



Communications Software Engineering Condition Synchronization and Liveness

Wolfgang Emmerich

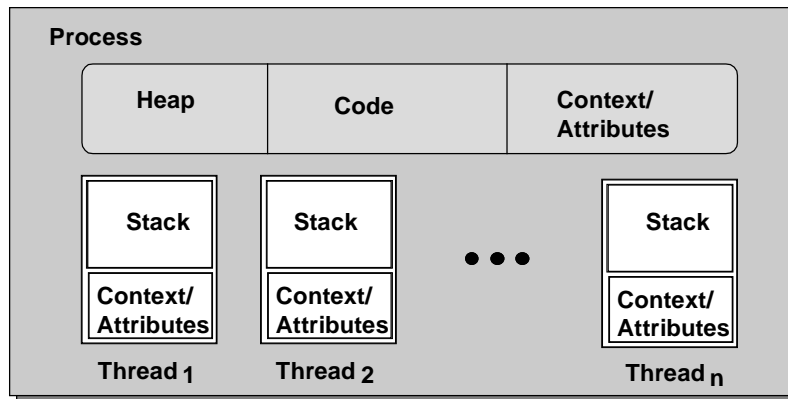


Lecture Overview

- ***Concurrency in Programming Languages***
- ***Mutual Exclusion***
- ***Condition Synchronization***
- ***Deadlocks***
- ***Liveness***



Threads and OS Processes



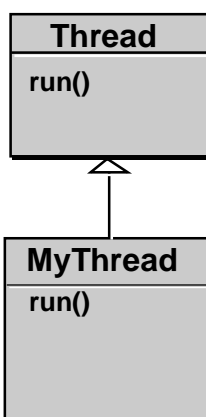
- OS process provides protected address space.
- Many threads may execute within space.
- Each thread: stack & context (saved registers).

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3



Threads using Inheritance



```
class MyThread extends Thread {
    public void run() {
        ...
    }
}
```

Creation of thread:

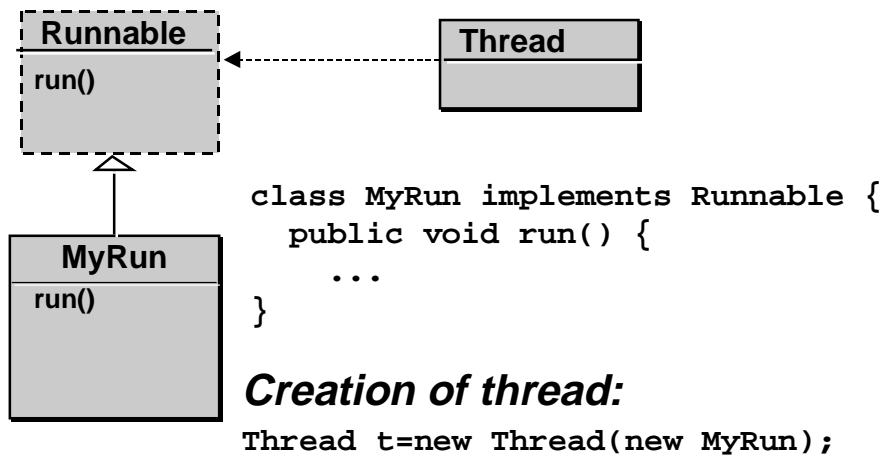
```
MyThread t=new MyThread();
```

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4



Threads implementing Interfaces



Thread Lifecycle

- **Started by start() which invokes run()**
- **Terminated when**
 - run() returns or
 - explicitly terminated by stop().
- **A started thread may be**
 - running or
 - runnable (waiting to be scheduled)
- **Thread gives up processor using yield().**
- **A thread may be suspended by suspend()**
- **If Suspended gets runnable by resume().**
- **sleep() suspends for a given time and then resumes**



FSP Model of Java Thread Lifecycle

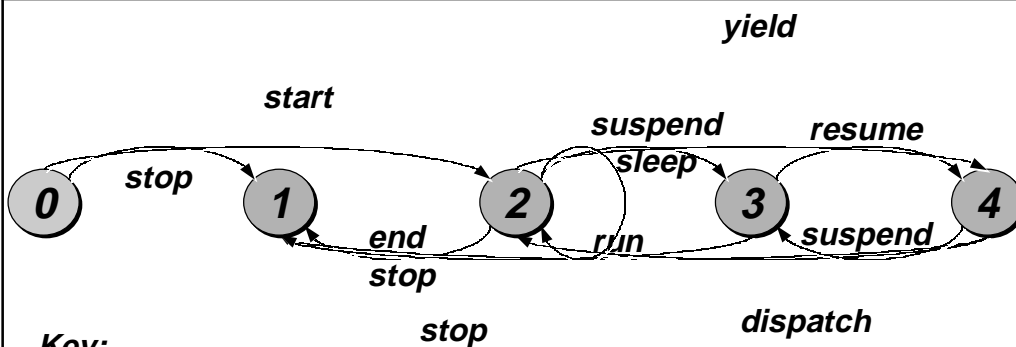
```

THREAD = CREATED,
CREATED = ( start -> RUNNING
           | stop -> TERMINATED),
RUNNING = ( {suspend,sleep}-> NON_RUNNABLE
           | yield -> RUNNABLE
           | {stop, end} ->TERMINATED
           | run -> RUNNING),
RUNNABLE= ( suspend -> NON_RUNNABLE
           | dispatch -> RUNNING
           | stop -> TERMINATED),
NON_RUNNABLE = ( resume ->RUNNABLE
                | stop -> TERMINATED),
TERMINATED = STOP.

```



LTS of Java Thread Lifecycle



Key:

- 0: CREATED
- 1: TERMINATED
- 2: RUNNING
- 3: NON_RUNNABLE
- 4: RUNNABLE



Example: Countdown Timer

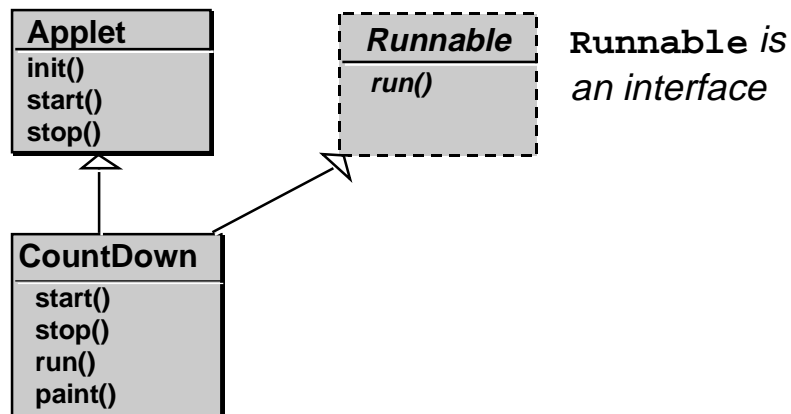
- **Demo: Countdown**

- **FSP of Countdown:**

```
COUNTDOWN (N=60) = COUNTDOWN[N],  
COUNTDOWN[i:0..N] =  
  ( when(i>0) tick->COUNTDOWN[i-1]  
    | when(i==0) beep->STOP  
  ).
```



Countdown Timer - Class diagram





CountDown Timer - Java class

```
import java.awt.*;           //windows toolkit
import java.applet.*;       //applet support
public class Countdown extends Applet implements Runnable{
    int counter; Thread cd;
    public void start() {    // create thread
        counter = 60; cd = new Thread(this); cd.start();
    }
    public void stop() { cd = null;}
    public void run() {     // executed by Thread
        while (counter>0 && cd!=null) {
            try{Thread.sleep(1000);}
            catch (InterruptedException e){}
            --counter; repaint(); //update screen
        }
    }
    public void paint(Graphics g) {
        if (counter>0)
            g.drawString(String.valueOf(counter),25,75);
        else g.drawString("Bang", 10, 50);
    }
}
```



Concurrent Threads

- *Parallel composition operator* | |
- *Implemented by creation of several new thread objects*
- **Example: ThreadDemo**
- *Creates two thread objects that execute concurrently*

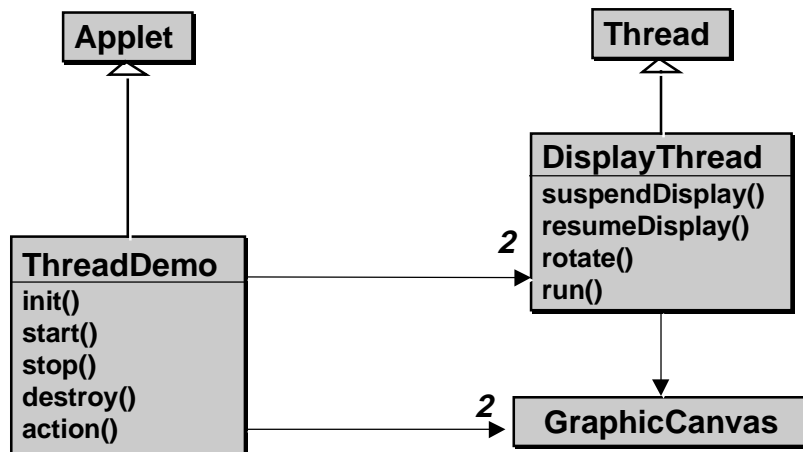


FSP Spec of Thread Demo

```
DISPLAY_THREAD = SUSPENDED,  
SUSPENDED = ( resume->RUNNING ),  
RUNNING = ( rotate->RUNNING  
           | suspend->SUSPENDED  
           ).  
|| THREAD_DEMO =  
  ( a:DISPLAY_THREAD | | b:DISPLAY_THREAD ).
```



Class Diagram of ThreadDemo





Summary

- ***Threads vs. operating system processes***
- ***Threads through class inheritance / interface implementation***
- ***Thread lifecycle***
- ***Concurrent threads by creating new thread objects***
- ***Class diagrams***
- ***Next: Java Thread Programming Lab***

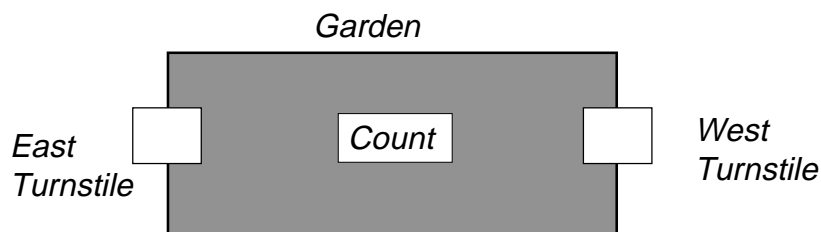


Mutual Exclusion



Ornamental Garden Problem

- Garden open to the public
- Enter through either one of two turnstiles
- Computer to count number of visitors



- Each turnstile implemented by a thread

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17



Ornamental Garden: Counter class

```
class Counter {
    int value_=0;
    public void increment() {
        int temp = value_; //read
        Simulate.interrupt();
        ++temp;             //add1
        value_=temp;       //write
    }
}
```

- Simulated interrupt calls `yield()` to force thread switch.

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18



Ornamental Garden: Turnstile class

```
class Turnstile extends Thread {
    Counter people_;
    Turnstile(Counter c) {
        people_ = c;
    }
    public void run() {
        while(true)
            people_.increment();
    }
}
```

■ *For full implementation see online version*



Ornamental Garden: Program

```
Counter people_ = new Counter();
Turnstile west_ = new Turnstile(people_);
Turnstile east_ = new Turnstile(people_);
west_.start();
east_.start();
```

■ *What will happen?*

Demo: Ornamental Garden



FSP Spec of Ornamental Garden

```
const N = 3 range T = 0..N
VAR = VAR[0],
VAR[u:T] = (read[u] -> VAR[u]
            | write[v:T]-> VAR[v]).
TURNSTILE = ( arrive -> INCREMENT
             | suspend-> resume-> TURNSTILE),
INCREMENT = (val.read[x:T] -> val.write[x+1]->
             TURNSTILE)+{val.read[T],val.write[T]}.
||GARDEN = (east:TURNSTILE || west: TURNSTILE
           || {east,west}::val:VAR
           )/{stop/east.suspend,
             stop/west.suspend,
             start/east.start,
             start/west.start}.
```

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Interference

- ***FSP spec supports the following trace:***
east.arrive→*east.val.read.0*→*west.arrive*→
west.val.read.0→*east.val.write.1*→*west.val.write.1*
- ***This is an example of a destructive update***
- ***Destructive updates caused by arbitrary interleaving of read and write actions on shared variables is called interference***
- ***Avoid interference by making access to critical sections mutually exclusive***



Critical Section

- A critical section is a sequence of actions that must be executed by at most one process or thread at a time
- Can be found by searching for sections of code that access or update variables or objects that are shared by concurrent processes.



Modelling Mutual Exclusion

- A lock can be modelled by:
`LOCK = (acquire->release->LOCK).`
- Attaching lock to shared resource (VAR):
`||LOCKVAR = (LOCK || VAR).`
- Critical section acquires/releases lock:
`INCREMENT = (value.acquire ->
val.read[x:T] -> val.write[x+1]->
value.release -> TURNSTILE)
+{val.read[T],val.write[T]}.`



Critical Sections in Java

- **Synchronised methods implement mutual exclusion**

- **Implicitly locking objects**

```
class Counter {
    int value_=0;
    public synchronized void increment() {
        int temp = value_; //read
        Simulate.interrupt();
        ++temp;           //add1
        value_=temp;     //write
    }
}
```

Demo: Correct Ornamental Garden



Synchronised Statements in Java

- **Locks on individual objects:**

```
public void run() {
    while(true)
        synchronized(people_){
            people_.increment();
        }
}
```

- **Less elegant than synchronized methods**
- **More efficient than synchronized methods**



Semaphores and Monitors



Semaphores

- ***Introduced by Dijkstra' in 1968***
- ***ADT with counter and waiting list***

P/Wait/Down:

```
if (counter > 0)
  counter--
else
  add caller to
  waiting list
```

S/Signal/Up:

```
if (threads wait)
  activate waiting
  thread
else
  counter++
```



Semaphores and Mutual Exclusion

- *One semaphore for each critical section*
- *Initialize semaphore to 1.*
- *Embed critical sections in wait/signal pair*
- *Example in Java:*

```
Semaphore S=new Semaphore(1);  
S.down();  
<critical section>  
S.up();
```

Demo: Semaphores



Evaluation of Semaphores

- + *Nice and simple mechanism*
- + *Can be efficiently implemented*
- + *Available in every programming language*
- *Too low level of abstraction*
- *Unstructured use of signal and wait leads to spaghetti synchronisation*
- *Error prone and errors are dangerous*
 - *Omitting signal leads to deadlocks*
 - *Omitting wait leads to safety violations*





Semaphore in Java

```
class Semaphore {
    private int value_;
    Semaphore (int initial) {
        value_ = initial;
    }
    synchronized public void up() {
        ++value_;
        notify();
    }
    synchronized public void down() {
        while (value_== 0) {
            try {wait();}
            catch (InterruptedException e){}
        }
        --value_;
    }
}
```

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31



Critical Regions

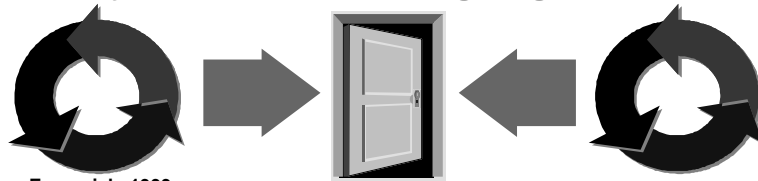
- ***Guarantee mutual exclusion by definition***
- ***Note subtle difference to critical sections***
- ***language features implement critical regions***
- ***Example: Java synchronised method***

32



Monitors

- **Hoare's response to Dijkstra's semaphores**
 - *Higher-level*
 - *Structured*
- **Monitors encapsulate data structures that are not externally accessible**
- **Mutual exclusive access to data structure enforced by compiler or language run-time**



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33



Monitors in Java

- **All instance and class variables need to be private *OR* protected**
- **All methods need to be synchronised**
- **Example: semaphore implementation**
- **Use of Monitors: Carpark Problem**

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34



Carpark Problem

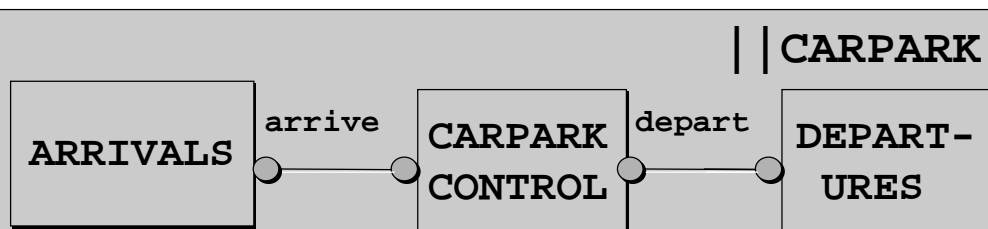
- *Only admit cars if carpark is not full*
- *Cars can only leave if carpark is not empty*
- *Car arrival and departure are independent threads*

Demo: CarPark



Carpark Model

- *Events or actions of interest:*
 - *Arrive and depart*
- *Processes:*
 - *Arrivals, departures and carpark control*
- *Process and Interaction structure:*





Carpark FSP Specification

```
CARPARKCONTROL(N=4) = SPACES[N],
SPACES[i:0..N] =
    (when(i>0) arrive-> SPACES[i-1]
    |when(i<N) depart-> SPACES[i+1]
    ).
ARRIVALS = (arrive-> ARRIVALS).
DEPARTURES = (depart-> DEPARTURES).
|| CARPARK =
    (ARRIVALS || CARPARKCONTROL || DEPARTURES).
```

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Java Class Carpark

```
public class Carpark extends Applet {
    final static int N=4;
    public void init() {
        CarParkControl cpk = new CarParkControl(N);
        Thread arrival,departures;
        arrivals=new Thread(new Arrivals(cpk));
        departures=new Thread(new Departures(cpk));
        arrivals.start();
        departures.start();
    }
}
```



Java Classes Arrivals & Departures

```
public class Arrivals implements Runnable {
    CarParkControl carpark;
    Arrivals(CarParkControl c) {carpark = c;}
    public void run() {
        while (true) carpark.arrive();
    }
}

class Departures implements Runnable {
    ...
    public void run() {
        while (true) carpark.depart();
    }
}
```



Java Class CarParkControl (Monitor)

```
class CarParkControl { // synchronisation?
    private int spaces;
    private int N;
    CarParkControl(int capacity) {
        N = capacity;
        spaces = capacity;
    }
    synchronized public void arrive() {
        ... -- spaces; ... } { // Block if full?
    synchronized public void depart() {
        ... ++ spaces; ... { // Block if empty?
    }
}
}
```



Problems with CarParkControl

- ***How do we send arrivals to sleep if car park is full?***
- ***How do we awake it if space becomes available?***
- ***Solution: Condition synchronisation***



Condition Synchronization



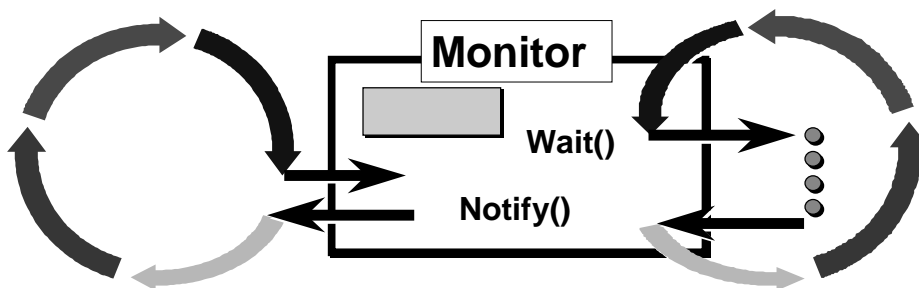
Thread Waiting Queues in Java

- `public final void notify()`
Wakes up a single thread that is waiting on this object's queue
- `public final void notifyAll()`
Wakes up all threads that are waiting on this object's queue
- `public final void wait()`
throws `InterruptedException`
Waits to be notified by another thread when notified must reacquire monitor



Condition synchronisation in Java

- *Thread enters monitor when it acquires mutual exclusion lock of monitor*
- *Thread exits monitor when releasing lock*
- *Wait causes thread to exit monitor*





Semaphore as a Java Monitor

```
class Semaphore {
    private int value_;
    Semaphore (int initial) {
        value_=initial;
    }
    public synchronised up() {
        ++value_;
        notify();
    }
    public synchronised down() {
        while (value_==0) wait();
        --value;
    }
}
```

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45



Condition Synchronisation in Java

- **FSP Model: when cond act -> NEWSTATE**

- **Java:**

```
public synchronized void act()
throws InterruptedException
{
    while (! cond) wait();
    // modify monitor data
    notifyAll();
}
```

- **Loop re-tests cond to make sure that it is valid when it re-enters the monitor**

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46



CarParkControl revisited

```
class CarParkControl {
    private int spaces;
    private int N;
    synchronized public void arrive() {
        while (spaces<=0) {
            try {
                wait();
            } catch(InterruptedException e){}
        }
        --spaces;
        notify();
    }
}
```

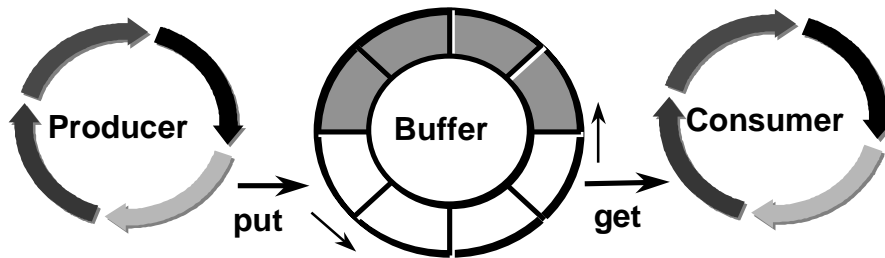


FSP and Condition Synchronisation

- ***For each guarded action in the FSP model of a monitor***
 - *Implement action as a synchronised method*
 - *That invokes `wait()` in a while loop before it begins*
 - *While condition is negation of guard condition*
- ***Every change in the monitor are signalled to waiting threads using `notify()` or `notifyAll()`***



Example: Producer/Consumer



Demo



Producer Consumer in FSP

```
PRODUCER = (put -> PRODUCER).  
CONSUMER = (get -> CONSUMER).  
BUFFER(SIZE=5) = BUFFER[0],  
BUFFER[count:0..SIZE] = (  
    when (count<SIZE) put->BUFFER[count+1]  
    |when (count>0) get -> BUFFER[count-1]).  
|| PC=(PRODUCER | | BUFFER | | CONSUMER).
```

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Bounded Buffer - Outline

```
class Buffer {
    private protected Object[] buf;
    private protected int in = 0; //index put
    private protected int out = 0; //index get
    private protected int count = 0; //no items
    private protected int size;
    Buffer(int size) {
        this.size = size;
        buf = new Object[size];
    }
    synchronized public void put(Object o) {...}
    synchronized public Object get() {...}
}
```



Bounded Buffer - put

```
synchronized public void put(Object o) {
    while (count==size) {
        try {
            wait();
        } catch (InterruptedException e) {}
    }
    buf[in] = o;
    ++count;
    in=(in+1) % size;
    notify(); // [count>0]
}
```



Bounded Buffer - get

```
synchronized public Object get() {
    while (count==0) {
        try {
            wait();
        } catch (InterruptedException e){}
    }
    Object o =buf[out];
    buf[out]=null; // for display purposes
    --count;
    out=(out+1) % size;
    notify(); // [count < size]
    return (o);
}
```

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53



Monitor Invariants

- **Monitor invariant is assertion concerning attributes encapsulated by monitor**
- **Assertion must hold when no thread is in monitor**
- **Examples:**
 - **CarParkControl: $0 \leq \text{spaces} \leq N$**
 - **Semaphore: $0 \leq \text{value}$**
 - **BoundedBuffer: $(0 \leq \text{count} \ \&\& \ 0 \leq \text{in} \leq \text{size} \ \&\& \ 0 \leq \text{out} \leq \text{size} \ \&\& \ \text{in} = (\text{out} + \text{count}) \% \text{size})$**
- **Used to reason about correctness monitors**

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54



Summary

- *Condition synchronization*
- *In Java using `wait()`, `notify()` and `notifyAll()`*
- *Used to implement Semaphores in Java*
- *Relation between FSP model and implementation in Java monitor*
- *Monitor invariants*



Deadlocks



Goals

- *Reader/Writer problem*
- *Starvation*
- *Dining Philosophers Problem*
- *Deadlocks*
- *Liveness Analysis using LTS*



Reader / Writer Problem

- *Monitors and Java's synchronize statement guarantee mutual access to objects / methods*
- *Often it is ok for multiple readers to access the object concurrently*
- *Properties required:*

Demo: Reader/Writer



Read/Write Monitor

```
class ReadWrite {
  private protected int readers = 0;
  private protected boolean writing = false;
  // Invariant: (readers>=0 and !writing) or
  // (readers==0 and writing)
  synchronized public void acquireRead() {
    while (writing) {... wait(); ...} ++readers;
  }
  synchronized public void releaseRead() {
    --readers; if(readers==0) notify();
  }
  synchronized public void acquireWrite() {
    while (readers>0||writing) {... wait(); ...}
    writing = true;
  }
  synchronized public void releaseWrite() {
    writing = false; notifyAll();
  }
}
```

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Starvation

59



Writer Starvation

- ***NotifyAll awakes both readers and writers***
- ***Program relies on Java having a fair scheduling strategy***
- ***When readers continually read resource: Writer never gets chance to write. This is an example of starvation.***
- ***Solution: Avoid writer starvation by making readers defer if there is a writer waiting***

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60



Read/Write Monitor (Version 2)

```
class ReadWrite {
  ... // as before
  private int waitingW = 0; // # waiting Writers
  synchronized public void acquireRead() {
    while (writing || waitingW > 0) {... wait(); ... }
    ++readers;
  }
  synchronized public void releaseRead() {... }
  synchronized public void acquireWrite() {
    while (readers > 0 || writing) {
      ++waitingW; ... try{ wait(); ... --waitingW; }
      writing = true;
    }
  }
  synchronized public void releaseWrite() {... }
}
```

Demo: Reader/Writer v2



Reader Starvation

- ***If there is always a waiting writer:
Readers starve***
- ***Solution: Alternating preference between
readers and writers***
- ***To do so: Another boolean attribute
readersturn in Monitor that indicates whose
turn it is***
- ***readersturn is set by releaseWrite() and
cleared by releaseRead()***



Read/Write Monitor (Version 3)

```
class ReadWrite {
  ... // as before
  private boolean readersturn = false;
  synchronized public void acquireRead() {
    while(writing || (waitingW>0 && !readersturn))
      { ... wait(); ... }
    ++readers;
  }
  synchronized public void releaseRead() {
    --readers; readersturn=false;
    if(readers==0) notifyAll();
  }
  synchronized public void acquireWrite() {... }
  synchronized public void releaseWrite() {
    writing=false; readersturn=true; notifyAll();
  }
}
```

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Demo: Reader/Writer v3

63



Deadlocks

- ***Process is in a deadlock if it is blocked waiting for a condition that will never become true***
- ***Process is in a livelock if it is spinning while waiting for a condition that will never become true (busy wait deadlock)***
- ***Both happen if concurrent processes and threads are mutually waiting for each other***
- ***Example: Dining philosophers***

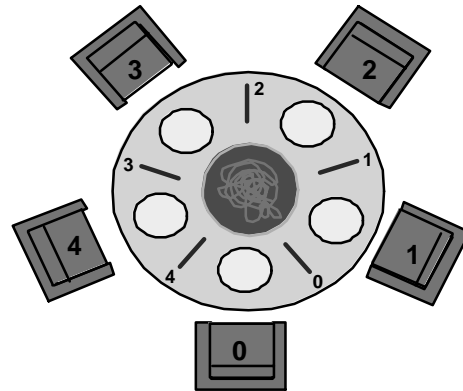
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64



Dining Philosopher Problem

- 5 Philosophers sit around table
- They think or eat
- Eat with 2 chopsticks
- Only 5 chopsticks available
- Each philosopher only uses sticks to her left and right



FSP Model of Dining Philosophers

```
PHIL=(hungry->left.get->right.get->eating->
      left.put->right.put->thinking->PHIL).
FORK = (left.get-> left.put -> FORK
        |right.get->right.put -> FORK).
|| COLLEGE(N=5)=
(phi[0..N-1]:PHIL| |fork[0..N-1]:FORK)
/{phi[i:0..N-1].left/fork[i].left,
 phi[i:0..N-1].right/fork[((i-1)+N)%N].right}.
```

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Dining Philosophers in Java

```
class Philosopher extends Thread {
    int identity;
    Chopstick left; Chopstick right;
    Philosopher(Chopstick left, Chopstick right) {
        this.left = left; this.right = right;
    }
    public void run() {
        while (true) {
            try {
                sleep(...);           // thinking
                right.get(); left.get(); // hungry
                sleep(...);           // eating
                right.put(); left.put();
            } catch (InterruptedException e) {}
        }
    }
}
```

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67



Chopstick Monitor

```
class Chopstick {
    boolean taken=false;
    synchronized void put() {
        taken=false;
        notify();
    }
    synchronized void get() throws
        InterruptedException {
        while (taken) wait();
        taken=true;
    }
}
```

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68



Applet for Diners

```
for (int i =0; i<N; ++I)
  // create Chopsticks
  stick[i] = new Chopstick();
for (int i =0; i<N; ++i){
  // create Philosophers
  phil[i]=new Philosopher(
    stick[(i-1+N)%N],stick[i]);
  phil[i].start();
}
```

Demo: Diners



Deadlock in Dining Philosopher

- *If each philosopher has acquired her left chopstick the threads are mutually waiting for each other*
- *Potential for deadlock exists independent of thinking and eating times*
- *Only probability is increased if these times become shorter*



Analysing cause of Deadlock

- ***We can use LTS for deadlock analysis***
- ***A dead state in the composed LTS is one that does not have outgoing transitions***
- ***Are these dead states reachable?***
- ***Use of reachability analysis***
- ***Traces to dead states helps understanding the causes of a deadlock***

LTSA



Deadlock Avoidance

- ***Deadlock in dining philosophers can be avoided if one philosopher picks up sticks in reverse order (right before left).***

Demo: Deadlock free Diners

- ***What is the problem with this solution?***
- ***Are there other solutions?***
- ***Deadlock can also be avoided if there is always one philosopher who thinks***



Summary

- *Reader / Writer Problem*
- *Starvation*
- *Avoidance of Starvation*
- *Dining Philosophers Problem*
- *Deadlocks and Livelocks*
- *Deadlock Avoidance*
- *Next Session: Safety*



Liveness & Progress



Motivation

- ***Problem with single lane bridge:***
- ***Cars cannot pass from north to south if there is a continuous stream of cars from south to north!***
- ***We would like to guarantee that cars will eventually cross the bridge.***
- ***In more general terms this is referred to as liveness***



Liveness

- ***A liveness property asserts that something good eventually happens.***
- ***We want to specify liveness for our FSP models***
- ***We want to analyze our FSP models to be certain that the liveness properties hold***
- ***General form of liveness requires consideration of temporal precedence relationship between states***
- ***We use more restricted form of progress***



Progress

- ***A progress property asserts that whatever state a system is in, it is always the case that a specified action will eventually be executed***
- ***Progress is the opposite form of starvation***
- ***Notion of progress is sufficiently powerful to capture wide range of liveness properties***
- ***Progress properties are simple to specify in FSP***



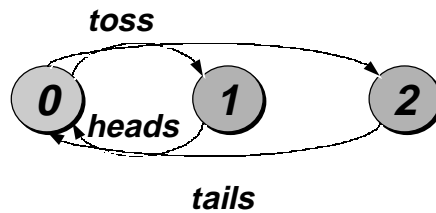
Progress Properties in FSP

- ***Specification of progress needs assumption of a fair scheduling policy.***
- ***If a transition from a set is chosen infinitely often and every transition in the set will be executed infinitely often, the scheduling policy is said to be fair.***
- ***progress $P = \{a_1, a_2, \dots, a_n\}$ defines a progress property P which asserts that in an infinite execution at least one of the actions a_1, a_2, \dots, a_n will be executed infinitely often.***



Example: Tossing Coins

```
COIN = ( toss -> heads -> COIN
        | toss -> tails -> COIN ).
toss
```

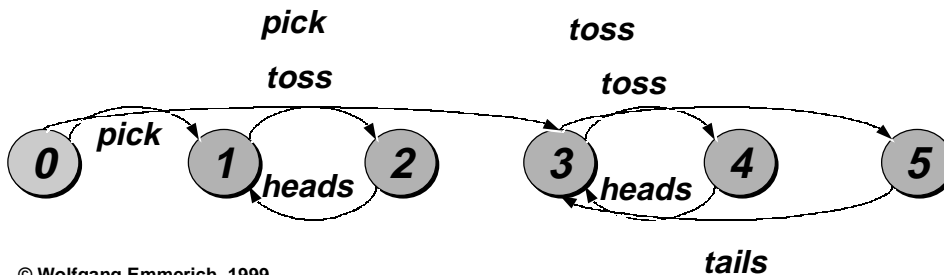


```
progress HEADS = {heads}
progress TAILS = {tails}
```



Example: Tossing Trick Coins

```
TWOCOIN = (pick->COIN | pick->TRICK),
COIN     = (toss -> heads -> COIN
            | toss -> tails -> COIN),
TRICK    = (toss->heads->TRICK).
progress HEADS = {heads}
progress TAILS = {tails}
```





Progress Analysis

- ***We can automate analysis of progress properties***
- ***A set of states where every state is reachable from every other state in the set and no state has transitions to states outside the set is a terminal set of states.***
- ***Terminal set of states can be found using a graph algorithm that searches for a strongly connected component.***

LTSA



Default Progress Properties

- ***Default progress properties assert in a system with fair choices that every action in the alphabet will be executed infinitely often.***
- ***Default progress properties of example:***
 - `progress p1 = {pick}`
 - `progress p2 = {toss}`
 - `progress p3 = {heads}`
 - `progress p4 = {tail}`
- ***How many violations?***

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Priorities

- *Default progress analysis of single lane bridge does not reveal violation.*
- *Problem is scheduling policy. Cars arriving in the south get 'priority' if there are already northbound cars on the bridge*
- *To detect such progress violations we have to reflect such priorities in the FSP model*

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High Priority in FSP

- $P \mid Q \ll \{a_1, \dots, a_n\}$ *specifies a composition in which the actions a_1, \dots, a_n have higher priority than any other action in the alphabet of $P \mid Q$ including the silent action τ . In any choice in this system which has one or more of the actions a_1, \dots, a_n labelling a transition, the transitions labelled with lower priority actions are discarded.*



Low Priority in FSP

- $||C = (P || Q) >> \{a_1, \dots, a_n\}$ specifies a composition in which the actions a_1, \dots, a_n have lower priority than any other action in the alphabet of $P || Q$ including the silent action τ . In any choice in this system which has one or more transitions not labelled by a_1, \dots, a_n , the transitions labelled by a_1, \dots, a_n are discarded.



Simplification of LTS

- Priorities simplify the LTS resulting of the composition.
- Example:
NORMAL = (work -> play -> NORMAL
 | sleep -> play -> NORMAL) .
|| HIGH = (NORMAL) << {work} .
|| LOW = (NORMAL) >> {work} .
- Use of priorities lead to more realistic liveness checks.

LTSA



Summary

- *Liveness*
- *Progress*
- *Progress Specification in FSP*
- *Progress-Analysis of LTS*
- *Priorities*