

COMP1008

Implementing Data Structures

Lists

Outline

- Classes and abstract data types.
- Iterators
- List Elements
- Lists
- Note – here we deal only with the implementation of data structures. 1b12 and 1b13 cover the properties of data structures.

A Class as a Data Abstraction

```
class Pair
{
    private int x ;
    private int y ;
    ...
    public Pair(int a, int b)
    { ... }
    ...
}
```

A new data abstraction is created here.

Also a new type.

Using a class...

```
...
Pair p = new Pair(1, 3) ;
Pair q = new Pair(34, -23) ;
...
```

- A Pair can now be directly used, rather than having to manage two separate variables.
- Pair is (a bit) more abstract and hides unwanted detail that would otherwise intrude.

Data Abstraction

- We know a class declaration creates a User Defined Type.
- We can also use a class as an *implementation* of a data abstraction or data type.
- An Abstract Data Type (ADT) provides a specification of a data type.

Abstract Data Types (ADTs)

- An abstract data type is:
 - A set of values.
 - A set of operations relating values of the type.
 - Specified formally (mathematically).
- An abstract data type description is abstract (!).
- It does not specify representation or algorithm.
 - Only behaviour.

A Stack ADT

Stack<T>

operations:

create: \rightarrow Stack

push: $\text{Stack}\langle T \rangle \times T \rightarrow \text{Stack}\langle T \rangle$

pop: $\text{Stack}\langle T \rangle \rightarrow \text{Stack}\langle T \rangle \times T$

top: $\text{Stack}\langle T \rangle \rightarrow T$

isEmpty: $\text{Stack}\langle T \rangle \rightarrow \text{Boolean}$

Parameterised Type:
Stack of T
(T is a type variable)

Operation
signatures
(types)

A Stack ADT (2)

Stack

axioms:

isEmpty(create) = true

isEmpty(push(s, e)) = false

top(create) = EXCEPTION

top(push(s, e)) = e

pop(create) = EXCEPTION

pop(push(s, e)) = (s, e)

Behavioural
specification

push(s, e) means push
value e on stack s,
returns a stack.

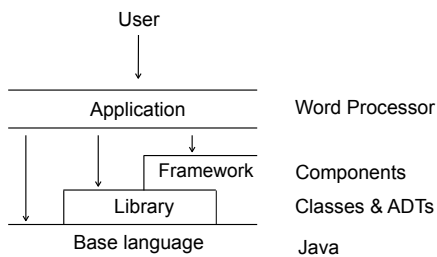
Abstract Data Types and Classes

- A class can be used to provide an *implementation* that *conforms* to an ADT specification.
- Typically ADTs are associated with data structures.
 - Collections or Containers.
 - Collections are objects that act as containers in which other objects (or really object references) are stored.
 - List, Tree, ArrayList, Graph, Hash Table, etc.

Why abstract?

- Abstraction builds on the idea of using lower-level concepts to implement higher level constructs.
- These higher level concepts effectively extend the language by introducing new features to the language (via new classes).
- Thus, we are raising the level of the language we are using.
 - Important principle, don't want to do everything at the lowest level.

Abstraction Layers



Questions?

Implementing a container

- Obviously use a class...
- Need a data structure to store contained *object references*:
 - one or more instance variables (private of course).
- Need algorithms to implement access operations as methods.

Implementation properties

- Need to consider:
 - Memory use.
 - Speed of operation.
- Typically trading off one property against another.
- Need to select implementations that match the needs of your program.
 - Typically have several implementations, conforming to the same interface for same abstraction.
 - List -> ArrayList, LinkedList.

Iterators

- Every container class has to provide a mechanism for accessing each element in sequence.
- Such a mechanism is called an *iterator*.
- Algorithms such as linear searching, comparison, function application depend on use of iterators.
- An iterator aims to decouple element access from container implementation.

Iterator Protocol

- Ideally we want a common iterator protocol across all of our container classes.
 - Make Iteration look the same for all container classes.
- Java provides a Collections Framework that includes various container classes and provides Iterator as the iterator protocol.

Familiar container - the Array!

- An array is a container but it is primitive and there is no class Array* (although arrays are actually objects).
- An array is a collection of items of the same type.
- The number of items is fixed.
- Efficient but low-level abstraction.
- *OK, there is a class Array but it is a collection of static utility methods.

Array Iteration

```
int[] array = new int[42];
for (int j = 0; j < array.length; j++)
{
    doSomething(array[j]);
}
```

Array indexing.
Depends on integer
index mapping to
element.

```
for (int n : array.length)
{
    doSomething(n);
}
```

Enhanced for loop.
More generic and will
work for other
containers that cannot
be indexed by integers.

Iterator Objects

- General abstraction of iteration.

```
ArrayList<String> a = new ArrayList<String> ();
...
for (Iterator<String> i = a.iterator(); i.hasNext(); )
{
    doSomething(i.next());
}
```

Iterator object stores state of iteration and gives access to next object reference.

Ask ArrayList object for an iterator.

Iterator v. Enhanced For Loop

- The enhanced for loop actually uses iterator objects.
 - Loop syntax mapped to creating/using iterator.
 - Works properly with nested loops.
- Container class should implement *Iterable* interface to work with enhanced for:


```
interface Iterable<E> {
    Iterator<E> iterator();
}
```

 - Call iterator method to get iterator object.
 - Container class responsible for provide correct iterator that works with its representation.

Iterator

- Type Iterator declared as an interface.

```
public interface Iterator<E>
{
    boolean hasNext();
    E next();
    void remove(); // May not be supported by
                  // implementing class
}
```

Interface Reminder

- An interface declares a collection public methods.
 - All methods are abstract - no method bodies.
 - No instance variables.
 - A class implements an interface and must override the methods.
 - (Like an abstract class declaring only abstract methods.)

Iterator Class

```
class MyIterator<E> implements Iterator<E>
{
    // Must override methods
    // declared in the interface.
}
```

- An iterator object allows each value in a collection to be visited in turn (iterated).
- A variable of type Iterator can reference an object of an implementing class.
- Iterator<String> iterator = new MyIterator<String>(...);

Iterating

```
public <E> void print(Iterator<E> iterator)
{
    while (iterator.hasNext())
    {
        System.out.println(iterator.next());
    }
}
```

Programming to an interface.

- Can print contents of any data structure that can provide an Iterator implementation.
- Class of actual iterator object does not need to be known.

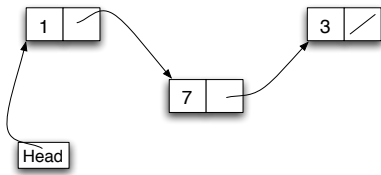
Iterator classes

- Typically declared as a nested class.
 - Inside (member of) a container class.
 - In the container class scope, so has access to private data.
 - Iterator object can access container object to get data.
 - Examples later.

Questions?

Linked Lists

- A linked list is implemented as a chain of linked elements (objects).

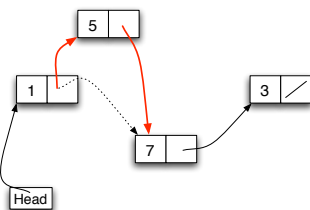


Linked Lists

- Each element or node consists of a stored value and a reference to the next element.
- A reference is maintained to the head of the list.
- An individual element is located by following the chain from the head.
 - Sequential access.
- Elements in a list (or vector, or array) are stored in sequence.
- Accessing elements relies on the sequence.
- A list is a *sequence container*.

Inserting/Removing a Value

- An element is inserted or removed by manipulating links.
- There is no need to shift other elements to add/remove space.



- Head/End are special cases.

List v. LinkedList v. ListElement

- To implement a LinkedList class we will have:
 - interface List<E>, defining public methods that all kinds of lists have.
 - class LinkedList<E>, defining a list implementation using a chain of elements.
 - class ListElement<E>, defining a list element used by LinkedList
 - ListElement will be part of the *private* implementation of LinkedList.
 - Not accessible externally.

List<E> Interface

```
public interface List<E> extends Iterable<E> {
    void insertHead(E val);
    E getHead();
    List<E> getTail();
    boolean isEmpty();
}
```

Extend the Iterable interface, so our Lists will provide a standard iterator.

Plus Iterator<E> iterator() inherited from Iterable.

List Element<E>

Nested in class LinkedList.

```
private static class ListElement<T> {
    public ListElement<T> next;
    public T val;
    public ListElement(ListElement<T> next, T val) {
        this.next = next;
        this.val = val;
    }
    public ListElement<T> copy() {
        return new ListElement<T>(next == null ? null : next.copy(), val);
    }
}
```

This is a *private* infrastructure class so *val* and *next* are public, and can be directly accessed in class LinkedList.

Helper method for copying chain of elements.

Using ListElements

- If a version of ListElement<T> is made a top level class, it could be used to created chains of objects directly.
 - Without a LinkedList class.
- Would need to provide methods to use the chain (add, remove, search, etc.).
- Useful where a full LinkedList class is not needed.

LinkedList<E>

```
public class LinkedList<E> implements List<E> {
    private ListElement<E> head;
    private static class ListElement<T> { // As seen on previous slide)
    public LinkedList() {
        head = null;
    }
    private LinkedList(ListElement<E> e) {
        head = e;
    }
    public void insertHead(E val) {
        head = new ListElement<E>(head, val);
    }
}
```

Private constructor is useful for LinkedList implementation but not meant to be used publicly.

LinkedList<E> (2)

```
public E getHead() {
    if (head == null) { return null; }
    else { return head.val; }
}
public List<E> getTail() {
    if ((head == null) || (head.next == null)) {
        return new LinkedList<E>();
    }
    return new LinkedList<E>(head.next.copy());
}
public boolean isEmpty() {
    return head == null;
}
```

Note that tail of list is copied.

List Iterator

- To provide an iterator, LinkedList should create and return an Iterator object.
 - Iterator knows how to access elements from the LinkedList implementation.
 - Iterator class will be another nested member class to have access to the LinkedList class scope.
 - Implements the Iterator interface, so will be a standard kind of iterator.

Getting an Iterator

- Ask the LinkedList:


```
public Iterator<E> iterator() {
    return new LinkedListIterator<E>(head);
}
```
- Declared in class LinkedList.
- Can have multiple iterators active at same time.
- But if list changes during iteration, iterator may break.
 - Unless a more sophisticated implementation is used.

LinkedListIterator

```
private class LinkedListIterator<T>
implements Iterator<E> {
    private ListElement<E> current =
        new ListElement<E>(head,null);
    public LinkedListIterator(ListElement<E> e) {
        current = e;
    }
    public boolean hasNext() {
        return (current != null)
            && (current.next != null);
    }
    public E next() {
        if (current != null) {
            current = current.next;
            return current.val;
        }
        return null;
    }
}

public void remove()
{
    throw new UnsupportedOperationException();
}
```

Remove is declared
in Iterator interface
so must be
implemented. But is
not supported so
throws an exception.

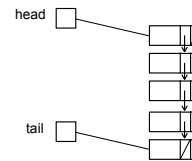
Another nested
member class.

Linked List Properties

- Inserting/removing at beginning.
- Insertion/removal in middle can be fast once the location is found.
- But there is the potential cost of linear access – $O(n)$.
- Good for situations when elements are repeatedly inserted and deleted.
 - And where linear access is required.
 - And where number of elements is unknown or changes frequently.

Double-Link List

- Links in both directions.
- Head and tail references.
- Some algorithms easier to implement but extra storage cost for each element.



Inserting?

- Provided a “Lisp style” list that provides head/tail operations.
 - car & cdr functions
 - Natural for divide & conquer style recursive algorithms.
 - Search the web for more about Lisp.
- But what about inserting elements at any position in the list?

Insert Iterator

```
private class LinkedListInsertIterator<T>
extends LinkedListIterator<E>
implements InsertIterator<E> {
    private ListElement<E> last = current;
    public void insert(E value) {
        if (head == null) {
            insertHead(value);
            current = new ListElement<E>(head,null);
            return;
        }
        if (current != null) {
            current.next = new ListElement<E>(current.next,value);
        }
    }
}
```

Summary

- Lists are a basic data structure build from chains of elements.
 - Exploits properties of references (pointers).
 - Not fixed size, can grow and shrink.
 - Suitable where data structure size changes frequently.
 - But $O(n)$ sequential access.
 - Start from head and search.
 - Not good good for searching/sorting.