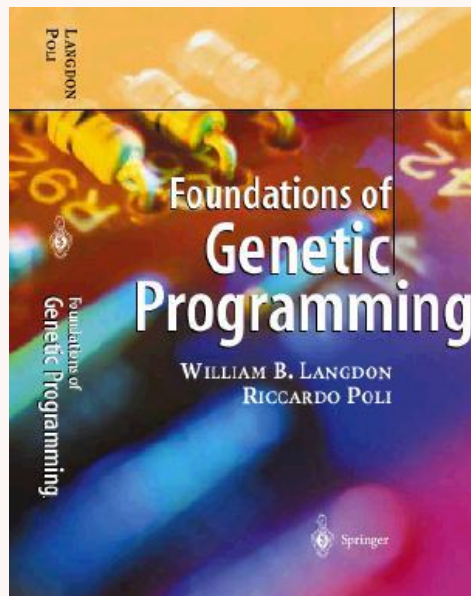
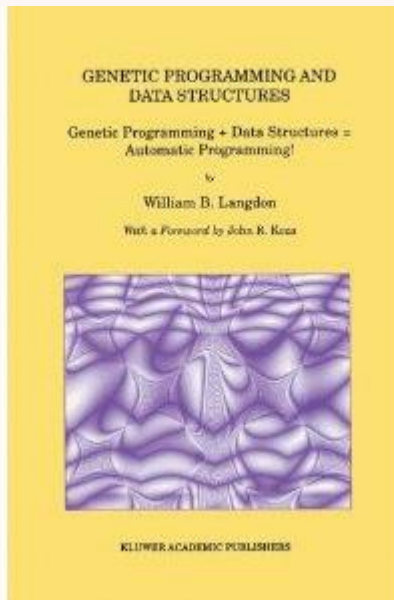
# Genetic Improvement



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# Discussion: Lessons for GI?

- With simple scalar fitness, almost everyone fails 5 tests.
- Need more fitness levels?
- Is “fitness” function too simple?
- Would a novelty reward help?
- Would multi-objective approach help?

# Discussion: Lessons for GI?

- Global search dominated by mutants which fail five of fourteen tests.
- 1<sup>st</sup> order, schema says global search hard
  - Epistasis, deception.
- ILS more practical than simple hillclimbing (HC)
- ILS shows big valley of local optima near global optima (human code)
- Even simple HC may work close to solution
- **START NEAR SOLUTION**

# Insight into Genetic Improvement?

- Triangle program is software engineering benchmark
  - small but akin to unit testing
- **Whole** fitness landscape
  - Much of search space passes most tests
  - Very few pass all tests
  - Large areas where neighbours pass 5 tests. **Neutral networks, plateaus.**
- **Global** schema analysis.
  - Low signal to noise, **deceptive**, epistasis
  - But (2-way mutation) closer to solution no deception.
- Many local optima, particularly close to global optima.
- Hill climbing can **always improve** (if allow neutral moves) but if start far from solution HC sometimes gets stuck.
- Iterated Local Search **often finds solution.**
- For global and hill climbing search **starting near human code** helps

All 17 comparisons are potential mutation sites. Shown in red

== replaced by <=  
> replaced by !=  
<= replaced by ==

(Chosen as they are the hardest to detect mutations.)

```
int gettri(int side1, int side2, int side3)
{
    int triang ;

    if( side1 <= 0 || side2 <= 0 || side3 <= 0){
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    }

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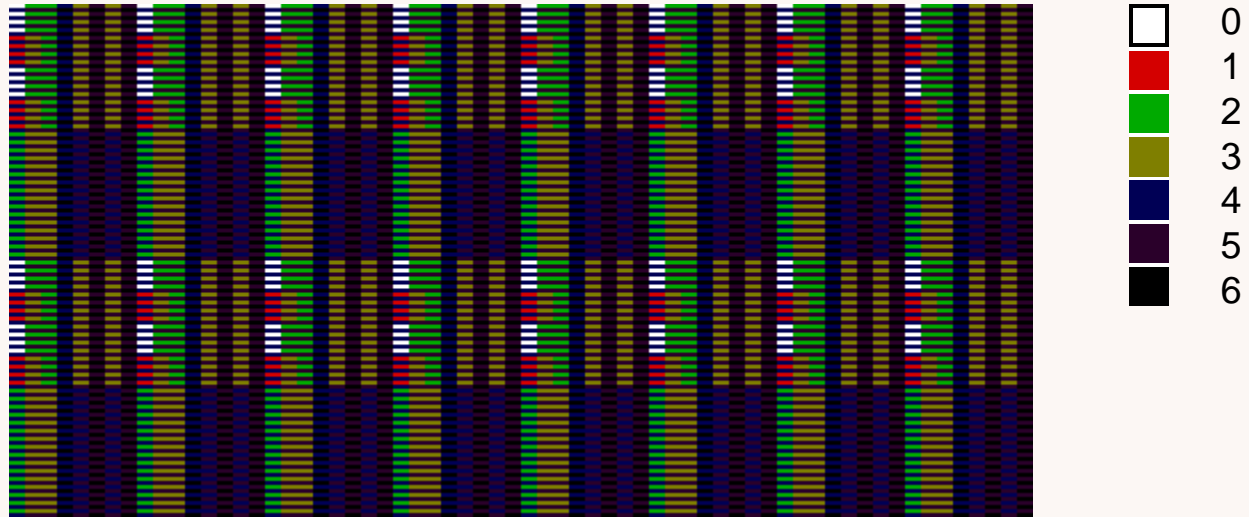
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```

# First Order Schema

Schema id	mean	sd	pop size	Pop size = $2sd_{12} /  \text{mean}_1 - \text{mean}_2 $
-4	3.719	$\pm 1.328$	1.9	
4	4.969	$\pm 1.075$		
-5	4.062	$\pm 1.478$	4.7	
5	4.625	$\pm 1.166$		
-6	3.812	$\pm 1.509$	2.4	
6	4.875	$\pm 0.927$		
-11	3.438	$\pm 1.273$	1.1	
11	5.250	$\pm 0.661$		
-14	4.312	$\pm 1.424$	43.5	
14	4.375	$\pm 1.293$		
-16	4.188	$\pm 1.550$	8.6	
16	4.500	$\pm 1.118$		

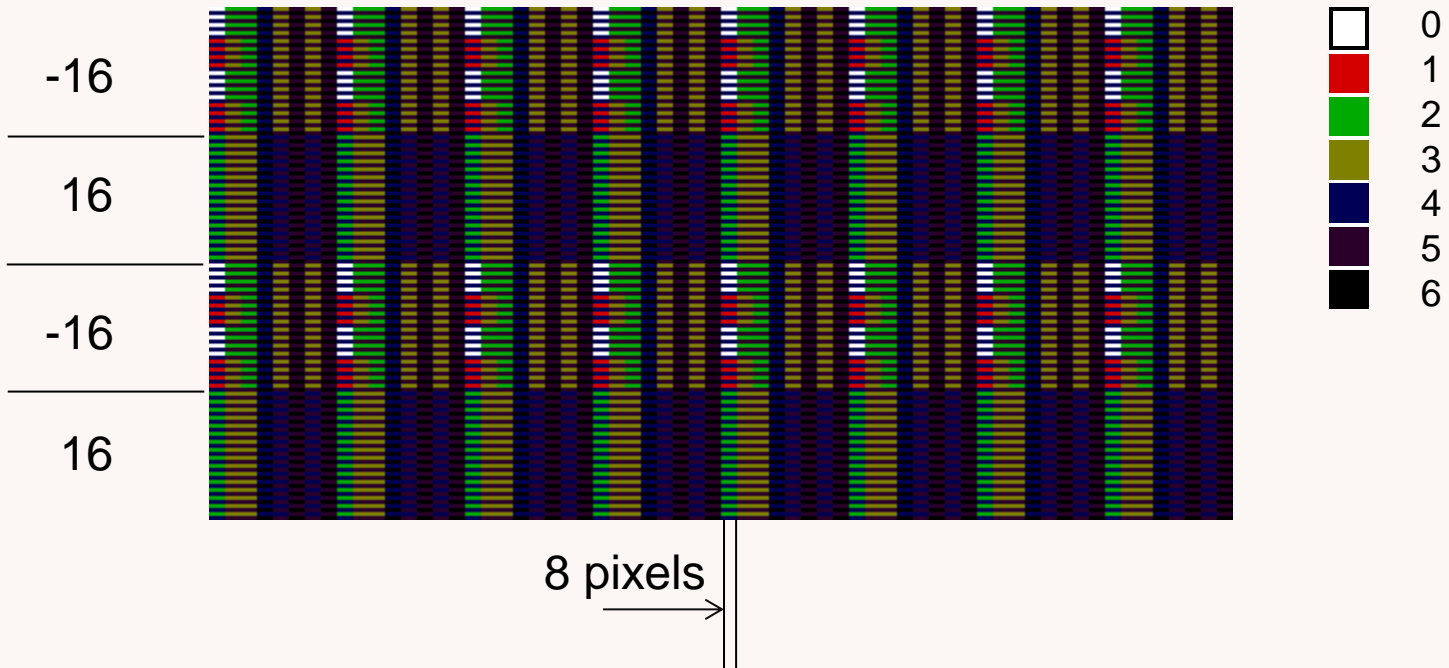
Table 2: Mean and standard deviation of number of tests failed for first order schema (excluding 22 with average means).

# Fitness in bit order ( $2^8 \times 2^9$ )



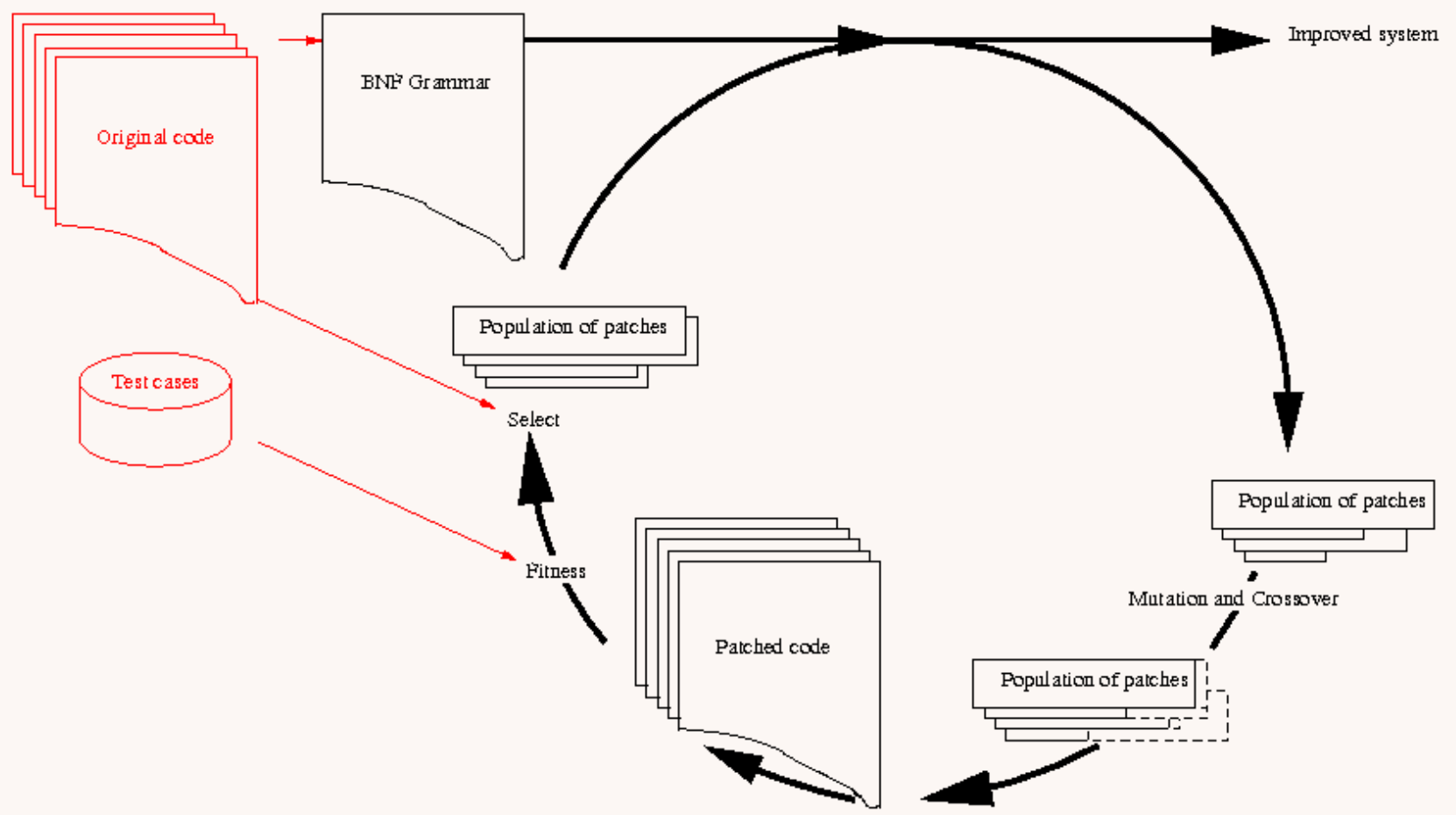
- 2048 global optima in white.
- Regular patterns indicate small building blocks.
- Vertical strips 8 pixels wide says first three bits do not impact fitness.
- Last but one bit gives four horizontal stripes:
  - two contain 50176 mutants fail  $\geq 4$  tests (dark)
  - others hold all the solutions (white)

# Fitness in bit order ( $2^8 \times 2^9$ )



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# Genetic Improvement evolves code patches





# Recent Successes of Genetic Improvement

- Automatic bug repair
  - [GenProg](#), e.g. 105 bugs fix most (multiple best papers, [IFIP TC2 Manfred Paul Award](#), 2 [Humies](#))
- Better programs
  - 70x [Bowtie2](#), [BarraCUDA](#), [pknots](#) 10000x
  - Less [energy](#), less [memory](#)
  - MOGA speed v. quality, e.g. [[SIGGRAPH](#)]
- Code transplant [[Marginean](#), e.g. best paper [ISSTA 2015](#)]
  - E.g. C++, code indent, call graph layout into [Kate](#) editor (we *can* evolve an editor) [Humie](#)

# Genetic Improvement Benchmarks

- Bugs to be fixed
  - GenProg <http://dijkstra.cs.virginia.edu/genprog/>
- Software Engineering
  - Many, e.g. SIR <http://sir.unl.edu>
- Fitness landscape
  - Mutation testing/GA fitness landscape for the Triangle Program, UCL CS [RN/16/05](http://www.cs.ucl.ac.uk/staff/W.Langdon/ppsn2016/triangle/)  
<http://www.cs.ucl.ac.uk/staff/W.Langdon/ppsn2016/triangle/>
  - Code and datasets online  
<http://www.cs.ucl.ac.uk/staff/W.Langdon/egp2017/triangle/>

# The Genetic Programming Bibliography

<http://www.cs.bham.ac.uk/~wbl/biblio/>

11484 references

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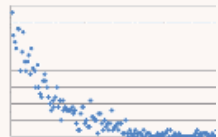
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