1. The RSA Public-Key Cryptosystem

Your colleague tells you that two TLS-enabled web servers $S_1$ and $S_2$ that use RSA in their TLS cipher suites have RSA public keys whose RSA moduli $n_1$ and $n_2$ satisfy $\gcd(n_1, n_2) > 1$. She does not, however, tell you what the common divisor is. The two TLS-enabled web servers have followed the usual algorithm for RSA key generation. Describe in full detail a tractable calculation you can perform (i.e., a calculation that will run in time on the order of less than days) that will reveal both
these two web servers’ RSA private keys. Be sure to justify your answer by explaining the relevant
details of the RSA cryptosystem.

[10 marks]

2. Format String Vulnerabilities
You and your friend discover a format string vulnerability in a popular server, and decide to write
an exploit for it that will make the server crash. An excerpt of the C source code for the function
containing the vulnerability follows:

```c
int vulnerable(void)
{
    char userinput[1024];
    ...
    sprintf(outstr, userinput);
    ...
}
```

Both `outstr` and `userinput` are of type `char *`. Each of these two pointers is four bytes in
length. `userinput` is a string that the server reads directly from a network socket (i.e., the content
of the string will be taken unmodified from within a request you can send the server). Assume that
`outstr` is extremely large, such that you can be certain you won’t overflow it, no matter how
many characters are printed by `sprintf()` during the processing of your exploit.

Your friend analyzes the behavior of the server, and determines the following facts:

- When the vulnerable server software is run under the version of Linux used on the server
  you wish to target with your exploit, inside the function `vulnerable()`, the return address
  for resuming execution in `vulnerable()`’s caller is stored on the stack at memory address
  `0xbfff8218`.
- When `sprintf()` begins processing the format string `userinput`, its “next argument to
  print” pointer points to a memory location that is exactly 48 bytes lower in memory than the
  location of the buffer `userinput`.

Assume that memory address `0xdeadbeef` is unmapped in the server process, so that if execution
at this address is attempted, the server will crash.

Design and supply the exact format string that, when placed verbatim by the server into `userinput`,
will cause the server to crash by attempting execution at address `0xdeadbeef` when the function
`vulnerable()` returns. Provide diagrams of the stack showing the steps in the execution of your
format string exploit.

N.B. that you should not use a buffer overflow vulnerability in your answer—you must use a format
string vulnerability only.

[10 marks]

3. TAOS Applied to SSL/TLS and NFS
In the assigned reading on TAOS, the authors describe how to use logical statements to model
authentication in distributed systems formally.
(a) Suppose that Alice uses a web browser on her desktop computer to place an order with amazon.com. The communication between her browser and amazon.com’s web server uses SSL/TLS 3.0, with RSA authentication (as described in class during the SSL/TLS lecture).

Using the notation and axioms defined in Section 2.1 of the TAOS paper, write out a formal derivation that proves that Alice’s web browser can trust that a response RSP received over the SSL/TLS channel from amazon.com’s SSL/TLS web server was sent by the real company Amazon.com, Inc. (Assume that Amazon.com, Inc. has registered a public key with an SSL/TLS certification authority trusted by Alice’s web browser, in the usual way.) Your derivation should conclude with the statement:

Amazon.com, Inc. says RSP

[7 marks]

(b) In a completely different context, consider an NFS deployment enhanced to use TAOS for user authentication, where each RPC request from a client workstation is authenticated by the NFS server in the exact fashion illustrated in Section 2.2 of the assigned TAOS reading.

Suppose an attacker, Mallet, wishes to gain access to Bob’s files stored on the NFS server. To do so, Mallet installs an unmodified but outdated version of the OS on Bob’s client workstation. Mallet happens to know that this version of the OS contains a vulnerability that will allow him to inject malicious code into the OS kernel while Bob is logged in and accessing his files over NFS. Mallet can thus inject malicious code into the kernel that sends Mallet a copy of the data for Bob’s files (since the file data are fully visible to the kernel while Bob is logged in and using his files).

Assume that TAOS is willing to boot any unmodified, released version of the OS on a workstation, including outdated ones.

Even so, TAOS provides adequate mechanisms to prevent Mallet’s attack from succeeding. Explain exactly what mechanisms TAOS provides to thwart this attack, and how Bob or the NFS server administrator should configure TAOS’s authentication functionality on the NFS server to do so.

Hint: as stated in the assigned reading on TAOS, the boot firmware of a workstation can accurately determine the OS revision it is booting . . .

[3 marks]

4. Kerberos

Kerberos Version 4 (the version of the protocol in the paper assigned for class) uses authenticators to protect against replay attacks.

Suppose that all nodes in a Kerberos realm have properly synchronized clocks, and that the clock synchronization system is secure against an adversary’s manipulation of any node’s clock.

The MIT Athena Kerberos deployment honored a Kerberos authenticator for 5 minutes beyond the timestamp within the authenticator. An eavesdropper could thus replay an overheard ticket and authenticator for five minutes, given that servers in this deployment didn’t cache past authenticators to ensure they weren’t reused.
(a) Describe an alternate, bidirectional protocol between server and client to replace the authenti-
cator that prevents such replay attacks, and requires no new keys beyond those already in use
in the Kerberos system. Your design must not require caching more than a constant amount
of state per Kerberos principal on the server.

[4 marks]

(b) Read the Appendix of the assigned reading on Kerberos, which describes the authors’ Ker-
berized NFS implementation. In this design, NFS does not include a Kerberos ticket and
authenticator in every NFS request from the client workstation to the server. When does the
user’s client workstation authenticate the user to the NFS server in this design, and how?

[3 marks]

(c) TAOS allows delegation: a user may delegate authority to a workstation acting on his behalf,
and that workstation may in turn delegate authority to another workstation, acting on behalf
of the same user. Does Kerberos support this kind of delegation? That is, can a user on
workstation A obtain a ticket granting access to a service on some server, and forward that
ticket as-is to another workstation, for use by that other workstation when requesting services
from the same server? Why or why not?

[3 marks]

5. SSL

When SSL 3.0 uses RSA authentication during the handshake at the start of the SSL connection, it
doesn’t provide forward secrecy. Describe a modification to the SSL 3.0 handshake (still only using
RSA during the handshake—you may not introduce additional ciphers not discussed in lecture!) that will provide forward secrecy. Please show a timeline for your modified SSL handshake (of
the form of the one given in lecture), indicating the interleaving of messages sent and received
by the client and server, the contents of each message, and showing when the client and server
execute any other operations required to implement your modification correctly. What, if any, are
the added costs of your solution over those of the “basic” RSA SSL handshake? Hint: consider
what fundamental property the key the server uses to decrypt the pre-master secret must have for
forward secrecy to hold.

[10 marks]

Problem set total: 50 marks